Experimental (n,γ) cross sections of the *p*-process nuclei ⁷⁴Se and ⁸⁴Sr

I. Dillmann,* M. Heil, and F. Käppeler

Institut für Kernphysik, Forschungszentrum Karlsruhe, Postfach 3640, D-76021 Karlsruhe, Germany

T. Rauscher and F.-K. Thielemann

Departement Physik und Astronomie, Universität Basel, Klingelbergstrasse 82, CH-4056 Basel, Switzerland

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The nucleosynthesis of elements beyond iron is dominated by the s and r processes. However, a small amount of stable isotopes on the proton-rich side cannot be made by neutron capture and are thought to be produced by photodisintegration reactions on existing seed nuclei in the so-called "p process". So far most of the p-process reactions are not yet accessible by experimental techniques and have to be inferred from statistical Hauser-Feshbach model calculations. The parametrization of these models has to be constrained by measurements on stable proton-rich nuclei. A series of (n,γ) activation measurements, related by detailed balance to the respective photodisintegrations, were carried out at the Karlsruhe Van de Graaff accelerator using the ⁷Li $(p,n)^7$ Be source for simulating a Maxwellian neutron distribution of kT = 25 keV. First results for the experimental (n,γ) cross sections of the light p nuclei ⁷⁴Se and ⁸⁴Sr are reported. These experimental values were used for an extrapolation to the Maxwellian averaged cross section at 30 keV, $\langle \sigma \rangle_{30}$, yielding 271±15 mb for ⁷⁴Se, and 300±17 mb for the total capture cross section of ⁸⁴Sr. The partial cross section to the isomer in ⁸⁵Sr was found to be 190±10 mb.

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I. INTRODUCTION

Astrophysical models can explain the origin of most nuclei beyond the iron group in a combination of processes involving neutron captures on long (s process) or short (r process) time scales [1, 2]. However, 32 stable, proton-rich isotopes between ⁷⁴Se and ¹⁹⁶Hg cannot be formed in that way. Those p nuclei are 10 to 100 times less abundant than the s and r nuclei in the same mass region. They are thought to be produced in the so-called γ or p process, where proton-rich nuclei are made by sequences of photodisintegrations and β^+ decays [3, 4, 5]. In this scenario, pre-existing seed nuclei from the s and rprocesses are destroyed by photodisintegration in a hightemperature environment, and proton-rich isotopes are produced by (γ, n) reactions. When (γ, p) and (γ, α) reactions become comparable or faster than neutron emission within an isotopic chain, the reaction path branches out and feeds nuclei with lower charge number Z. The decrease in temperature at later stages of the p process leads to a freeze-out via neutron captures and mainly β^+ decays, resulting in the typical *p*-process abundance pattern with maxima at 92 Mo (N=50) and 144 Sm (N=82).

The currently most favored astrophysical site for the p process is explosive burning in type II supernovae. The explosive shock front heats the outer O/Ne shell of the progenitor star to temperatures of 2-3 GK, sufficient for

providing the required photodisintegrations. Following the nucleosynthesis in such astrophysical models, good agreement with the required p production is found, with exception of the low (A<100) and intermediate ($150 \le A \le$ 165) mass range, which are underproduced by factors of 3-4 [6]. Because of these persisting problems, alternative scenarios (such as type Ia supernovae and X-ray bursters) have been suggested, each with their own, inherent difficulties [7, 8, 9]. Currently, however, it is not yet clear whether the observed underproductions are due to a problem with astrophysical models or with the nuclear physics input, i.e. reaction rates. Thus, a necessary requirement towards a consistent understanding of the pprocess is the reduction of uncertainties in nuclear data. By far most of the several hundreds of required photodisintegration rates and their inverses need to be inferred from Hauser-Feshbach statistical model calculations [10], e.g. the codes NON-SMOKER [11, 12, 13] and MOST [14, 15]. Experimental data can improve the situation in two ways, either by directly replacing predictions with measured cross sections in the relevant energy range, or by testing the reliability of predictions at other energies when the relevant energy range is not experimentally accessible.

The role of (n,γ) reactions in the p process was underestimated for a long time, although it is obvious that they have an influence on the final p-process abundances. Neutron captures compete with (γ,n) reactions and thus hinder the photodisintegration flux towards light nuclei, especially at lower-Z isotopes and even-even isotopes in the vicinity of branching-points. The influence of a variation of reaction rates on the final p abundances has

^{*}Electronic address: iris.dillmann@ik.fzk.de; also at Departement für Physik und Astronomie, Universität Basel.

been studied previously [16, 17]. It turned out that the p abundances are very sensitive to changes of the neutron-induced rates in the entire mass range, whereas the proton-induced and α -induced reaction rates are important at low and high mass numbers, respectively.

Rayet et al. [18] have also studied the influence of several components in their *p*-process network calculations. Their nuclear flow schemes show that branching points occur even at light p nuclei, and are shifted deeper into the proton-rich unstable region with increasing mass and temperature. In contradiction to Woosley and Howard [3], who claimed for their network calculations that (n, γ) can be neglected except for the lightest nuclei $(A \leq 90)$, Rayet et al. also examined the influence of neutron reactions for temperatures between $T_9 = 2.2$ and 3.2 GK by comparing overabundance factors if (n, γ) reactions on Z>26 nuclides are considered or completely suppressed. As a result, the overabundances were found to change by up to a factor 100 (for ⁸⁴Sr) if the (n,γ) channel was artificially suppressed. This rather high sensitivity indicates the need for reliable (n,γ) rates to be used in *p*-process networks.

Although recent efforts are directed to calculation or measurement of photodisintegration cross sections and rates [19, 20, 21, 22, 23, 24, 25], astrophysical photodisintegration rates can easily be inferred from capture rates by detailed balance, even in theoretical work [12]. The stellar reaction rate $N_A < \sigma v >^*_{n,\gamma}$ for the reaction $a + n \rightarrow b + \gamma$ is related to its inverse rate by

$$N_A < \sigma \upsilon >_{\gamma,n}^* = \frac{(2J_a+1)(2J_n+1)}{2J_b+1} \sqrt{\left(\frac{A_a}{A_b}\right)^3} \times \frac{G_a(T)}{G_b(T)} exp\left(-\frac{Q_{n,\gamma}}{kT}\right) N_A < \sigma \upsilon >_{n,\gamma}^* (1)$$

with the Avogadro number N_A , the nuclear spins J and masses A, the respective temperature-dependent partition functions G(T) and the reaction Q value in the exponent. Measuring or calculating a rate in the direction of positive Q value ensures best numerical accuracy and consistency between forward and backward reaction. This is important when implementing those rates in reaction networks for nucleosynthesis models.

Moreover, stellar cross sections and rates have to be employed for the computation of reverse rates. In a stellar environment, nuclei are fully thermalized with the environment, resulting in a thermal excitation of both the target and the final nucleus. Only stellar cross sections including the excitation in form of a stellar enhancement factor (SEF) can be used to properly account for all transitions when applying detailed balance. For reactions with positive Q values for captures, a laboratory measurement of the capture cross section will encompass by far more of the relevant transitions than a photodisintegration experiment, even with the target being in the ground state [20].

For the past decade there has been a continuing effort to measure nuclear data for the p process, both for

charged particle reactions [17, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38] and for neutron induced reactions [17, 35, 39, 40, 41]. The present work comprises the first measurement of (n,γ) cross sections for the *p*-process isotopes ⁷⁴Se and ⁸⁴Sr at kT=25 keV, with the aim to improve the *p*-process database and to help testing theoretical predictions. Since it is not possible to measure cross sections directly at *p*-process temperatures of kT=170-260 keV, we have to perform the measurements at *s*-process (and freeze-out) temperatures of kT= 25 keV, and then extrapolate theoretically by means of the respective energy dependent cross sections (see Sec. V).

The measurement of stellar (n,γ) rates requires a "stellar" neutron source yielding neutrons with a Maxwell-Boltzmann energy distribution. We achieve this by making use of the ${}^{7}\text{Li}(p,n){}^{7}\text{Be}$ reaction. In combination with the activation or time-of-flight technique, this offers a unique tool for comprehensive studies of (n,γ) rates and cross sections for astrophysics.

In Sec. II, the experimental technique and sample characteristics are outlined, followed by the description of the data analysis in Sec. III. The results are presented in Sec. IV. A comparison to theory and extrapolation to higher energies is given in Sec. V. The paper is concluded with a summary and a short outlook in Sec. VI.

II. EXPERIMENTAL TECHNIQUE

All measurements were carried out at the Karlsruhe 3.7 MV Van de Graaff accelerator using the activation technique. Neutrons were produced with the ⁷Li(p,n)⁷Be source by bombarding 30 μ m thick layers of metallic Li on a water-cooled Cu backing with protons of 1912 keV, 30 keV above the reaction threshold. The resulting quasistellar neutron spectrum approximates a Maxwellian distribution for $kT = 25.0 \pm 0.5$ keV [42]. Hence, the proper stellar capture cross section can be directly deduced from our measurement.

For the activations natural samples of selenium metal (0.89% ⁷⁴Se) and various strontium compounds (0.56%⁸⁴Sr) were used. In order to verify the stoichiometry, samples of $Sr(OH)_2$ and SrF_2 were dried at 300°C and 800°C, respectively. The powders were pressed to thin pellets, which were enclosed in a 15 μ m thick aluminium foil and sandwiched between 10-30 μ m thick gold foils of the same diameter. In this way the neutron flux can be determined relative to the well-known capture cross section of ¹⁹⁷Au [42]. The activation measurements were carried out with the Van de Graaff accelerator operated in DC mode with a current of $\approx 100 \ \mu$ A. The mean neutron flux over the period of the activations was $\approx 1.5 \times 10^9$ n/s at the position of the samples, which were placed in close geometry to the Li target. Throughout the irradiation the neutron flux was recorded in intervals of 1 min using a ⁶Li-glass detector for later correction of the number of nuclei, which decayed during the activation (factor f_b in Eq. 4).

Over the course of the present measurements, a total of 17 activations (5 for Se and 12 for Sr) have been carried out with modified experimental parameters (see Table I). Five short-time activations of 3 h to 5 h were used for determining the partial cross section of the ${}^{84}\text{Sr}(n,\gamma){}^{85}\text{Sr}^m$ reaction feeding the isomer in ${}^{85}\text{Sr}$ with a half-life of 67.6 m. The ${}^{84}\text{Sr}(n,\gamma){}^{85}\text{Sr}^g$ cross section to the ground state was separately deduced from seven long-time activations.

TABLE I: Activation schemes and sample characteristics. The suffix "m" denotes short time activations for measurements of the partial cross section to the ${}^{85}\text{Sr}^m$ isomeric state. Φ_{tot} gives the neutron exposure of the sample during the activation.

Sample	Ø	Mass	Atoms	t_a	Φ_{tot}
No.	[mm]	[mg]	$^{74}\mathrm{Se}$ or $^{84}\mathrm{Sr}$	[h]	[neutrons]
Se					
se-1	6	151.8	1.03×10^{19}	16	1.10×10^{14}
se-2	10	200.2	1.36×10^{19}	7	1.53×10^{13}
se-3	6	102.2	6.94×10^{18}	23	1.64×10^{14}
se-4	10	207.8	1.41×10^{19}	24	0.99×10^{14}
se-5	10	147.8	1.00×10^{19}	24	1.16×10^{14}
$Sr(OH)_2$					
sr-1	6	67.6	1.88×10^{18}	23	1.45×10^{14}
sr-2	10	161.2	4.47×10^{18}	25	8.03×10^{13}
$sr-3^a$	6	119.8	3.32×10^{18}	21	1.59×10^{14}
sr-4m	6	147.5	4.09×10^{18}	3	1.13×10^{13}
sr-5m	10	195.3	5.42×10^{18}	3	2.27×10^{13}
\mathbf{SrF}_2					
sr-6	10	478.3	1.28×10^{19}	24	1.16×10^{14}
sr -7 ^b	10	195.7	5.25×10^{18}	43	1.31×10^{14}
sr-8m	8	204.5	5.49×10^{18}	4	3.29×10^{13}
sr-9m	10	314.4	8.44×10^{18}	5	2.77×10^{13}
$SrCO_3$					
sr-10	8	91.2	2.08×10^{18}	21	1.64×10^{14}
sr-11	10	152.1	3.47×10^{18}	21	9.30×10^{13}
sr-12m	8	222.6	5.09×10^{18}	3	1.91×10^{13}

^{*a*}Heated at 300° C for 4 h.

^bHeated at 800°C for 1 h.

III. DATA ANALYSIS

A. General procedure

The induced γ -ray activities were counted after the irradiation in a well defined geometry of 76.0 ± 0.5 mm distance using a shielded HPGe detector in a low background area. Energy and efficiency calibrations have been carried out with a set of reference γ -sources in the energy range between 60 keV and 2000 keV. Fig. 1 shows the γ -ray spectra of the induced activities in the ⁷⁴Se and ⁸⁴Sr samples.

The total amount of activated nuclei Z at the end of the irradiation can be deduced from the number of events C in a particular γ -ray line registered in the HPGe detector during the measuring time t_m [47]. The factor t_w corresponds to the waiting time between irradiation and activity measurement.

$$Z = \frac{C(t_m)}{\varepsilon_{\gamma} I_{\gamma} k_{\gamma} (1 - e^{-\lambda t_m}) e^{-\lambda t_w}}$$
(2)

The factors ε_{γ} and I_{γ} account for the HPGe efficiency and the relative γ intensity per decay of the respective transition (Table II). The factor k_{γ} introduces the correction for γ -ray self-absorption in the sample [47]. For disk shaped samples with a thickness d and γ -ray absorption coefficients μ [48], one obtains

$$k_{\gamma} = \frac{1 - e^{-\mu d}}{\mu d}.$$
(3)

The factor

$$f_b = \frac{\int_0^{t_a} \phi(t) \ e^{-\lambda(t_a - t)} \ dt}{\int_0^{t_a} \phi(t) \ dt}$$
(4)

accounts for the decay of activated nuclei during the irradiation time t_a as well as for variations in the neutron flux. This factor can be calculated from the neutron flux history recorded throughout the irradiation with the ⁶Li glass detector in 91 cm distance from the target.

The number of activated nuclei ${\cal Z}$ can also be written as

$$Z(i) = N_i \ \sigma_i \ \Phi_{tot} \ f_b(i), \tag{5}$$

where $\Phi_{tot} = \int \phi(t) dt$ is the time-integrated neutron flux and N_i the number of atoms in the sample. As our measurements are carried out relative to ¹⁹⁷Au as a standard, the neutron flux Φ_{tot} cancels out:

$$\frac{Z(i)}{Z(Au)} = \frac{\sigma_i \ N_i \ f_b(i)}{\sigma_{Au} \ N_{Au} \ f_b(Au)}$$
$$\iff \sigma_i = \frac{Z(i) \ \sigma_{Au} \ N_{Au} \ f_b(Au)}{Z(Au) \ N_i \ f_b(i)}.$$
(6)

The reference value for the experimental ¹⁹⁷Au cross section in the quasi-stellar spectrum of the ⁷Li(p,n)⁷Be source is 586±8 mb [42]. By averaging the induced activities of the gold foils, one can determine the neutron flux Φ_{tot} at the position of the sample and deduce the experimental cross section σ_i of the investigated sample as shown in Eq. 6.

B. Ground-state correction

In the case of the activation of ⁸⁴Sr, where the neutron capture populates both, ground and isomeric state in ⁸⁵Sr, the analyzing procedure is more complicated. While the partial cross section to the isomeric state can be easily calculated as described above, the partial cross

TABLE II: Decay properties of the product nuclei. Shown here are only the strongest transitions, which were considered for analysis. Isotopic abundances are from Ref. [43].

Reaction	Isot. abund. $[\%]$	Final state	Half life	$E_{\gamma} [keV]$	I_{γ} [%]	Ref.
74 Se(n, γ) 75 Se	0.89 ± 0.04	Ground state	119.79 \pm 0.04 d	136.0	58.3 ± 0.7	[44]
				264.7	58.9 ± 0.3	
${}^{84}\mathrm{Sr}(\mathrm{n},\gamma){}^{85}\mathrm{Sr}$	0.56 ± 0.01	Ground state	$64.84\pm0.02~{\rm d}$	514.0	95.7 ± 4.0	[45]
		Isomer	67.63 \pm 0.04 m	151.2 (EC)	12.9 ± 0.7	
				231.9 (IT)	84.4 ± 2.2	
$^{197}\mathrm{Au}(\mathrm{n},\gamma)^{198}\mathrm{Au}$	100	Ground state	$2.69517 \pm 0.00021 \ \mathrm{d}$	411.8	95.58 ± 0.12	[46]



FIG. 1: Decay spectra of the activated Se and Sr samples. The Se spectra shows also the γ -lines at 121 keV, 280 keV and 401 keV, which were not considered for analysis.

section to the ground state has to be corrected for those nuclei, which decayed during activation and measuring time already by isomeric transition.

The amount of isomer and ground state nuclei after the activation time t_a is described by Eq.7:

$$Z_m(t_a) = N \ \sigma_m \ \Phi_{tot} \ f_m^b \tag{7}$$

$$Z_g(t_a) = N \Phi_{tot} (\sigma_g f_g^b + Y \sigma_m \lambda_m g_m).$$
(8)

Y is the branching ratio of the isomeric transition (0.866 for ${}^{85}\mathrm{Sr}^m$), and the factor \mathbf{g}_m is calculated with:

$$g_m = \frac{\int_0^{t_a} e^{-\lambda_g(t_a-t)} dt \int_0^t \phi(t^*) e^{-\lambda_m(t-t^*)} dt^*}{\int_0^{t_a} \phi(t) dt}.$$
 (9)

The relation between the activity of the ground state and the measured count rate C_g can be calculated by

$$C_g(t_w + t_m) = k_\gamma \, \varepsilon_\gamma \, I_\gamma \int_{t_w}^{t_w + t_m} A_g(t) \, dt.$$
 (10)

 $A_g(t)$ is further described as

$$A_g(t) = A_g(t_a) \ e^{-\lambda_g t} + + Y \frac{\lambda_g}{\lambda_g - \lambda_m} A_m(t_a) \ (e^{-\lambda_m t} - e^{-\lambda_g t}).$$
⁽¹¹⁾

Inserting $A_i = Z_i \lambda_i$, solving the integral and converting to $Z_q(t_a)$ leads to

$$Z_g(t_a) = \frac{C(t_w + t_m)}{k_\gamma \ \varepsilon_\gamma \ I_\gamma \ (e^{-\lambda_g t_w} - e^{-\lambda_g(t_w + t_m)})} - \frac{Y \ \frac{\lambda_g}{\lambda_g - \lambda_m} \ Z_m(t_a) \ (e^{-\lambda_m t_w} - e^{-\lambda_m(t_w + t_m)})}{e^{-\lambda_g t_w} - e^{-\lambda_g(t_w + t_m)}} +$$
(12)
$$+ \frac{Y \ \frac{\lambda_m}{\lambda_g - \lambda_m} \ Z_m(t_a) \ (e^{-\lambda_g t_w} - e^{-\lambda_g(t_w + t_m)})}{e^{-\lambda_g t_w} - e^{-\lambda_g(t_w + t_m)}}.$$

Thus, σ_g can finally be deduced from Eq. 8 by inserting $\mathbf{Z}_g(\mathbf{t}_a)$:

$$\sigma_g = \frac{Z_g(t_a)}{N \ \Phi_{tot} \ f_g^b} - \frac{Y \ \sigma_m \ \lambda_m \ g_m}{f_g^b}.$$
 (13)

The second term in Eq. 13 describes the isomeric transition, for which the ground-state cross section has to be corrected. For half-lives longer than the ground-state, this part introduces major corrections, whereas for very short half-lives this term becomes negligible.

A. General

In an astrophysical environment with temperature T, the neutron spectrum corresponds to a Maxwell-Boltzmann distribution

$$\Phi \sim E_n \ e^{-E_n/kT}.\tag{14}$$

The experimental neutron spectrum of the ${}^{7}\text{Li}(p,n){}^{7}\text{Be}$ reaction approximates a Maxwellian distribution with kT=25 keV almost perfectly [42]. But to obtain the exact Maxwellian averaged cross section $\langle \sigma \rangle_{kT} = \frac{\langle \sigma v \rangle}{v_T}$ for the temperature T, the energy-dependent cross section $\sigma(E)$ has to be folded with the experimental neutron distribution to derive a normalization factor NF= $\frac{\sigma}{\sigma_{exp}}$. The region beyond the resonances (2.4 keV for ${}^{74}\text{Se}$ and 3.5 keV for ${}^{84}\text{Sr}$) was then multiplied with the normalization factor NF. The proper Maxwellian averaged cross section as a function of thermal energy kT was then derived from the normalized cross section (Fig. 2) in the energy range $0.01 \leq E_n \leq 4000$ keV.

$$\frac{\langle \sigma \upsilon \rangle}{\upsilon_T} = \langle \sigma \rangle_{kT} = \frac{2}{\sqrt{\pi}} \frac{\int_0^\infty \frac{\sigma(E_n)}{NF} E_n \ e^{-E_n/kT} \ dE_n}{\int_0^\infty E_n \ e^{-E_n/kT} \ dE_n}.$$
(15)

In this equation, $\frac{\sigma(E_n)}{NF}$ is the normalized energydependent capture cross section and E_n the neutron energy. The factor $v_T = \sqrt{2kT/m}$ denotes the most probable velocity with the reduced mass m.

For astrophysical applications, laboratory cross sections have to be converted to stellar cross sections involving thermally excited targets by applying a correction factor, the so-called stellar enhancement factor (SEF) [12]. While there are only comparatively few cases with low-lying nuclear states in the *s* process where the correction is important, it is to be expected that the SEF may be larger at the much higher *p*-process temperatures. However, this is not the case for the *p* nuclei considered here, as illustrated by Table III.

TABLE III: Stellar enhancement factors for different temperatures [12].

T [GK]	$kT \; [\mathrm{keV}]$	$SEF(^{74}Se)$	$\mathrm{SEF}(^{84}\mathrm{Sr})$
0.3	26	1.00	1.00
2.0	172	1.01	1.02
2.5	215	1.02	1.06
3.0	260	1.03	1.09

For ⁷⁴Se and ⁸⁴Sr, energy-dependent neutron capture cross sections were available from JEFF 3.0 [49], ENDF-B VI.8 [50], and NON-SMOKER [12, 13, 51], whereas JENDL 3.3 [52] provides only data for ⁷⁴Se. The energy region between 10 eV and 2.9 keV in JEFF, ENDF-B and JENDL includes experimentally evaluated data [53] and differs only in the strength of the resonances. The trend beyond 2.9 keV is deduced from statistical model calculations and deviates from NON-SMOKER when the (n,p) channel opens at $E_n>600$ keV (⁷⁴Se) and $E_n>750$ keV (⁸⁴Sr), respectively. In the following sections we will use the energy dependencies of JEFF 3.0 to determine Maxwellian averaged cross sections and compare the results only with NON-SMOKER.

B. Uncertainties

The experimental uncertainties are summarized in Table IV. Since nearly every stellar neutron cross section measurement was carried out relative to gold, the error of 1.4% [42] in the gold cross section cancels out.

Uncertainties between 1.4% (for samples with 10 mm diameter) and 2.9% (6 mm diameter) are due to an estimated sample position uncertainty of 0.25 mm relative to the Au foils during the activation, which affects neutron flux seen by the sample. For the Se samples, a fairly large contribution results from the 4.5% error of the isotopic abundance [43]. In the case of the ⁸⁴Sr(n,γ)⁸⁵Sr^{g+m} capture cross sections, considerable contributions come from the uncertainties of the γ -ray intensities. The errors in the time factors f_b , $f_w = e^{-\lambda t_w}$ and $f_m = e^{-\lambda t_m}$ are negligible in all measurements except those of the partial cross section to ⁸⁵Sr^m (t_{1/2} = 67.6 m) due to the rather long half-lives of the product nuclei in comparison with t_w and t_m . The error in the masses could be neglected for all samples except for the gold foils.

TABLE IV: Compilation of uncertainties.

Source of uncertainty		Uncertainty (%)			
-	$^{197}\mathrm{Au}$	$^{74}\mathrm{Se}$	$^{84}\mathrm{Sr}{ ightarrow}\mathrm{g}$	$^{84}\mathrm{Sr}{\rightarrow}\mathrm{m}$	
Gold cross section	1.4^{a}	-	-	-	
Isotopic abundance	-	4.5	1.8	1.8	
Detector efficiency	1.5	1.5	1.5	1.5	
Divergence of n flux	-	1.4 - 2.3	1.5 - 2.9	1.5 - 2.9	
Sample mass	0.2	-	-	-	
γ -Ray intensity	0.1	$0.5/\ 1.2^b$	4.2^c	$5.4/2.6^d$	
$\gamma\text{-Ray}$ self-absorption	-	0.2	0.2	0.2	
Counting statistics	1.0	0.4 - 1.6	3.6 - 5.3	0.4 - 2.0	
Time factors f_b , f_m , f_w	-	-	-	0.2 - 1.3	
Total uncertainty		$5.5 - 5.7^{e}$	$6.5 - 7.9^{e}$	4.3 - 7.1 ^e	

^aNot included in the final uncertainty, see text.

 $^b136~{\rm keV}/$ 265 keV.

 $^{c}514 \text{ keV}$

^d151 keV/ 232 keV.

^eIncl. uncertainty from Au.

The conservatively assumed overall uncertainty for the Se measurements is 5.7%. The partial cross sections to the 85 Sr ground and isomeric states have uncertainties of 7.1% and 5.3%, respectively, leading to a combined error of 5.6% in the total capture cross section. These uncertainties were also adopted for the Maxwellian av-

eraged cross sections, assuming that the uncertainties of the theoretical energy dependence were negligible for the extrapolation to kT = 30 keV.

C. 74 Se $(n,\gamma)^{75}$ Se

The ${}^{74}\text{Se}(n,\gamma){}^{75}\text{Se}$ reaction was analyzed via the two strongest transitions in ${}^{75}\text{As}$ at 136.0 keV and 264.7 keV. The results from the individual Se activations are listed in Table V. The capture cross section derived with the experimental neutron distribution is 281 ± 16 mb and was calculated as the weighted mean value of all five activations.

TABLE V: Results from the Se activations.

Activation	Cross sectio	n [mb]
$^{74}{ m Se}({ m n},\gamma)^{75}{ m Se}$	(136 keV)	(265 keV)
se-1	283 ± 16	276 ± 16
se-2	270 ± 15	259 ± 14^{a}
se-3	273 ± 16	265 ± 15
se-4	291 ± 16	287 ± 16
se-5	300 ± 17	284 ± 16
Mean cross section	281 ± 1	16

^aValue not included in mean value.

D. 84 Sr(n, γ) 85 Sr

In case of ⁸⁴Sr, neutron captures populate both, ground and isomeric state of ⁸⁵Sr. While ⁸⁵Sr^g decays can be identified via the 514 keV transition in ⁸⁵Rb, the decay of the isomer proceeds mainly via transitions of 232 keV and 151 keV. The isomeric state is 239 keV above the ground state and decays either via a 7 keV- 232 keV cascade (internal transition, 86.6%) or directly by electron capture (13.4%) into the 151 keV level of the daughter nucleus ⁸⁵Rb.

The partial cross section to the isomeric state can be easily deduced from the above mentioned transitions at 151 keV and 232 keV and yields 189 ± 10 mb (see Table VI). The cross section to the ground state has to be corrected for the internal decay of the isomer during the activation and measuring time, and results in 112 ± 8 mb. This leads to a total capture cross section of 301 ± 18 mb.

The corresponding isomeric ratio is $IR = 0.63 \pm 0.04$, in perfect agreement with the value of 0.63 ± 0.06 reported for thermal neutrons [54]. A NON-SMOKER estimation showed that the isomeric ratio is almost independent of the energy kT in the relevant range.

TABLE VI: Results from the Sr activations.

Activation	cross section [mb]			
$^{84}{ m Sr}({ m n},\gamma)$	$ ightarrow^{85}{f Sr}^g$	\rightarrow^{85}	\mathbf{Sr}^m	
	(514 keV)	(151 keV)	(232 keV)	
sr-1	114 ± 9			
sr-2	124 ± 8			
sr-3	102 ± 8			
sr-4m		189 ± 13	194 ± 10	
sr-5m		194 ± 13	194 ± 8	
sr-6	106 ± 7	178 ± 12	189 ± 8	
sr-7	107 ± 7			
sr-8m		186 ± 12	190 ± 9	
sr-9m		187 ± 12	191 ± 8	
sr-10	122 ± 8	192 ± 13	192 ± 9	
sr-11	106 ± 7			
sr-12m		178 ± 12	189 ± 9	
Mean cross section	112 ± 8	189 :	± 10	

V. COMPARISON WITH THEORY

A. Maxwellian cross sections for kT = 25 keV

⁷⁴Se(n, γ): Normalization of the energy dependent cross sections $\sigma(E_n)$ from NON-SMOKER, JEFF 3.0, ENDF-B VI.8 and JENDL 3.3 with the experimental value of 281 mb yields normalization factors between 0.568 and 0.736 (see Table VII). Fig. 2 shows the normalized $\sigma(E)$ spectra for JEFF and NON-SMOKER in comparison with the original spectra. The Maxwellian averaged cross section at kT=25 keV deduced with the JEFF dependence is $\langle \sigma \rangle_{25}=298$ mb.

⁸⁴**Sr**(\mathbf{n},γ): The normalization factors for ⁸⁴Sr vary between 0.774 and 1.076 (Table VII). With the normalized spectra of JEFF (Fig. 2) the resulting total stellar capture cross section $\langle \sigma \rangle_{25}$ (total) is 326 mb. With our isomeric ratio of 0.63 we calculate for the partial cross section to the isomer ⁸⁵Sr^m $\langle \sigma \rangle_{25}$ (part)= 205 mb.

TABLE VII: Cross sections derived by folding the experimental neutron distribution with the $\sigma(E)$ data of different libraries. NF denotes the respective normalization factors compared to the experimental cross section.

	$^{74}\mathrm{Se}$		84 Sr		
	cross section	NF	cross section	NF	
Experiment	281 mb	1.000	301 mb^a	1.000	
JEFF 3.0	160 mb	0.568	234 mb^a	0.779	
ENDF-B VI.8	160 mb	0.568	233 mb^a	0.774	
JENDL 3.3	207 mb	0.736	-	-	
NON-SMOKER	$206~\rm{mb}$	0.731	324 mb^a	1.076	

^aTotal capture cross section

B. Extrapolation to higher temperatures

Table IX shows the Maxwellian averaged cross sections for different thermal energies deduced with JEFF. The respective reaction rates were calculated from $\langle \sigma \rangle_{kT}$ via

$$N_A < \sigma v >= 26445.5 < \sigma >_{kT} \sqrt{kT/m}$$
(16)

with *m* being the reduced mass. The units for $\langle \sigma \rangle_{kT}$, the thermal energy kT and the reaction rate $N_A \langle \sigma v \rangle$ are [mb], [keV] and [mole⁻¹ cm³ s⁻¹], respectively. By convention, stellar neutron capture rates for *s*-process studies are compared at kT = 30 keV, which corresponds also to the freeze-out temperature of 3.5×10^8 K. For *p*process applications, the cross sections should be extrapolated to the energy range, which is relevant for the *p* process, i.e. 170 keV $\leq kT \leq 260$ keV, corresponding to temperatures of (2 to 3) $\times 10^9$ K.

For ⁷⁴Se a Maxwellian averaged cross section of $\langle \sigma \rangle_{30} = 271$ mb is derived, in perfect agreement with the previously estimated value of 267±25 mb from Ref. [41]. The result for ⁸⁴Sr is $\langle \sigma \rangle_{30}$ (tot) = 300 mb, 18% lower than the 368±125 mb from Ref. [41]. The partial cross section to the isomer yields $\langle \sigma \rangle_{30}$ (part) = 190 mb.

Fig. 3 shows theoretical predictions for the $\langle \sigma \rangle_{30}$ values of 74 Se [13, 14, 15, 41, 55, 56, 57, 58] and 84 Sr [13, 14, 15, 41, 55, 57, 58, 59] in comparison with our experimental value. In the case of 74 Se agreement is only found with the old and new MOST predictions [14, 15] and with the normalized NON-SMOKER cross sections in [41], which account for known systematic deficiencies in the nuclear inputs of the calculation. For ⁸⁴Sr, older predictions from Refs. [55, 57, 59] are in rather good agreement. Not shown in this plot is a corrected prediction from the old MOST code of 2002 [60] of 296 mb, which was also in good agreement with our experimental Maxwellian cross section at kT=30 keV. Table VIII gives a comparison between the two Hauser-Feshbach models MOST (with the versions of 2002 [14] and 2005 [15]) and NON-SMOKER, and the previous recommended (semiempirical) value from Ref. [41]. A full list of all 32 pnuclei can be found in [61].

Further extrapolation to temperatures between kT= 5 keV and 260 keV (Fig. 4) shows the different energy dependence of the data based on the NON-SMOKER, JEFF and MOST predictions. For this plot, the curves of NON-SMOKER and MOST were normalized to the JEFF values at kT= 25 keV. In the case of ⁷⁴Se the data libraries deviate at low and agree at higher energies, whereas ⁸⁴Sr exhibits an opposite trend. The results for the Maxwellian averaged cross sections at *p*-process temperatures are $\langle \sigma \rangle_{260}$ = 115 mb for ⁷⁴Se and 161 mb for ⁸⁴Sr, corresponding to stellar reaction rates of 4.92×10⁷ and 6.91×10⁷ mole⁻¹ cm³ s⁻¹, respectively. The temperature trends of the reaction rates are shown in Fig. 5.

TABLE VIII: Present Maxwellian averaged cross sections $\langle \sigma \rangle_{30}$ at kT = 30 keV compared to the Hauser-Feshbach calculations MOST and NON-SMOKER and data in [41].

$^{74}\mathrm{Se}$	Source	$<\sigma>_{30}$ [mb]	Reference
	NON-SMOKER	207	[13]
	MOST 2002	304	[14]
	MOST 2005	247	[15]
	Bao et al.	267 ± 25	[41]
	This work	271 ± 15	
84 Sr	Source	$<\sigma>_{30}$ [mb] ^{<i>a</i>}	Reference
	NON-SMOKER	393	[13]
	MOST 2002	74^b	[14]
	MOST 2005	246	[15]
	Bao et al.	368 ± 125	[41]
	This work	300 ± 17	

^{*a*} Total capture cross section.

^b Original value. Corrected value [60] is 296 mb for ⁸⁴Sr.

TABLE IX: Maxwellian averaged cross sections and reaction rates (including SEF from Table III) for thermal energies between kT = 5 keV and 260 keV derived with the energy dependence of JEFF 3.0.

		74 Se		84 Sr
kT	$<\sigma>_{kT}$	$N_A < \sigma v >$	$<\sigma>_{kT}{}^{a}$	$N_A < \sigma v >$
$[\mathrm{keV}]$	[mb]	$[\mathrm{mole}^{-1}\mathrm{cm}^{3}\mathrm{s}^{-1}]$	[mb]	$[\mathrm{mole}^{-1}\mathrm{cm}^{3}\mathrm{s}^{-1}]$
5	775	4.61×10^{7}	683	4.07×10^{7}
10	500	4.21×10^{7}	499	4.20×10^{7}
15	395	4.08×10^{7}	413	4.25×10^{7}
20	337	4.01×10^{7}	361	4.30×10^{7}
25	298	3.97×10^{7}	326	4.33×10^{7}
30	271	3.95×10^{7}	300	4.37×10^{7}
40	233	3.93×10^{7}	264	4.44×10^{7}
50	209	3.94×10^{7}	240	4.52×10^{7}
60	192	3.97×10^{7}	224	4.61×10^{7}
80	170	4.06×10^{7}	201	4.79×10^{7}
100	157	4.17×10^{7}	187	4.99×10^{7}
170	133	4.60×10^{7}	167	5.79×10^{7}
215	123	4.79×10^{7}	164	6.41×10^{7}
260	115	4.92×10^{7}	161	$6.91\!\times\!10^7$

^aTotal capture cross section

VI. SUMMARY AND OUTLOOK

We have presented the first results of an ongoing experimental program to determine more precise *p*-process reaction rates in the mass range A=70-140. The stellar (n,γ) cross sections of the *p* nuclei ⁷⁴Se and ⁸⁴Sr have been measured for the first time, yielding values of 281 mb for ⁷⁴Se, and 112 mb for the ground and 189 mb for the isomeric state to ⁸⁵Sr with our experimental neutron spectrum. The respective Maxwellian averaged cross sections for kT=30 keV were derived with the energy dependence of JEFF 3.0 and result in $\langle \sigma \rangle_{30} = 271\pm15$ mb for ⁷⁴Se, and $\langle \sigma \rangle_{30}$ (total)= 300 ± 17 mb for ⁸⁴Sr. The isomeric ratio IR was found to be 0.63 ± 0.04 and thus yields a partial stellar cross section



FIG. 2: Energy-dependent cross sections $\sigma(E)$ for ⁷⁴Se and ⁸⁴Sr, predicted by JEFF 3.0 and NON-SMOKER. Shown are the original data in comparison with the normalized data. Since the resonances in both cases are experimentally, only the curve beyond this region was normalized to our experimental value.



FIG. 3: Comparison of theoretically predicted Maxwellian averaged cross sections $\langle \sigma \rangle_{30}$ and the experimental values (derived with the energy dependence of JEFF 3.0) for ⁷⁴Se and ⁸⁴Sr.



FIG. 4: Temperature dependence of Maxwellian averaged cross sections derived by normalizing different predicted cross sections to the value deduced with JEFF 3.0 at kT=25 keV.

7.0x10 5.0x10³ reaction rate [mole⁻¹cm³s⁻¹] reaction rate [mole⁻¹cm³s⁻¹] 6.0x10 4.5x10³ 5.0x10 Se 4.0x10³ 4.0x10 0 40 80 120 160 0 40 80 120 160 200 240 200 240 kT [keV] kT [keV]

FIG. 5: Temperature trend of the reaction rates for ⁷⁴Se and ⁸⁴Sr derived with the normalized energy-dependent cross sections of JEFF 3.0 (see Table IX).

of $\langle \sigma \rangle_{30}$ (part.) = 190±10 mb.

Over the past decade, a lot of work has been devoted to measure cross sections and reaction rates of p nuclei, but experimental (p,γ) , (α,γ) and photodisintegration rates are still very scarce. The situation for stellar (n,γ) cross sections is somewhat better, but it should be pointed out that nearly all of the (n,γ) measurements were performed in energy regions relevant for the s process (kT=30 keV)instead of 100 < kT < 260 keV for the p process), whereas the charged particle rates are measured close to the respective p-process Gamow window.

The measurements presented in this paper mark the beginning of an extensive experimental program to determine more precise neutron cross sections of stable p nuclei. Within this program, we have already finished the measurement on 96 Ru [35], and preliminary values

are available for ¹⁰²Pd, ¹²⁰Te, ¹³⁰Ba, ¹³²Ba and ¹⁷⁴Hf [61]. All available experimental information will be summarized in an upcoming paper, including an extrapolation to the full range of p-process temperatures and the calculation of inverse reaction rates by detailed balance.

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