



The Gliese 86 Binary System: A Warm Jupiter Formed in a Disk Truncated at ≈ 2 au

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Abstract

Gliese 86 is a nearby K dwarf hosting a giant planet on a ≈ 16 day orbit and an outer white dwarf companion on a \approx century-long orbit. In this study we combine radial velocity data (including new measurements spanning more than a decade) with high angular resolution imaging and absolute astrometry from Hipparcos and Gaia to measure the current orbits and masses of both companions. We then simulate the evolution of the Gl 86 system to constrain its primordial orbit when both stars were on the main sequence; the closest approach between the two stars was then about 9 au. Such a close separation limited the size of the protoplanetary disk of Gl 86 A and dynamically hindered the formation of the giant planet around it. Our measurements of Gl 86 B and Gl 86 Ab’s orbits reveal Gl 86 as a system in which giant planet formation took place in a disk truncated at ≈ 2 au. Such a disk would be just big enough to harbor the dust mass and total mass needed to assemble Gl 86 Ab’s core and envelope, assuming a high disk accretion rate and a low viscosity. Inefficient accretion of the disk onto Gl 86 Ab, however, would require a disk massive enough to approach the Toomre stability limit at its outer truncation radius. The orbital architecture of the Gl 86 system shows that giant planets can form even in severely truncated disks and provides an important benchmark for planet formation theory.

Unified Astronomy Thesaurus concepts: [Protoplanetary disks \(1300\)](#); [Planetary system formation \(1257\)](#); [Planet formation \(1241\)](#); [Stellar evolution \(1599\)](#); [Close binary stars \(254\)](#)

Supporting material: machine-readable table

1. Introduction

Thousands of exoplanets are now known in a huge variety of systems and in an enormous range of dynamical configurations (Luger et al. 2017; Shallue & Vanderburg 2018; Lam et al. 2020). These include hot Jupiters (Butler et al. 1997; Henry et al. 2000; Tinney et al. 2001), outer Jovian planets (Jones et al. 2010; Wittenmyer et al. 2014; Venner et al. 2021), smaller planets of all sizes and orbital distances (Barclay et al. 2013; Jenkins et al. 2015; Smith et al. 2018), planets around binaries (P-type systems; Welsh et al. 2012; Orosz et al. 2019; Kostov et al. 2021), and planets around individual stars within binaries (S-type systems; Hatzes et al. 2003; Ramm et al. 2016; Teske et al. 2016). This diversity suggests that planet formation is a robust, if not a universal, process accompanying star formation.

Planet formation in binaries is an especially important test bed for the planet formation process. The existence of the

binary provides natural constraints on the properties of circumstellar and circumbinary disks and therefore on the material available for planet formation. Both P- and S-type planets must form within a disk, but one that is dynamically interacting with the binary in an environment very different from the canonical solar nebula.

Su et al. (2021) conducted a statistical study of the S-type planetary systems detected from radial velocity (RV) surveys to generalize the characteristics of these systems. Table 1 of that paper summarizes the properties of 80 planet-hosting binaries; 10 of them (HD 42936, HD 87646, HD 59686, HD 7449, γ Cep, HD 4113, HD 41004, 30 Ari, Gl 86, and HD 196885) have separations smaller than 30 au. Jang-Condell (2015) argued that the frequent appearance of the planets in close binaries indicates that the formation process is robust. However, that the binaries are close to each other limits the amount of material in the circumstellar disk and significantly reduces the chance of forming planetary embryos. To better understand the planet formation under such conditions, we focus on Gl 86 and investigate its orbital parameters and possible planet formation scenarios in this paper.

Gl 86 is the second-closest planetary system containing a warm or hot Jupiter, after Gl 876, with a distance of 10.761 ± 0.005 pc (Lindegren et al. 2021) and an age of

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Table 1
Direct Imaging Astrometry of Gl 86

Date (Jyear)	ρ (arcsec)	PA (deg)	Reference
2000.82	1.73 ± 0.03	119 ± 1	Els et al. (2001)
2003.87	1.906 ± 0.015	107.5 ± 0.5	Lagrange et al. (2006)
2004.73	1.941 ± 0.014	105.3 ± 0.6	Lagrange et al. (2006)
2005.03	1.93 ± 0.02	104.0 ± 0.4	Mugrauer & Neu- häuser (2005)
2005.57	1.969 ± 0.011	102.7 ± 0.4	Lagrange et al. (2006)
2012.2468	2.351 ± 0.002	88.96 ± 0.04	Farihi et al. (2013)
2016.0 ^a	2.5725 ± 0.0020	83.36 ± 0.10	Lindegren et al. (2021)
2016.8606	2.6220 ± 0.0040	82.19 ± 0.10	STIS, this work

Note.

^a Measurement is not instantaneous.

≈ 10 Gyr (Fuhrmann et al. 2014). Queloz et al. (2000) discovered this system using the CORALIE echelle spectrograph and found an RV signal corresponding to an $m \sin i \approx 4 M_{\text{Jup}}$ planet with a 15.8 day orbital period, as well as a distant and massive companion causing a long-term RV drift. Els et al. (2001) used the ADONIS adaptive optics system on the ESO 3.6 m Telescope at La Silla to observe Gl 86 and identified a wide companion that they inferred to be a brown dwarf causing the RV drift. Mugrauer & Neuhäuser (2005) performed additional high-contrast observations and found that this wide companion is, instead, a cool white dwarf, and they ruled out any additional stellar companions between $0''.1$ and $2''.1$, or 1–23 au. Lagrange et al. (2006) used Very Large Telescope/NACO to obtain photometric and astrometric measurements, confirmed that the companion is a white dwarf rather than a brown dwarf, and inferred its mass to be $0.48 M_{\odot} \leq m \leq 0.62 M_{\odot}$ based on the amplitude of the RV trend observed by Queloz et al. (2000). Brandt et al. (2019) used all of the above measurements, as well as additional relative astrometry from Farihi et al. (2013) and the proper motion anomaly between Hipparcos and Gaia DR2 (Brandt 2018), to determine the mass and orbital parameters of the white dwarf.

The Gl 86 system, with a white dwarf on a ≈ 20 au orbit and a close-in, gas-giant exoplanet, challenges planet formation models. From a theoretical perspective, such close binary systems are expected to be hostile to the formation of giant planets owing to disk truncation (e.g., Artymowicz & Lubow 1994) and destructive planetesimal collisions (e.g., Paardekooper & Leinhardt 2010; Rafikov & Silsbee 2015), and this is largely borne out by observations (e.g., Wang et al. 2014; Kraus et al. 2016). The Gl 86 system presents a further problem because when both stars were on the main sequence the separation between them was even smaller and the stability and feasibility of forming the inner planet become even more questionable. Both Lagrange et al. (2006) and Farihi et al. (2013) doubted the orbital stability of the inner planet since the semimajor axis of the primordial binary system was too small. In order to work out a theory regarding the formation of the warm Jupiter in the Gl 86 system, it is necessary to better constrain Gl 86’s current and primordial orbital parameters and the stellar masses.

In this paper, we perform a new fit to the masses and orbits of the Gl 86 system using absolute astrometry from the latest Gaia Data Release (EDR3; Lindegren et al. 2021; Gaia Collaboration et al. 2021), together with RV and relative

astrometry data from the literature. We discuss the resulting orbital elements of the Gl 86 system in Section 2. In Section 3, we simulate the binary’s evolution based on an N -body integrator program in order to constrain its primordial orbit. In Section 4, we discuss some implications that the primordial orbit has on the formation of the planet surrounding Gl 86 A and the challenges the planet faced by the time it was formed. (Because Gl 86 B starts with a higher mass and ends with a lower mass owing to mass loss, we consistently call Gl 86 A the host and Gl 86 B the companion stars, instead of primary and secondary, to avoid confusion.) Finally, Section 5 summarizes our results.

2. The Current Orbit of Gl 86

We use the open-source Python package `orvara` (Brandt et al. 2021) to fit for the current masses and orbits in the Gl 86 system. The program can fit any combination of RVs, relative astrometry, and absolute astrometry from Hipparcos and Gaia. We use all of these types of data to constrain Gl 86. In this section, we describe the input data and our resulting fit.

2.1. Data

We use the absolute astrometry from Hipparcos (ESA 1997; van Leeuwen 2007) and Gaia’s latest data release (Gaia Collaboration et al. 2021) as cross-calibrated by Brandt (2021). The Hipparcos-Gaia Catalog of Accelerations (HGCA; Brandt 2018, 2021) provides three proper motions on the Gaia EDR3 reference frame; differences between them indicate astrometric acceleration. For Gl 86, the two most precise proper motions are the one computed from the position difference between Hipparcos and Gaia and the Gaia EDR3 proper motion. These two measurements are inconsistent with constant proper motion at nearly 300σ significance.

We use relative astrometry from multiple literature sources. Table 1 lists our adopted relative astrometry for Gl 86 B, where ρ is the separation between the two stars and PA is the position angle (east of north). The last data point in Table 1 was imaged on 2016 November 10 using the Space Telescope Imaging Spectrograph (STIS) as part of program GO-14076 (PI Gänsicke). The imaging was performed using the narrowband filter F28X500II (central wavelength 3738 Å, FWHM 57 Å) with a series of four 2 s exposures in a standard dither pattern. This filter has no red leak, and thus the bright host star remains unsaturated and in the linear response regime. The white dwarf companion is also detected in all four frames, at approximate signal-to-noise ratios between 13 and 19. This set of images was used to robustly measure the separation of the binary, where the companion star was found at offset $2''.6220 \pm 0''.0040$ with position angle $82^\circ.185 \pm 0^\circ.098$ under the J2000 frame.

We note that the relative position measurement of the two stars in Gaia EDR3 is less straightforward than the other relative astrometry measurements. It is the difference between the 2016.0 positions of five-parameter astrometric solutions to each star in the binary. The formal uncertainties are tiny but are subject to possible systematics from the proximity of the two stars and from their straddling of the $G = 13$ mag boundary where the window function changes (Cantat-Gaudin & Brandt 2021; Gaia Collaboration et al. 2021). We treat the measurement as instantaneous and, somewhat arbitrarily, adopt uncertainties similar to the HST uncertainties. This avoids

Table 2
RV Data of Gl 86

Date	RV (m s ⁻¹)	σ_{RV} (m s ⁻¹)
2450831.03498	958.65	1.66
2451211.96513	1227.68	2.17
2451213.98147	1282.40	2.28
2451214.92978	1227.60	1.94
2451235.93120	601.25	1.92
...

Note. All RVs are available electronically. Table 2 is published in its entirety in the machine-readable format. A portion is shown here for guidance regarding its form and content.

(This table is available in its entirety in machine-readable form.)

having Gaia solely drive the result and mitigates the possible impact of systematics.

The RV data come from the UCLES échelle spectrograph (Diego et al. 1990) on the Anglo-Australian Telescope. Those results spanning 1998–2005 were published in Butler et al. (2006). We also include a further 34 previously unpublished UCLES RVs spanning 2006–2015 (Table 2), for a total time baseline of 17.8 yr. The RV data are processed through the same pipeline, but they have some discrepancy with Butler et al. (2006) owing to minor pipeline tweaks and the fact that they have the mean stellar RV subtracted. Thanks to Gl 86 A’s very large acceleration, the mean RV has changed appreciably with an additional 9 yr of data.

2.2. Orbital Fit

We use `orvara` to fit a superposition of Keplerian orbits to the Gl 86 A astrometry and RVs and relative astrometry. We use log-uniform priors for semimajor axis and companion mass, a geometric prior on inclination, and uniform priors on the remaining orbital parameters. We adopt the Gaia EDR3 parallax as our parallax prior; `orvara` analytically marginalizes parallax out of the likelihood. We use a log-uniform prior on RV jitter.

We adopt an informative prior on the mass of Gl 86 A. Brandt et al. (2019) obtained $M_A = 1.39^{+0.24}_{-0.23} M_\odot$ by using the cross-calibrated Hipparcos and Gaia DR2 astrometry in a fit to Gl 86 B. Their prior was log-flat, but stellar evolution allows a much narrower prior. Fuhrmann et al. (2014) modeled Gl 86 A’s atmosphere using high-resolution spectroscopy and concluded that $M_A = 0.83 \pm 0.05 M_\odot$. We adopt this as our prior on Gl 86 A’s mass.

The log likelihood function consists of three parts: the χ^2 values of RV (including a penalty term for RV jitter), relative astrometry, and absolute astrometry. To maximize the likelihood is equivalent to minimizing the negative log likelihood,

$$-2 \ln \mathcal{L} = \chi^2 = \chi_{\text{RV}}^2 + \chi_{\text{rel ast}}^2 + \chi_{\text{abs ast}}^2 \quad (1)$$

In addition, the RV zero-point, parallax, and the proper motion of the system’s barycenter are marginalized out as nuisance parameters. We refer readers to the `orvara` paper for more details on the formulae and techniques used.

We use Markov Chain Monte Carlo (MCMC) to explore the posterior probability distribution with the `emcee` (Foreman-Mackey et al. 2013) and `ptemcee` (Vousden et al. 2016) packages. Parallel-tempering MCMC uses walkers at many temperatures, each multiplying an extra factor of $1/\sqrt{T}$ by the

Table 3
MCMC Results

Parameter	Value
Host star	
$M_A (M_\odot)$	$0.870^{+0.035}_{-0.026}$
White dwarf companion	
$M_B (M_\odot)$	0.5425 ± 0.0042
a_B (au)	23.7 ± 0.3
e_B	0.429 ± 0.017
i_B (deg)	$126.44^{+0.47}_{-0.49}$
Ω_B (deg)	234.2 ± 1.0
Inner planet	
$m_b \sin i_b (M_{\text{Jup}})$	$4.266^{+0.11}_{-0.087}$
a_b (au)	$0.1177^{+0.0015}_{-0.0012}$
e_b	0.0478 ± 0.0024

Note. Ω is the longitude of ascending node.

exponent of the likelihood. A larger temperature means a more flattened-out posterior probability distribution and enables hotter temperature walkers to explore more parameter space. Temperature swaps can happen periodically while preserving detailed balance. Parallel tempering helps to explore multi-modal posteriors and avoid getting stuck at some local minimum. We use 100 walkers, 30 temperatures, and 2×10^5 steps; we keep every 50th step and use the coldest chain for inference. We discard the first 1.25×10^5 steps as burn-in.

2.3. Results

Our first step with our resulting chains is to test whether they include formally well-fitting orbits. A satisfactory fit will have each data point contribute ≈ 1 to the total χ^2 . Unfortunately, our best-fit χ^2 of relative separation is 59.4, and that of position angle is 50.5; both are much too large for eight data points. Our high best-fit χ^2 values show that either we have underestimated uncertainties or there is an additional component in the system. Any additional component massive enough to affect the astrometry would have to orbit Gl 86 B to avoid detection in the precision RVs and direct imaging of Gl 86 A. Bringing the relative astrometry into agreement requires a perturbation of ~ 10 mas, which could be caused by a $\sim 20 M_{\text{Jup}}$ companion on a ~ 2 au orbit. However, such companions are rare (Halbwachs et al. 2000; Marcy & Butler 2000), and we have just two relative astrometry measurements at mas precision. This is insufficient to constrain the mass and orbit of a hypothetical substellar companion to Gl 86 B. We provisionally attribute the high χ^2 values to a combination of underestimated uncertainties and systematics in the data.

For our final orbit analysis, we inflate the uncertainties in the absolute astrometry by a factor of 2 and add 10 mas to our relative separation uncertainties and $0^\circ.05$ to our position angle uncertainties, both in quadrature, in addition to the error inflation used by Brandt et al. (2019). This brings the χ^2 values to an acceptable level ($\chi_{\text{rel sep}}^2 = 11.8$ and $\chi_{\text{PA}}^2 = 11.3$) and has only a minor impact on our derived parameters. The mass of Gl 86 B changes by just 0.5%, while the best-fit semimajor axis decreases from ≈ 25 to ≈ 24 au and the best-fit eccentricity increases from 0.38 to 0.43. Table 3 lists the full set of orbital parameters.

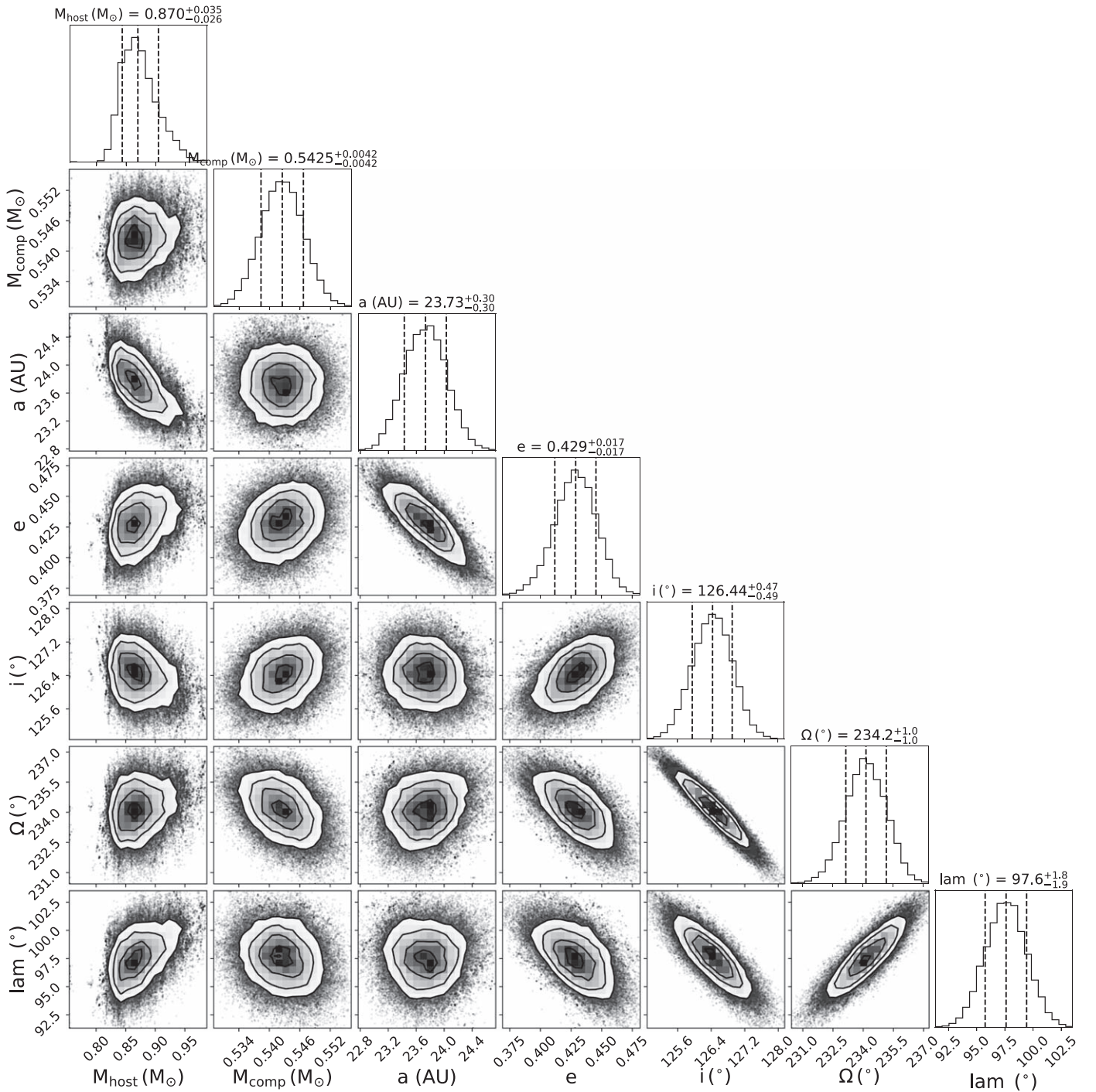


Figure 1. The corner plot of parameters of the white dwarf GI 86 B. Along the diagonal are the marginalized distributions of each parameter. Others are 2D joint posterior distributions of each of two parameters. Most parameters are well constrained, though some are strongly covariant.

The MCMC results are summarized in Figures 1 and 2. The parameters for the white dwarf companion GI 86 B are well constrained, but some parameters are strongly correlated. For example, its semimajor axis is anticorrelated with the eccentricity, and its inclination is also anticorrelated with its longitude of ascending node. The inner planet, GI 86 Ab, has an orbital period much shorter than either the Hipparcos or Gaia mission baseline. This, combined with the planet's low $m \sin i$, means that we have

almost no constraint on its orbital inclination or orientation. Even epoch astrometry from Gaia DR4 might not detect the $\lesssim 100 \mu\text{s}$ orbit of GI 86 A about its barycenter with GI 86 Ab.

Figure 3 shows the relative astrometric orbit of GI 86 AB, and Figure 4 shows the RV, separation, position angle, and proper motions as a function of time. For display purposes, we have removed the signal from the planet GI 86 Ab, as it has a very short period and would obscure the overall trend.

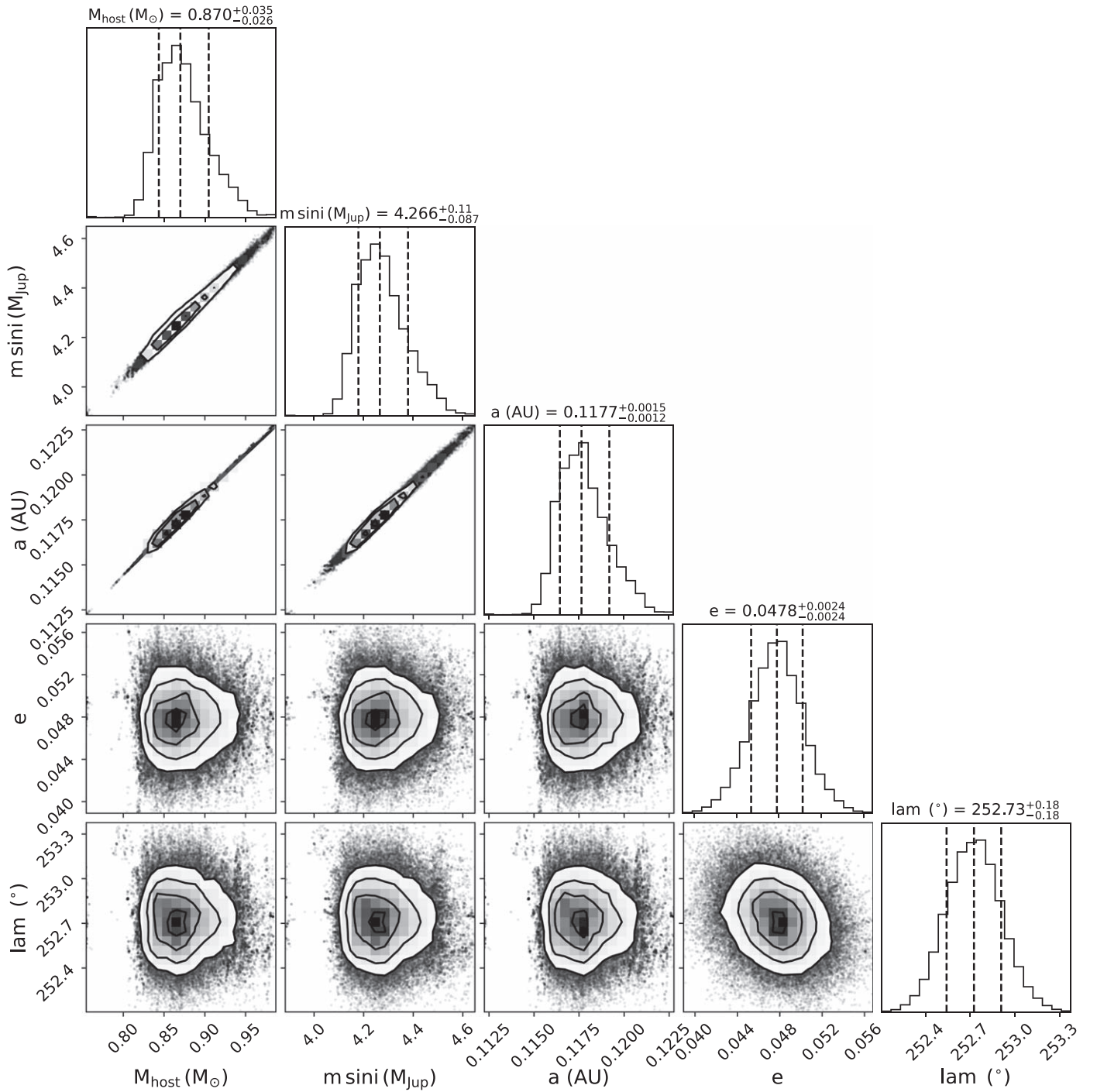


Figure 2. Same as Figure 1, but for the parameters of the planet Gl 86 Ab. The planet’s short orbital period prevents a constraint on either inclination or position angle; we plot only $m \sin i$. The near-total correlation between mass and semimajor axis results from Kepler’s third law.

3. The Primordial Orbit of Gl 86

In the previous section we obtained the orbital parameters of the current Gl 86 system. Next, we work out the primordial orbit when both stars were on the main sequence. To account for the alteration of the orbit throughout the period of Gl 86 B’s mass loss, a simulation is necessary. Unfortunately, most stellar evolution codes, such as MESA (Paxton et al. 2011), cannot evolve stars backward in time. Hence, we set up MESA with a suite of different initial masses of Gl 86 B and adopt the one whose final mass is closest to its current mass, and we use

Mercury (Chambers 2012), a general-purpose N -body integration package, to simulate the evolution of Gl 86’s orbit in Section 3.2.

From MESA, we find that when $M_{\text{initial}} = 1.39 M_{\odot}$, the final mass of Gl 86 B, $0.543 M_{\odot}$, is closest to the mass obtained in the previous section. This initial mass is consistent with Kalirai et al. (2008), who formulated the relation by studying the spectroscopic observations of a sample of 22 white dwarfs in two older open clusters, NGC 7789 and NGC 6819, plus data from the very old cluster NGC 6791; measuring the current masses of those white dwarfs; and calculating their

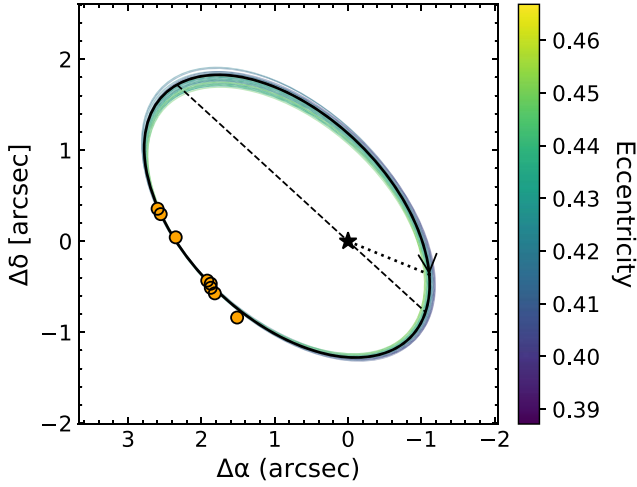


Figure 3. Relative astrometric orbit of Gl 86 AB. The solid black curve indicates the most probable orbit. The colored curves show 50 randomly selected orbits from the posterior probability distribution, with color denoting eccentricity. The star symbol at the origin represents the host star, the dotted line connects the host star to the periastron, and the dashed line is the line of nodes. The orange circles are the relative astrometry data points.

corresponding progenitor masses. Cummings et al. (2018) analyzed open cluster photometry of NGC 6121, NGC 6819, NGC 7789, Praesepe, the Hyades, and NGC 2099 and updated the initial-final mass relation (IFMR) of Kalirai et al. (2008) based on MESA Isochrones and Stellar Tracks (MIST) and PAdova-TRIeste Stellar Evolution Code (PARSEC) models. Although these two models indicate divergent IFMR for higher masses due to mismatched estimation of the Pleiades cluster’s age, they are remarkably consistent with each other for $M_{\text{initial}} < 5.5 M_{\odot}$,

$$M_f = (0.080 \pm 0.016) \times M_i + (0.489 \pm 0.030) M_{\odot} \quad (\text{MIST - based, } 0.83 M_{\odot} < M_i < 2.85 M_{\odot}) \quad (2)$$

$$M_f = (0.0873 \pm 0.0190) \times M_i + (0.476 \pm 0.033) M_{\odot} \quad (\text{PARSEC - based, } 0.87 M_{\odot} < M_i < 2.80 M_{\odot}). \quad (3)$$

However, these two models result in an $M_{\text{B, initial}}$ of 0.67 and $0.76 M_{\odot}$, respectively, which demand more than the Hubble time to evolve Gl 86 to the white dwarf stage and fall outside the domain of M_{initial} . Therefore, we claim that Gl 86 is an outlier according to this new IFMR. Another example of an outlier of this IFMR is DQ Procyon B (Bond et al. 2015).

We attribute the different M_{initial} to the different input physics and their implementations in the codes of the stellar evolution models (Choi et al. 2016). In our study, we simplify the assumption by adopting the input files in MESA’s test suite `1M_pre_ms_to_wd/`, leaving everything unchanged except for initial mass and metallicity, and ignoring other complicated mechanisms such as rotation and mass transfer.

In the remainder of this section, we first review analytic theoretical expectations for the evolution of semimajor axis and eccentricity and confirm that they are consistent with Mercury’s results. We then evolve the orbit of a $1.39 M_{\odot}$ star around a $0.870 M_{\odot}$ star to infer the initial dynamical configuration of Gl 86 AB.

3.1. Mass Loss

After a star evolves off the main sequence and passes the subgiant branch, its radius expands and its envelope becomes loosely bound. The radiation pressure due to photon flux expels the envelope. The star will experience mass loss during the red giant branch (RGB; $\dot{M} \approx -10^{-8} M_{\odot} \text{ yr}^{-1}$), the asymptotic giant branch (AGB; $\dot{M} \approx -10^{-8}$ to $-10^{-4} M_{\odot} \text{ yr}^{-1}$), and planetary nebula ($\dot{M} \approx -10^{-6} M_{\odot} \text{ yr}^{-1}$) phases, during which mass is cast away in the form of an isotropic stellar wind.

MESA computes the (isotropic) mass loss of Gl 86 B as a function of time. Figure 5 shows the mass of Gl 86 B with different metallicity versus the star age. Although Gl 86 B lost mass most rapidly by the end of the AGB, the $Z=1\%$ case lost $0.478 M_{\odot}$ in 0.602 Myr, equivalent to a rate of $7.95 \times 10^{-7} M_{\odot} \text{ yr}^{-1}$, if we approximate the average mass loss as linear. Even during the final thermal pulses that expel the envelope, mass loss proceeds on a timescale of $\sim 10^4$ yr. This remains much longer than the orbital period of ≈ 100 yr, making the mass loss very nearly adiabatic.

We can apply this in the relation between speed v and separation r for a Keplerian orbit with semimajor axis a ,

$$v = 2GM_{\text{tot}} \left(\frac{1}{r} - \frac{1}{2a} \right). \quad (4)$$

We differentiate with respect to time, setting $\dot{v} = 0$ for isotropic mass loss, and take the orbit average:

$$-\frac{1}{M_{\text{tot}}} \frac{dM_{\text{tot}}}{dt} = \frac{1}{a \left(\left\langle \frac{2a}{r} \right\rangle - 1 \right)} \frac{da}{dt}, \quad (5)$$

where

$$\left\langle \frac{2a}{r} \right\rangle = \frac{1}{P} \int_0^P \frac{2a}{r(t)} dt = 2, \quad (6)$$

and P is the orbital period. Equations (6) and (5) yield

$$M_{\text{tot}} a = \text{constant}, \quad (7)$$

which recovers Equation (16) of Jeans (1924).

For the secular evolution of the eccentricity, Hadjidemetriou (1963) presents the evolution of eccentricity in a binary system with slow mass loss,

$$\frac{de}{dt} = -(e + \cos f) \frac{\dot{M}}{M}, \quad (8)$$

where f is the true anomaly. Taking the time average and using Equation (13) of Dosopoulou & Kalogera (2016), the secular result is then

$$\begin{aligned} \left\langle \frac{de}{dt} \right\rangle &= \frac{1}{P} \int_0^P \frac{de}{dt} dt \\ &= \frac{1}{P} \int_0^P -\frac{e + \cos f}{M} \frac{dM}{dt} dt \\ &= -\frac{\dot{M}(1-e^2)^{3/2}}{2\pi M} \int_0^{2\pi} \frac{e + \cos f}{(1 + e \cos f)^2} df \\ &= 0. \end{aligned} \quad (9)$$

Equations (7) and (9) show that isotropic, adiabatic mass loss will expand the orbit, but at fixed eccentricity. This still holds with anisotropic mass loss, as long as we keep the adiabatic assumption and further assume that the anisotropic wind and jets are symmetric with respect to the equator (Veras et al. 2013; Dosopoulou & Kalogera 2016).

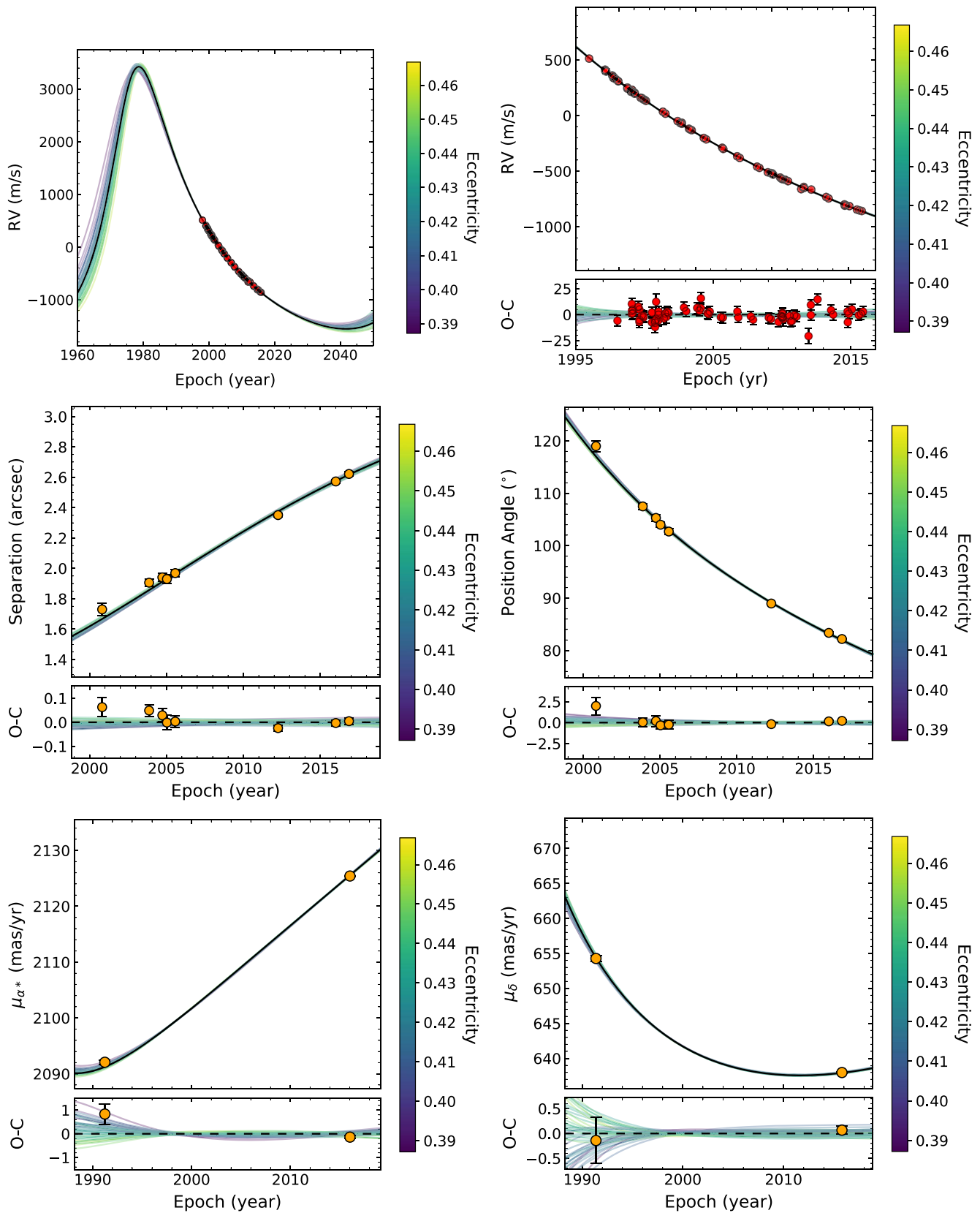


Figure 4. MCMC fitting results of the RV orbit (top), separation and position angle (middle), and proper motions (bottom). The black curve indicates the highest likelihood orbit; the 50 colored curves are randomly selected from the posterior and color-coded by eccentricity. For clarity, the influence of the inner planet GI 86 Ab has been subtracted from all panels. Data points in all figures are shown with filled circles, while the small lower panels show the residuals of the fit.

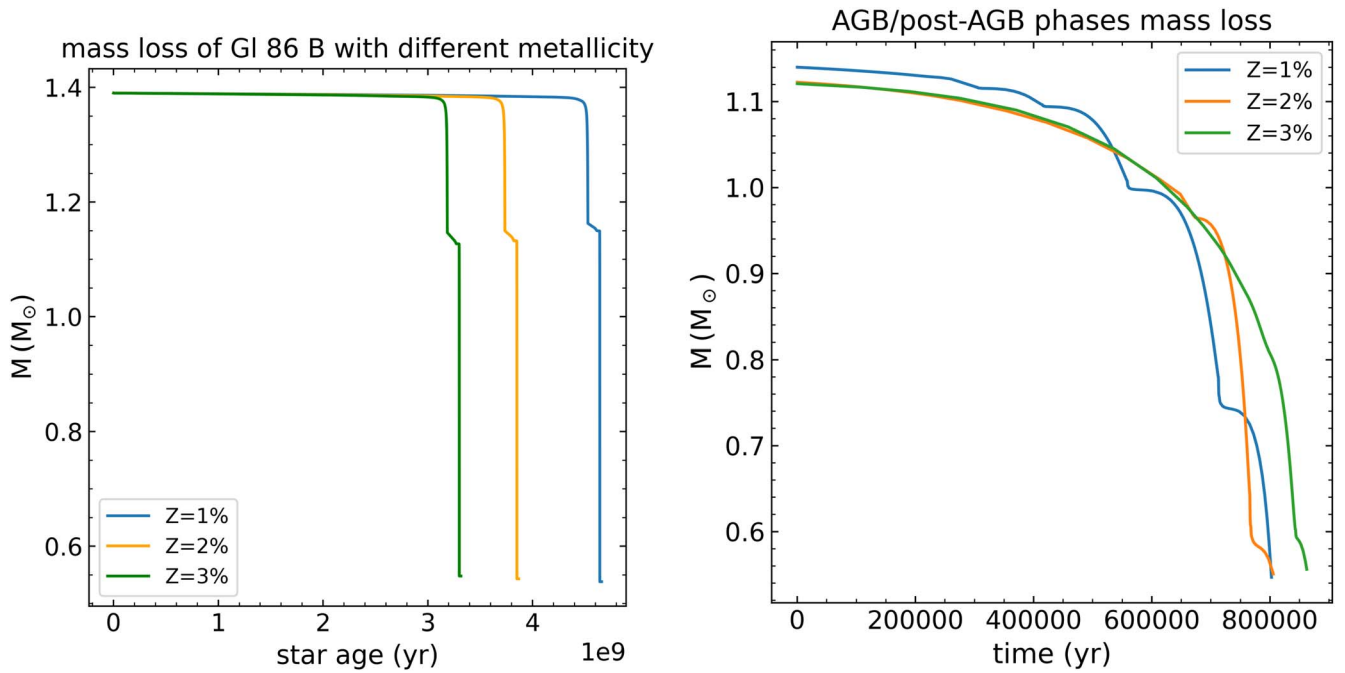


Figure 5. Left: the mass of Gl 86 B vs. star age, assuming different metallicity. Right: the mass loss of Gl 86 B was most rapid during the AGB and post-AGB phases, where it lost about $0.57 M_{\odot}$ in the last 0.8 Myr of evolution. However, even during the final stages, mass was lost over several $\times 10^4$ yr, much longer than the ≈ 100 yr orbital time of Gl 86 B.

We next consider mass transfer due to the ejection of Gl 86 B’s envelope and its possible accretion onto Gl 86 A through the Roche lobe. Once a star is large enough to fill out its Roche lobe, it transfers mass to its companion via the first Lagrangian point L_1 . We can tell whether a star passes its Roche lobe or not using a by-product of the MESA simulation, the radius of Gl 86 B as a function of time, and a calculator for Roche lobe properties (Leahy & Leahy 2015), to show the 3D illustration of the Roche lobe of Gl 86 B (Figure 6). The result shows that the Roche lobe is very spacious, and the surface of Gl 86 B is far from touching that of the Roche lobe when Gl 86 B reaches its maximum size during the AGB stage. This suggests that there was no mass transfer/ejection throughout the evolution of the binary, when the primordial semimajor axis was 14.8 au (see Section 3.2).

3.2. Binary Evolution

In Section 3.1, we have argued that Gl 86 B’s mass loss was mostly isotropic. We further assume that the mass loss was adiabatic and linear for the whole duration when Gl 86 B lost mass because the fractional mass-loss rate is small on an orbital timescale. Our simplifying assumption of a constant mass-loss rate does not change the evolution’s overall physical results (see Equation (7)).

We integrate the orbit of Gl 86 B around Gl 86 A using Mercury with the general Bulirsch–Stoer algorithm and assuming linear mass loss. It is slow but accurate in most situations and can dynamically adjust the step size. Our Mercury integration reproduces the orbit of the companion with respect to the host (Figure 7) and enables us to visualize its slow and steady expansion throughout time.

Mercury’s simulation agrees with the secular evolution of semimajor axis and eccentricity in Equations (7) and (9); these are shown in the two panels of Figure 8.

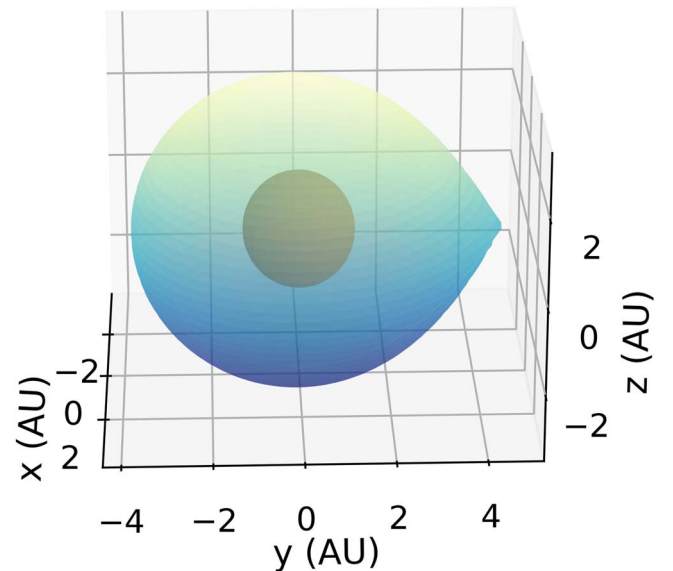


Figure 6. The blue and yellow shade is the 3D Roche lobe of Gl 86 B when it was in the post-AGB phase, during which Gl 86 B expanded most. The orange sphere represents the size of Gl 86 B at that time. The figure demonstrates that it is safe to assume that there is no mass transfer, as Gl 86 B is far from touching the surface of the Roche lobe.

4. Feasibility and Challenges of Planet Formation in the Gl 86 System

4.1. Mechanism of Planet Formation

There are two main phases of the formation of a Jovian planet by core accretion. The first phase is the formation of the planetary core, for which two main theoretical mechanisms have been advanced: planetesimal accretion and pebble accretion. Planetesimal accretion, once the dominant hypothesis (Pollack et al. 1996), has difficulty forming a core and

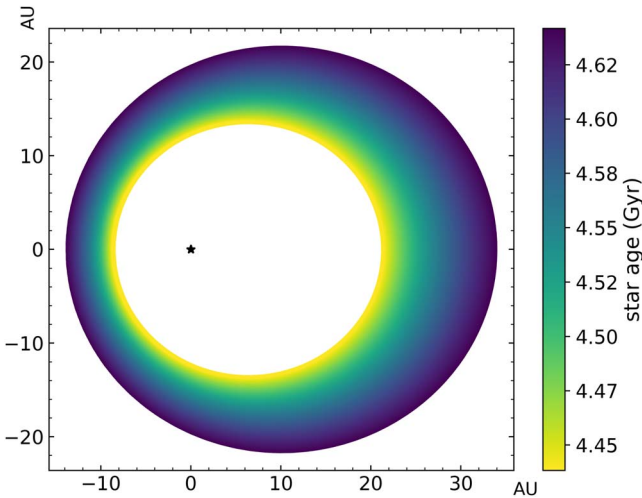


Figure 7. Mercury simulation of the orbit of Gl 86 B about Gl 86 A during the period of Gl 86 B’s mass loss. The star symbol at the origin stands for Gl 86 A. When both stars were on the AGB phase, where Gl 86 B mainly started to lose mass, it was at the innermost (yellow) orbit. As it shed mass, the semimajor axis increased, and it gradually spiraled out and ended up as a white dwarf at the outermost (purple) orbit.

accreting a gaseous envelope before the protoplanetary disk dissipates (Lambrechts & Johansen 2012). The theory of pebble accretion has become increasingly popular as a solution to this problem (Bitsch et al. 2015; Johansen & Lambrechts 2017; Bitsch et al. 2019). Although planetesimal accretion still dominates during the early stage of the growth of the planetary embryo, pebble accretion becomes significant when the core is several hundred kilometers in size. Pebbles passing by the core experience the drag force of the gas in the protoplanetary disk, undergo Bondi–Hill accretion, and quickly spiral in (Johansen & Lambrechts 2017). This drastically reduces the timescale and enables the formation of the planet within the lifetime of the protoplanetary disk.

The second phase starts after the core reaches the isolation mass, during which the core carves a shallow gap and stops the drift of pebbles from accumulating to the core. Then, the core starts to accrete from the gaseous envelope. This process is slow until runaway gas contraction initiates when the mass of the envelope exceeds that of the core (Bitsch et al. 2015, 2018).

In rare cases, a planet could start as a circumbinary planet and be tidally captured by one of the stars, ending up as a circumstellar planet (Gong & Ji 2018). It can also form around one star and be captured by the other (Kratter & Perets 2012). However, both mechanisms typically produce highly eccentric planets, in conflict with Gl 86 Ab’s low observed eccentricity of 0.0478 ± 0.0024 . It is possible that Gl 86 Ab was captured as an eccentric planet and tidally circularized. However, its orbital period is 15.8 days, while the tidal circularization period cutoff for the 4 Gyr old open cluster M67 has been measured to be ≈ 12 days (Meibom & Mathieu 2005; Geller et al. 2021). Planets on longer periods remain eccentric; they need more than 4 Gyr to circularize. The cooling age of the white dwarf Gl 86 B is just 1.25 ± 0.05 Gyr (Farihi et al. 2013), far too little time for tidal circularization of Gl 86 Ab. In the rest of the paper, we consider only the scenario in which Gl 86 Ab formed around its current host star.

The mechanism of planetary formation in specific close binaries has been investigated by Jang-Condell (2015). They studied the feasibility of planet formation in HD 188753 A,

γ Cep A, HD 41004 A, HD 41004 B, HD 196885 A, and α Cen B. They tested a suite of 18 different combinations of viscosity parameters α and accretion rates \dot{M} , given the binary parameters M_{host} , M_{comp} , a , and e , and counted how many (α, \dot{M}) models satisfied the core accretion or disk instability mechanism, respectively. The conventional criterion for core accretion to occur is whether the total solid mass in the disk exceeds $10 M_{\oplus}$, the least amount of mass to create a rocky core and initiate gas accretion. Jang-Condell (2015) found that except for HD 188753 A, where none of the models fit the observed system properties, core accretion was overwhelmingly more likely than disk instability for the formation of the planet. Jang-Condell et al. (2008) also pointed out that disk instability can only occur in the most massive disks with extremely high accretion rates.

In order to form Gl 86 Ab, we must then satisfy two requirements. First, we must have enough solid material in the disk to assemble a $\approx 10 M_{\oplus}$ core. Second, the disk itself must exceed the current mass of Gl 86 Ab in order to supply the gaseous envelope. In the following section we will work out the total mass of Gl 86’s disk under different models. We will assume a minimum dust mass of $10 M_{\oplus}$ and a minimum total mass of $5 M_{\text{Jup}}$ in order to have any chance of forming Gl 86 Ab.

4.2. Total Disk Mass and Dust Mass

In this section we compute both the total mass of the disk and its mass in dust suitable for forming the core of Gl 86 Ab. We take the total dust mass to be a dust-to-gas ratio multiplied by the total disk mass, which is the integral of the disk’s surface density from the inner rim to the outer truncation radius. We will compute the truncation radius due to the stellar companion first and the inner rim next.

4.2.1. Truncation Radius

The protoplanetary disk around Gl 86 A could not have extended past the orbit of Gl 86 B and in fact would have been truncated at a significantly smaller radius. The first criterion that needs to be satisfied to truncate a disk is that the resonant torque should be greater than the viscous stresses. A viscosity-dependent tidal distortion and resonant interactions exert torques on the disk with opposite directions. If the torque of the resonant interaction surpasses that of the tidal distortion, a gap would be opened and the disk would be truncated.

The magnitude of resonant torques varies at different resonant states (m, l) , where $m \geq 0$ is the azimuthal number and l the time-harmonic number. At a given resonant state, there are three different types of resonances: the inner Lindblad resonance (ILR), the outer Lindblad resonance (OLR), and corotational resonance (CR). They occur at different positions according to Equations (9) and (10) of Artymowicz & Lubow (1994, hereafter AL94):

$$r_{\text{CR}} = (m/l)^{2/3} \mu_{\star}^{1/3} a \quad (10)$$

$$r_{\text{LR}} = [(m \mp 1)/l]^{2/3} \mu_{\star}^{1/3} a, \quad (11)$$

where μ_{\star} equals $M_{\text{host}}/(M_{\text{host}} + M_{\text{comp}})$ for the circumstellar disk of M_{host} , $M_{\text{comp}}/(M_{\text{host}} + M_{\text{comp}})$ for the circumstellar disk of M_{comp} , and 1 for the circumbinary disk. The minus and plus signs in Equation (11) correspond to the ILR and OLR, respectively. The ILR dominates in the circumstellar case, and

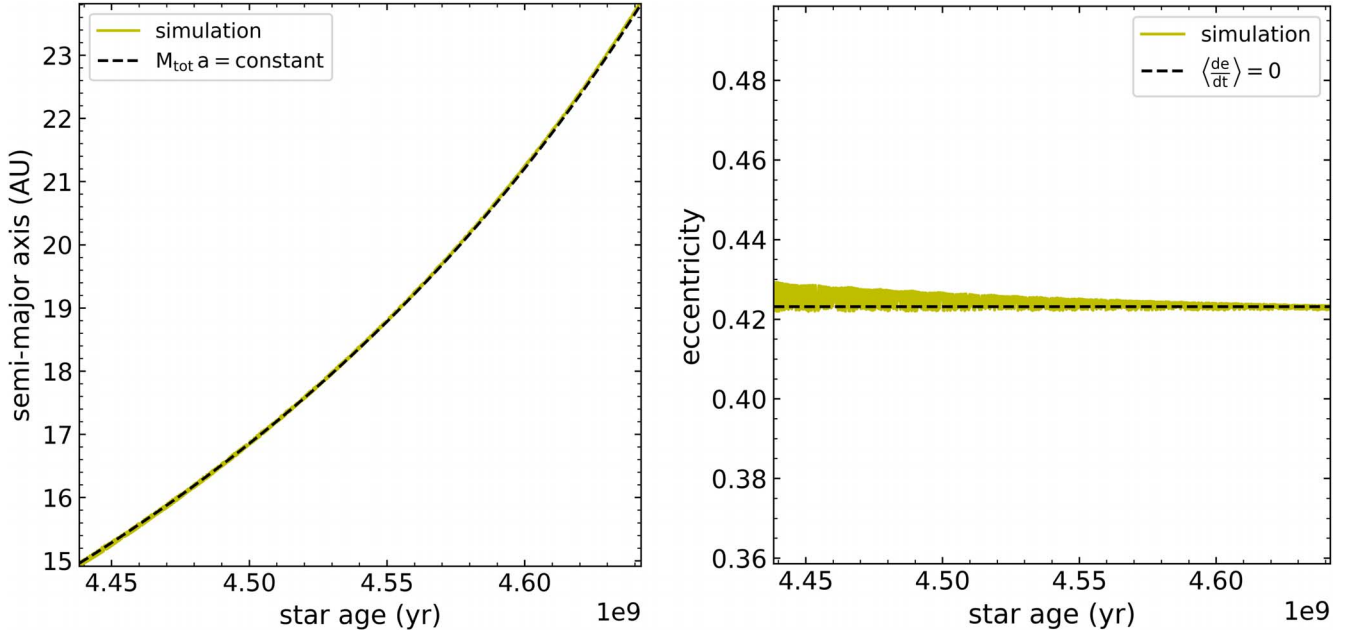


Figure 8. The secular evolution of the semimajor axis (left) and eccentricity (right) of GI 86’s orbit since the AGB phase of GI 86 B assuming constant mass loss. The yellow curves are the simulation results from Mercury. The dashed black curves are analytic expectations from theory. The semimajor axis goes from 15.0 to 23.7 au, and the eccentricity remains unchanged.

the OLR dominates in the circumbinary case. We are looking for the smallest possible radius at which the resonant torque is greater than the viscous stress or satisfies Equation (15) of AL94. We check the ILR first because it dominates in a circumstellar disk, and it has the smallest radius among the three types of resonant interactions given an (m, l) set. With the method elaborated in AL94, this first criterion breaks down as

$$\alpha^{1/2} \left(\frac{H}{r} \right) = \left(\frac{a |\phi_{ml}|}{GM} \right) \frac{(\pi m)^{1/2} (m \pm 1)^{1/6} |\lambda \mp 2m|}{2\mu_*^{2/3} l^{2/3}}, \quad (12)$$

where $\lambda = m$ for the ILR of the circumstellar disk and $\lambda = -(m + 1)$ for the OLR of the circumbinary disk, and α is the viscosity parameter (Shakura & Sunyaev 1973). The left-hand side of Equation (12) indicates the magnitude of viscous stress. The larger the α , the stronger the viscous stress. We can also write the left-hand side as $\frac{1}{\sqrt{\text{Re}}}$ in terms of Reynolds number Re, where

$$\text{Re} = \frac{1}{\alpha} \left(\frac{r}{H} \right)^2. \quad (13)$$

With $M_1 = 0.870 M_\odot$ and $M_2 = 1.39 M_\odot$, the left panel of Figure 9 shows the radial positions where resonant interaction occurs in units of semimajor axis versus the distribution of the eccentricity at which the torque is large enough to balance the viscous stress. As the eccentricity increases, the magnitude of the resonant torque gets larger, which means that the disk can be truncated more easily. Squares connected by dotted lines share the same Reynolds number. The gray line in the figure indicates that the eccentricity of GI 86 is 0.429. We can read the positions where the circumstellar disk is truncated, based on how the gray line intersects with the r versus e curves. For Reynolds numbers equal to $10^3, 10^4, 10^5, 10^6, 10^8, 10^{11}, 10^{14}$, the truncation radii are $0.22a, 0.18a, 0.16a, 0.15a, 0.12a, 0.10a, 0.08a$, or $3.3, 2.7, 2.3, 2.2, 1.8, 1.4, 1.2$ au, respectively. The right panel shows the resulting truncation radii with respect

to different Reynolds numbers, ranging from 10^3 to 10^{14} , at $e = 0.429$ and in terms of au. The black circles are the truncation radii corresponding to a sequence of Reynolds numbers starting from 10^3 to 10^{14} , incrementing with a factor of 10 for each step.

The second criterion is that gap opening time t_{open} should last for a reasonably short time relative to the viscous timescale. The gap opening time, approximately the same as the viscous closing time, equals $t_{\text{open}} \approx (\Delta r)^2 / \nu$, where Δr is the radial extent of the gap and ν is the viscosity. According to the formula of viscosity,

$$\nu = \alpha c_s H, \quad (14)$$

where c_s is the sound speed and H is the height of the disk. $H = c_s / \Omega$, where Ω is the Keplerian orbital angular frequency

$$\Omega = \sqrt{\frac{G(M_1 + M_2)}{r^3}}. \quad (15)$$

Hence,

$$\begin{aligned} \nu &= \alpha c_s H \\ &= \alpha H^2 \Omega. \end{aligned} \quad (16)$$

With Equations (13), (16), and $\Omega = \frac{2\pi}{P}$, we have

$$\begin{aligned} \frac{t_{\text{open}}}{P} &\approx \left(\frac{\Delta r}{r} \right)^2 \frac{\text{Re}}{2\pi} \\ &= \left(\frac{\Delta r}{r} \right)^2 \frac{1}{2\pi\alpha} \left(\frac{r}{H} \right)^2 \\ &\approx \frac{1}{2\pi\alpha}. \end{aligned} \quad (17)$$

Since α ranges between 0.001 and 0.1, t_{open} is approximately $1P - 100P$, which is short compared to the disk’s lifetime on the main sequence.

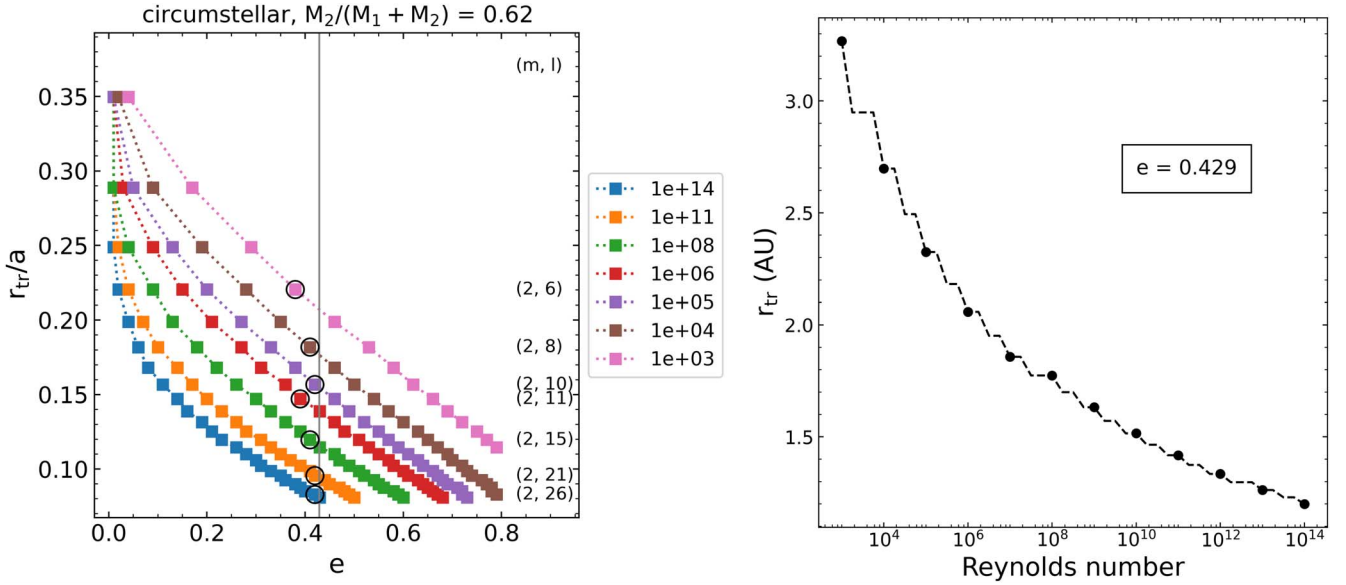


Figure 9. Left: locations of resonant interactions between the circumstellar disk around the present Gl 86 A and the primordial orbit of Gl 86 A and B. The present eccentricity is shown by a vertical line, while different colors indicate different Reynolds numbers. Because the Reynolds number is inversely proportional to the viscosity coefficient, a larger Reynolds number means smaller viscous stress. The squares on each strip represent a large enough eccentricity that gives rise to a resonant torque that overcomes the viscous stress. From the plot, we can read off the truncation radii of Gl 86’s protoplanetary disk for different Reynolds numbers. Black circles indicate those radii (AL94). Right: the truncation radii in terms of the Reynolds numbers at $e = 0.429$. The black circles are the truncation radii corresponding to a sequence of Reynolds numbers starting from 10^3 to 10^{14} , incrementing with a factor of 10 for each step.

4.2.2. Inner Rim

The inner part of a protoplanetary disk can be divided into four components: a dust-free region, a dust halo, a condensation front, and an optically thick disk (Figure 1 of Ueda et al. 2017, henceforth U17). The dust in this region functions as a feedback regulation. If the temperature of the disk is lower than T_{ev} , then the dust condenses and heats up. Otherwise, the temperature goes down when the dust evaporates since the emission-to-absorption ratio of the dust is lower than that of the gas (U17). The temperature in this region is approximately high enough (1200–2000 K) to evaporate dust (Natta et al. 2001), and the inner rim of the disk lies between the dust halo and condensation front. When stellar flux illuminates the inner rim of the disk, the near-infrared (NIR) emission from dust at the sublimation radius stands out among the intercepted flux. NIR long-baseline interferometry effectively presents the distribution of the dust grains, and the emission in the K -band continuum suggests where the inner rim is (Gravity Collaboration et al. 2019). Gravity Collaboration et al. (2021) used the Very Large Telescope Interferometer to observe the NIR K band of 17 T Tauri stars that weigh between 0.5 and $3 M_{\odot}$, the smaller counterpart of Herbig Ae Be stars. Setting aside the four targets whose mass is $\geq 1.9 M_{\odot}$, the remaining 13 targets (mass between 0.4 and $1.5 M_{\odot}$ and luminosity between 0.41 and $3.90 L_{\odot}$) have dust sublimation radii between 0.05 and 0.10 au and K -band half-flux radii between 0.1 and 0.2 au.

Gl 86 A is a Sun-like star, whose disk structure resembles that of T Tauri stars. The dust sublimation temperature is close as well. With a specific accretion rate of $3.6 \times 10^{-9} M_{\odot} \text{ yr}^{-1}$ (the observation of Gravity Collaboration et al. 2021 shows that accretion rates do not affect the inner rim location), irradiated hydrostatic disk models show that the silicate sublimation front begins at around 0.08 au, that a curved dust rim exists between 0.08 and 0.15 au, a small shadowed region between 0.2 and 0.3 au, and a flared disk beyond 0.3 au (Flock et al. 2019). The

simulation also shows a steep rise of gas density at 0.13 au, corresponding to the rise of dust density of the wedge-shaped inner rim with multisize grain distribution (Gravity Collaboration et al. 2019). Therefore, we set 0.13 au as the start of the inner rim of Gl 86 A’s protoplanetary disk. This is similar to Gl 86 Ab’s current orbital radius of 0.11 au.

4.2.3. Disk Mass

With the truncation radius and the inner rim worked out, the next step is to compute the total mass of the disk and the mass of solid material available to form the core of Gl 86 Ab. In this section we derive the expression of the disk surface density and then integrate it numerically.

The hydrostatic equilibrium equation reads

$$\dot{M} = 3\pi\nu\Sigma_G = 3\pi\alpha H^2\Omega\Sigma_G, \quad (18)$$

where Σ_G is the surface density of gas. We combine Equations (13), (15), (16), and (18) to get

$$\Sigma_G(\text{Re}, \dot{M}, M_1, M_2) = \frac{\dot{M} \text{Re}}{3\pi\sqrt{G(M_1 + M_2)}r}. \quad (19)$$

The integral of Equation (19) from the inner rim to the truncation radius is the total mass of a protoplanetary disk. The result is consistent with Table 1 of Jang-Condell & Sasselov (2003).

In order to form Gl 86 Ab, the protoplanetary disk must have had enough solids to form the planetary core and enough mass to supply the gaseous envelope. The total dust mass is the disk mass multiplied by a dust-to-gas ratio, which starts around 10^{-10} near the star and increases rapidly near the inner edge of the disk. It reaches a plateau of 10^{-2} when it reaches the optically thick disk (e.g., Figure 2 of U17). We adopt 10^{-2} as the dust-to-gas ratio. A minimum $10 M_{\oplus}$ total dust mass implies a disk mass of $1000 M_{\oplus}$, or $\approx 3 M_{\text{Jup}}$. The disk must also have supplied Gl 86 Ab’s envelope and must therefore

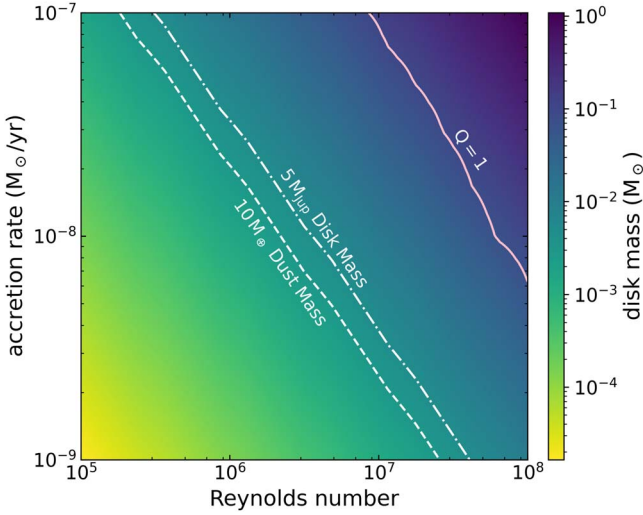


Figure 10. Total mass of the protoplanetary disk of Gl 86 A in terms of Reynolds number and accretion rate. The mass is negligible in the lower left corner, with small Reynolds numbers and low accretion rates, and large in the upper right corner, with large Reynolds numbers and large accretion rates. The dashed white line indicates a disk mass of $1000 M_{\oplus}$, or $3.0 \times 10^{-3} M_{\odot}$, or a dust mass of $10 M_{\oplus}$ assuming a dust-to-gas ratio of 10^{-2} . The dashed-dotted white line represents $5 M_{\text{Jup}}$ disk mass. The protoplanetary disk of Gl 86 A must have occupied the space to the right of these white lines in order to have possibly formed Gl 86 Ab. To the right of the pink line the disk is Toomre unstable ($Q < 1$) at its truncation radius.

have exceeded the planet’s current mass of $\geq 4.3 M_{\text{Jup}}$ (depending on the inclination). We adopt $5 M_{\text{Jup}}$ as the minimum disk mass that could have possibly permitted the formation of Gl 86 Ab.

We ignore Reynolds numbers higher than 10^8 , as such Reynolds numbers rarely occur, and a typical Reynolds number is only $\sim 10^5$ (AL94). For large Reynolds numbers, the truncation radii are so small that they are very close to the inner rim. However, as the disk mass is proportional to Re (see Equation (19)), it can still be unreasonably large when Re is large even if the disk mass is integrated from the inner rim to the truncation radius. Huge Reynolds numbers require extremely small viscous stresses α , and the resulting disk mass exceeds the current mass of Gl 86 A.

Figure 10 shows the total disk mass in terms of Reynolds number and accretion rate. With accretion rates ranging from 10^{-9} to $10^{-7} M_{\odot} \text{ yr}^{-1}$ and Reynolds numbers ranging from 10^5 to 10^8 , the total disk mass goes from 10^{-5} to $1 M_{\odot}$. The region to the right of the dashed (dashed-dotted) white line indicates dust (disk) mass higher than $10 M_{\oplus}$ ($5 M_{\text{Jup}}$). To the right of both lines, the disk exceeds the minimum mass to supply the material to form Gl 86 Ab.

Figure 10 shows that with a Reynolds number $\gtrsim 10^7$, the protoplanetary disk can contain enough material to form Gl 86 Ab despite its truncation at ≈ 2 au. This minimum mass corresponds to about twice the minimum-mass solar nebula (Hayashi 1981) integrated from 0.13 to 2 au. Still, this requires a very high efficiency in converting disk mass to planet mass. At very high disk masses, which would allow for a less efficient conversion of disk mass to planet mass, the disk approaches the Toomre stability limit (Safronov 1960; Toomre 1964). The pink line on Figure 10 indicates that this stability limit has been breached at the disk’s outer truncation radius.

4.2.4. Discussion

Changes to our assumptions can present further difficulties in accounting for Gl 86 Ab. One example is our assumption of a $Z = 0.010$ metallicity for the system. Literature measurements of $[\text{Fe}/\text{H}]$ for Gl 86 A vary from -0.30 (Ramírez et al. 2007) to -0.16 (Allende Prieto et al. 2004), while the majority fall between -0.25 and -0.20 (e.g., Santos et al. 2000, 2004; Ramírez et al. 2013). We adopt -0.23 for $[\text{Fe}/\text{H}]$ and 0.0134 for solar metallicity (Grevesse et al. 2012), which give $Z = 0.0134 \times 10^{-0.23} \approx 0.008$. We approximate this value to be 0.01 . Supposing that the actual metallicity is only $2/3$ of what we assume, it requires a disk mass of 1.5 times higher to get the same $10 M_{\oplus}$ dust mass. Then, the $10 M_{\oplus}$ dust mass line (dashed white line) in Figure 10 could move up and overlap with the $5 M_{\text{Jup}}$ (dashed-dotted white line) disk mass line. It might even surpass the $5 M_{\text{Jup}}$ line and give a stronger constraint.

Another challenge is the reliability of the planet formation mechanisms, namely, pebble accretion and planetesimal accretion. These mechanisms can be characterized by inefficient coagulation of the solid material onto the planetary core, despite that the formation of planets appears to be common and efficient (Howard et al. 2012). Guillot et al. (2014) demonstrate that the filtering efficiency of planetesimals decreases as they grow in size, being collided only by dust particles greater than a millimeter in size. Meanwhile, when most dust grows to some specific size, it drifts inward to the central star owing to gas drag and a slow inward flow of gas. Therefore, the embryos might need to be several times higher than $10 M_{\oplus}$. Other mechanisms, such as orderly growth and capture into vortices, might come to play to reduce the loss of solids onto the central stars. Inefficiencies in converting disk solids to a protoplanetary core, and subsequently accreting the disk onto the forming planet, would place the disk closer to the Toomre stability limit. Gl 86 Ab thus presents an essential example of a very massive, albeit truncated, disk and/or efficient conversion of a protoplanetary disk’s mass into a warm Jupiter.

One alternative that could circumvent the difficulty of planet formation is via the second-generation planet (Perets 2010). Such a scenario occurs if the planet formed less massive after the post-MS evolution of the companion star (called first-generation planet) and served as a seed for the second-generation planet by accreting material from the companion. We have denied mass transfer via Roche lobe overflow in Section 3.1. Nevertheless, wind mass transfer could deliver the metal-rich solid materials, forming a disk around the host star (Abate et al. 2013; Perets & Kenyon 2013), and making the second-generation planet a promising mechanism.

5. Conclusions

In this study we fit for the orbital parameters of the Gl 86 system based on RV and astrometric data. We find the white dwarf secondary, Gl 86 B, to have a mass $0.5425 \pm 0.0042 M_{\odot}$ and the inner planet Gl 86 Ab to have $m \sin i = 4.266_{-0.087}^{+0.11} M_{\text{Jup}}$. We cannot constrain the inclination and orientation of the inner planet, but we obtain good constraints on all other parameters. We obtain an eccentricity of 0.429 ± 0.017 and a semimajor axis of 23.7 ± 0.3 au for the white dwarf’s current orbit. In order to obtain a satisfactory fit to HST astrometry, we require an inflation of ≈ 10 mas in the relative astrometry uncertainties. This could also point to an unseen massive companion orbiting

Gl 86 B, which would make the system especially unique. The existence of such a companion might be confirmed or refuted with individual epoch astrometry from a future Gaia data release, since both Gl 86 A and Gl 86 B are detected in Gaia, or by further astrometric monitoring of the system.

Mass loss by the white dwarf Gl 86 B means that its current orbit differs from its primordial orbit. We combine the MESA with a current white dwarf mass of $0.5425 \pm 0.0042 M_{\odot}$ to infer an initial mass of $1.39 M_{\odot}$. We then run a simulation backward in time to derive the primordial orbit of Gl 86 AB. We verify that the semimajor axis a satisfies $M_{\text{tot}}a = \text{constant}$ and eccentricity e satisfies $\left\langle \frac{e}{i} \right\rangle = 0$, in agreement with analytic theory. When both stars were on the main sequence, we infer a semimajor axis of 14.8 au and an eccentricity matching its current value of 0.429. This relation assumes isotropic, adiabatic mass loss, as the maximum size of the Gl 86 B was not large enough to initiate Roche lobe overflow.
















Finally, we examine how the formation of Gl 86 Ab took place under such a dynamically challenging situation. We find a truncation radius of ≈ 2 au for Gl 86 A's protoplanetary disk, with somewhat smaller values at higher Reynolds numbers, by balancing the viscous stress and ILLR torque. We then derive an expression of the total disk mass and infer a total dust mass assuming a dust-to-gas ratio of 1%. Despite the short separation between the two stars when they were both on the main sequence, the disk mass is sufficient to provide the material to form Gl 86 Ab in the high accretion rate and large Reynolds number (low viscosity) range. This scenario requires an efficient conversion of dust to a planetary core. Inefficient conversion of material would require a more massive disk, which would then approach the Toomre stability limit at its outer truncation radius.

The Gl 86 system, with a $\gtrsim 4 M_{\text{Jup}}$ planet formed within a disk truncated at ≈ 2 au, demonstrates that giant planet formation is possible even in adverse circumstances. It shows that severely truncated disks around stars in binaries can birth super-Jovian exoplanets, and it provides an important benchmark for planet formation theory.

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Software: astropy (Astropy Collaboration et al. 2013; Price-Whelan et al. 2018), emcee (Foreman-Mackey et al. 2013), ptemcee (Vousden et al. 2016), mercury (Chambers 2012), MESA (Paxton et al. 2011, 2013, 2015, 2018, 2019), orvara (Brandt et al. 2021), scipy (Virtanen et al. 2020), numpy (Oliphant 2006; van der Walt et al. 2011), All the HST data used in this paper can be found in MAST: <https://doi.org/10.17909/s1za-k885>.

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