Modeling and Simulation of Electrical Impedance Tomography (EIT) on Ventilated Patients with ARDS Lungs

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Abstract—Bedside monitoring of lung recruitment is a key feature in the ventilatory management of patients with acute respiratory distress syndrome. Electrical Impedance Tomography is a relatively new imaging technique which reconstructs the electrical conductivity distribution in a lung cross section from electrical measurements made on electrodes placed on the surface of the thorax. The induced conductivity changes can be continuously monitored to assess the topographical distribution of air in the lung and optimise the ventilation strategy. The purpose of this paper is to illustrate these principles on a physiological model of the lung mechanics simulating the concept of recruitment in ventilated patients with acute respiratory distress syndrome.

I. INTRODUCTION

ACUTE Respiratory Distress Syndrome (ARDS) is a sudden, life-threatening lung dysfunction associated with severe and diffuse alveolar damage and increased microvascular permeability leading to pulmonary edema and heterogeneous lung density redistribution [1], [2]. Compliance of either lung is decreased causing increased work of breathing (WOB) and subsequent respiratory failure. The fundamentals of therapy are the provision of lung rest and supportive breathing in the Intensive Care Unit (ICU) using mechanical ventilation with a careful attention to fluid balance. Mechanical ventilation may, however, result in secondary lung damage referred to as Ventilator-Induced Lung Injury (VILI) caused by barotraumas (repetitive closing and reopening of injured alveoli) and/or pulmonary over distension when the lung units are physically stretched beyond their normal maximum inflation point.

Positive End Expiratory Pressure (PEEP) is the most effective way to achieve adequate oxygenation in ARDS patients. It improves the Functional Residual Capacity (FRC) and prevents recruited alveoli to collapse. However very high PEEP may decrease venous return and cardiac output and increase the risk of the development of extra pulmonary air (eg. Pneumothorax) [3]. Low Tidal Volumes ($V_t$) is another effective standard of ventilator therapy in patients with ARDS [4]. Ideally, mechanical ventilation should be conducted with sufficient PEEP to prevent end-expiratory collapse and tidal recruitment, and with a small tidal volume to avoid end-inspiratory over distension. However, due to the absence of a bedside monitoring technique, the choice of optimal ventilator titration strategy remains controversial.

Arterial blood gas analysis and the recording of Pressure-Volume (P-V) curve give only an indication of the overall lung function. Currently, chest Computed Tomography (CT scanner) is the most reliable technique for the clinical assessment of regional lung recruitment and ventilation distribution in patient with ARDS. By measuring lung densities, well-aerated regions can be easily differentiated from poorly and non-aerated lung regions. However, CT exposes the patient to radiations and is not a routine technique that is available at the bedside.

Electrical Impedance Tomography (EIT) is a promising noninvasive monitoring technique that allows real-time imaging of regional ventilation of the lungs at the bedside. EIT, however, has a low spatial resolution as compared to CT and Magnetic Resonance Imaging (MRI) and is sensitive to electrode placement.

The basic principle of EIT is based on the injection of small currents of about 5mA between adjacent surface electrodes placed circumferentially around the thorax and measurement of the resulting potential differences. Since air is a poor conductor of electric current, lung tissue filled with air will have a low conductivity in contrast to water and blood. Images can be reconstructed and displayed in real-time to monitor conductivity changes resulting from the respiratory activity.

The first clinical EIT images were obtained from the Sheffield Group [5] who used a filtered version of the back-projection method used in X-ray CT imaging. Recently a software package (EIDORS) implementing different methods for the solution of the forward and inverse problems in EIT is available for public use [6].

Many current ongoing research studies are being directed at demonstrating the ability of EIT to image regional lung ventilation in a clinical setting [7]–[10]. Comprehensive literature reviews in this field can be found in [11], [12].

The purpose of this paper is to demonstrate the principles of EIT imaging on a physiological model of the lung mechanics. The lung conductivity/volume relationship was modeled using published data recorded from EIT and spirometry measurements performed on a human subject [13]. A 2D finite element cross-sectional model of the thorax with sixteen electrodes was employed to simulate EIT measurements and reconstruct the conductivity distribution.
II. SIMULATION MODEL SETUP

The simulation setup shown in Fig. 1 includes a model of the respiratory mechanics, a parametric model describing the relationship between the assumed lung volume ($V$) and the left ($\sigma_L$) and right ($\sigma_R$) lung conductivities and a finite element cross section model of the thorax on which the EIT current injection and voltage measurements are performed. These simulated EIT data (assumed to be the ‘real measurements’) are then matched with the model predicted data set until some precision is reached.

A detailed description of these model components is presented in the following sections.

A. Model of the Lung Mechanics

A model based on simple physiology and lung mechanics has been proposed by Hickling [14], [15]. The model is based on the fact that recruitment and derecruitment of the lung alveoli are the principal cause of inflation and deflation respectively.

The lung is modeled as multiple units or alveoli which are distributed into compartments characterized by different superimposed pressure (gravitational pressure due to lung weight). In the upright position, the gravitational pressure increases linearly from the uppermost (independent region) compartment to the lowermost (dependant region) compartment. In the supine position the superimposed pressure increases from the ventral compartment (independent region) to the dorsal compartment (dependant region).

The lung units are described by their compliance curve which gives a nonlinear relationship between the applied pressure and the lung unit volume. The following equation is used to model this relationship [16]:

$$V = V_0 \left(1 - \exp(-P \log(2 / h))\right)$$

Where $V$ is the lung volume, $V_0$ is the maximum volume at high pressure, $P$ is the pressure and $h$ is the half-inflation pressure.

In the model, the lung unit can assume only two possible states: recruited (or open) and de-recruited (or closed) [16], [17]. These two states are governed only by the Threshold Opening Pressure (TOP) which the critical pressure above which the lung unit pops open and Threshold Closing Pressure (TCP) below which the unit collapses respectively. The model uses normally distributed TOP and TCP pressures with a specific mean and standard deviation [18] that may be adjusted to reflect the heterogeneous characteristic of alveoli under different abnormal lung conditions such as ARDS [19], [20]. Fig. 2 illustrates the mechanics of a single lung unit during inflation and deflation.

During inflation (or expiration) when the applied pressure exceeds the TOP, the lung unit pops open and assumes a volume according to the PV equation (1). During deflation (expiration) when the applied pressure falls below the TCP, the lung unit collapses and its volume becomes zero.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of alveoli per compartment</td>
<td>9000</td>
</tr>
<tr>
<td>Number of compartments</td>
<td>30</td>
</tr>
<tr>
<td>Gravitational pressure</td>
<td>0 to 14.5 cmH₂O</td>
</tr>
<tr>
<td>Lung volume (litres)</td>
<td>6</td>
</tr>
<tr>
<td>$V_0$ (litres)</td>
<td>3.8</td>
</tr>
<tr>
<td>$h$</td>
<td>5</td>
</tr>
</tbody>
</table>
B. Model of the Conductivity-Lung Volume Relationship

This parametric model provides a link between the lung mechanics and EIT models. It defines the relationship between changes in the basal conductivity of the lungs and the inspired fraction of air. The data used to derive this model were obtained from EIT and spirometry measurements recorded from a human subject during a respiratory cycle [13]. The left ($\sigma_L$) and right ($\sigma_R$) lung relative conductivities estimated from a thorax model for different inspiration levels are listed in Table 2 [13]. The inspiration fraction $F$ is defined as: $F = (V_{asp} - V_{min})/(V_{max} - V_{min})$. Where $V_{asp}$ represents the tidal volume, $V_{min}$ and $V_{max}$ are respectively the minimum and maximum volumes assumed during tidal breathing.

<table>
<thead>
<tr>
<th>$F$ (%)</th>
<th>$\sigma_L$</th>
<th>$\sigma_R$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0.8</td>
<td>0.8</td>
</tr>
<tr>
<td>20</td>
<td>1.0</td>
<td>0.8</td>
</tr>
<tr>
<td>40</td>
<td>0.9</td>
<td>0.7</td>
</tr>
<tr>
<td>60</td>
<td>0.7</td>
<td>0.6</td>
</tr>
<tr>
<td>80</td>
<td>0.5</td>
<td>0.6</td>
</tr>
<tr>
<td>100</td>
<td>0.4</td>
<td>0.5</td>
</tr>
</tbody>
</table>

Fitting these discrete values to a third order polynomial gives the parametric model plotted in Fig. 3.

C. Model of EIT

In EIT, current patterns are injected into the body via surface electrodes and boundary voltages are measured to reconstruct a cross-sectional image of internal distribution of the conductivity or resistivity. The quality of reconstructed images depends on (i) the number of electrodes and data collection strategy and (ii) the reconstruction algorithm employed. The most popular data collection strategy is the so-called adjacent or four-electrode whereas the type of reconstruction algorithm ranges from the simplest linearised single-step method to a computationally intensive iterative techniques.

Mathematically, the problem of recovering the conductivity or resistivity within the body from the surface measurements of currents and potentials is a nonlinear inverse problem and severely ill-posed. At low frequencies, these quantities are related by Laplace’s equation and Newman type boundary condition:

$$\nabla \cdot (\sigma \nabla u) = 0$$

$$\sigma \frac{\partial u}{\partial n} = \begin{cases} \vec{J} & \text{under the electrodes} \\ 0 & \text{elsewhere} \end{cases}$$

Where $\sigma$ is the conductivity, $u$ is the potential, $\vec{J}$ is the density of the injected current and $\vec{n}$ is the normal vector to the surface. For the uniqueness of the solution of (2), a variety of assumptions have to be made [18]. To solve the inverse problem one needs to solve the forward problem for some assumed conductivity distribution and compare the generated voltages with those obtained from real measurements. The finite element method was employed for the numerical solution of (2) by subdividing the 2D cross-section of the thorax into a finite number of triangular elements. The electric potential is expressed as a linear combination of the nodal basis functions. Each element is assumed to be homogenous and having the same conductivity. The Finite Element Model (FEM) shown in Fig. 4 was used to simulate the subject’s cross section of the thorax. The FEM was divided into four regions of different conductivities which were fixed to their basal values except those of the left and right lung that were varied according to Fig. 3. EIT numerical solution involves updating the conductivity distribution until the predicted and measured voltages match each other within a desired accuracy. The Gauss-Newton iterative algorithm implemented in [6] was used in this work.

III. SIMULATION RESULTS

In ARDS, the lungs become stiffer and the lung units tend to open and collapse at higher pressures compared with normal lung. In the model, the Mean and Standard Deviation (SD) of TOP and TCP pressures were given the values shown in Table 2 to simulate different intensities of ARDS [19], [21]. The Mean indicates the pressure at which the maximum of recruitment (TOP) and derecruitment (TCP) of lung units occurs, whereas SD describes the spread of the lung units’ population with respect to the TOP and TCP. Moreover the Functional Residual Capacity (FRC), that is
the amount of air that stays in the lungs during normal breathing, is also reduced in ARDS affected lungs. Estimated values for FRC under the degrees of ARDS conditions considered are given in Table 2.

### TABLE II
**TOP AND TCP PRESSURES FOR THE SIMULATED ARDS SCENARIOS**

<table>
<thead>
<tr>
<th>Degree of ARDS</th>
<th>TOP (cmH₂O)</th>
<th>TCP (cmH₂O)</th>
<th>FRC (litres)</th>
</tr>
</thead>
<tbody>
<tr>
<td>normal</td>
<td>Mean 4.5</td>
<td>Mean 2</td>
<td>FRC 2.4</td>
</tr>
<tr>
<td>mild</td>
<td>Mean 10</td>
<td>Mean 2.9</td>
<td>FRC 2.2</td>
</tr>
<tr>
<td>moderate</td>
<td>Mean 14.5</td>
<td>Mean 4.5</td>
<td>FRC 1.8</td>
</tr>
<tr>
<td>severe</td>
<td>Mean 24.5</td>
<td>Mean 4.8</td>
<td>FRC 1.5</td>
</tr>
</tbody>
</table>

Fig. 5 shows the plots of the Gaussian distributions of TOP and TCP pressures for the classes of simulated lung conditions given in Table 2.

Fig. 5. Gaussian distribution of TOP and TCP of normal and ARDS conditions (mild, moderate and severe).

A tidal breathing cycle is simulated by traversing up (inflation) and then down (deflation) the airway pressure range in small steps from PEEP to PIP (Peak Inspiratory Pressure) and then from PIP to PEEP respectively.

Fig. 6 shows the PV curves obtained for healthy and ARDS affected lungs. PEEP and PIP were set to 0 and 40 cmH₂O respectively.

In ARDS, the PV curves are right-shifted and characterized by larger hysteresis between the inflation and deflation limbs which is reflected by the difference in TOP and TCP pressures.

Fig. 7 presents the simulations of the severe ARDS model for four different values of PEEP (10, 12, 14, and 16 cmH₂O) under constant PIP (40 cmH₂O). Higher PEEP values lead to higher derecruitment volume which accounts for the lung units that are aerated at end-inspiration and remain open during expiration.

Fig. 7. PV curves of the simulated severe ARDS lung with PEEP = 10 cmH₂O (a), 12 cmH₂O (b) 14 cmH₂O (c) and 16 cmH₂O (d).

The physiological model of the lung mechanics simulating different degrees of ARDS conditions is incorporated with the EIT model in the simulation setup of Fig. 1.

Again, the model is cycled through the assigned airway pressure and at each pressure step the calculated lung volume is used to set the new conductivities of the left and right lungs on the thorax model of Fig. 4. EIT data are then generated using adjacent drive patterns with an injected current of 5 mA. These measured EIT data are compared to those predicted from another FEM model using the same drive and measurement patterns until some desired accuracy has been achieved. On convergence, the reconstructed image of the lung conductivity distribution is displayed. The image sequence is obtained by calculating conductivity changes from a reference state which defines the basal conductivities for the lungs and the rest the organs to a new state. This is the so-called difference imaging the EIT terminology as compared to absolute image which tries to recover the absolute value of the conductivity or resistivity from the boundary measurements.

Figs. 8 and 9 show the sequence of lung image slices (progressing from left to right and top to bottom) reconstructed from a simulated breath related to the moderate and severe ARDS models with the ventilator PEEP and PIP set to 0 and 40 cmH₂O respectively. Clear lung regions correspond to expiration at FRC and dark regions correspond to inspiration. This image contrast is the result of
the simulated changes in the conductivity of the left and right lungs. Lung inflation begins at slice 6.

Fig. 8. Temporal lung image slices of a breath (expiration-inspiration-expiration) related to moderate ARDS model. PEEP = 0 cmH₂O, PIP = 40 cmH₂O.

In the moderate ARDS model, lung inflation has begun at slice number 6, whereas in the case of severe ARDS model it has commenced at slice 8 confirming the results obtained with the static PV curves of Fig. 6 and the fact that TOP pressures of the lung units in the case of severe ARDS are higher than in moderate ARDS model.

Figs. 10 and 11 show the effect of PEEP on these models of ARDS lungs. PEEP was set to 10 cmH₂O with all the other parameters maintained to their previous values. Lung inflation starts at slice 6 and recruitment is maintained for those lung units whose TCP pressures are below the PEEP value selected. This PEEP value resulted in a larger derecruitment volume, which is the lung expansion at the end of expiration, in the moderate ARDS model than in the severe again due to the difference in the distribution of TCP pressures in these two models (Table 2).

Fig. 10. Image slices of a respiratory cycle related to moderate ARDS model. PEEP = 10 cmH₂O, PIP = 40 cmH₂O.

Fig. 11. Temporal lung image slices of a breath (expiration-inspiration-expiration) related to severe ARDS model. PEEP = 0 cmH₂O, PIP = 40 cmH₂O.

Interestingly, these simulation results demonstrate that EIT is able to continuously track ventilation distribution in the lungs, and thus can be effectively used to adjust the level of PEEP that is sufficient to prevent alveolar collapse during lung deflation.
IV. CONCLUSION

EIT is an established monitoring technique with the potential of becoming a valuable bedside tool for the assessment of the pulmonary function. EIT is capable of tracking local changes in pulmonary air contents and thus, can be used to continuously guide a proper titration of PEEP in the care of ARDS patients.

A simulation model based on respiratory physiology has been developed to demonstrate the principles of EIT monitoring on ARDS affected lung models under mechanical ventilation. The model is not intended to be a perfect and complete representation of the respiratory physiology of ventilated patients affected by ARDS. However, while relatively simple, it gives a good understanding of the processes of recruitment and derecruitment in ARDS affected lungs and illustrates how ventilator settings can be optimized with the aid of EIT monitoring techniques.

The model was able to reproduce images of the ventilated lung under different ARDS conditions which were consistent and presented a good agreement with the pressure-volume curve simulation results obtained for the same model of ARDS lungs. A rather simplistic parametric model has been used here to relate left and right lung conductivities to lung volume; however, more comprehensive models that would take into account the effect of anthropometric variables, gender and posture can be used.

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REFERENCES