

Faraday tomography of LoTSS-DR2 data: I. Faraday moments in the high-latitude outer Galaxy and revealing Loop III in polarisation[★]

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ABSTRACT

Context. Observations of synchrotron emission at low radio frequencies reveal a labyrinth of polarised Galactic structures. However, the explanation for the wealth of structures remains uncertain due to the complex interactions between the interstellar medium and the magnetic field. A multi-tracer approach to the analysis of large sky areas is needed.

Aims. This paper aims to use polarimetric images from the LOFAR Two metre Sky Survey (LoTSS) to produce the biggest mosaic of polarised emission in the northern sky at low radio frequencies (150 MHz) to date. The large area this mosaic covers allows for detailed morphological and statistical studies of polarised structures in the high-latitude outer Galaxy, including the well-known Loop III region.

Methods. We produced a 3100 square degree Faraday tomographic cube using a rotation measure synthesis tool. We calculated the statistical moments of Faraday spectra and compared them with data sets at higher frequencies (1.4 GHz) and with a map of a rotation measure derived from extragalactic sources.

Results. The mosaic is dominated by polarised emission connected to Loop III. Additionally, the mosaic reveals an abundance of other morphological structures, mainly narrow and extended depolarisation canals, which are found to be ubiquitous.

Conclusions. We find a correlation between the map of an extragalactic rotation measure and the LoTSS first Faraday moment image. The ratio of the two deviates from a simple model of a Burn slab (Burn 1966) along the line of sight, which highlights the high level of complexity in the magnetoionic medium that can be studied at these frequencies.

Key words. ISM: general, structure, magnetic fields - radio continuum: ISM - techniques: polarimetric, interferometric

1. Introduction

In the last decade, radio astronomy at low frequencies has flourished as a result of major technical advancements and the development of a new generation of radio interferometers. One such instrument is the LOw-Frequency ARray (LOFAR; van Haarlem et al. 2013), which aims to, among other scientific goals, provide a deep imaging survey of the entire northern sky. Its ongoing 120 – 168 MHz survey, the LOFAR Two-meter Sky Survey (LoTSS, Shimwell et al. 2017, 2019), focusses on exploring the formation and evolution of supermassive black holes, galaxies, clusters, and large-scale structures in the Universe and our Galaxy. The observations of polarised Galactic synchrotron emission obtained in this survey are of extremely high value

for use in studies of the Galactic magnetic field and interstellar medium (ISM).

Polarised synchrotron emission associated with structures in the Milky Way is affected by Faraday rotation as it propagates through a web of a magnetised and ionised ISM. As it propagates, its linear polarisation plane is rotated by a wavelength-dependent angle ($\Delta\theta$) described by Faraday depth (Φ) as follows:

$$\frac{\Delta\theta}{[\text{rad}]} = \frac{\lambda^2}{[\text{m}^2]} \frac{\Phi}{[\text{rad m}^{-2}]} = \frac{\lambda^2}{[\text{m}^2]} 0.81 \int_0^d \frac{n_e}{[\text{cm}^{-3}]} \frac{B_{\parallel}}{[\mu\text{G}]} \frac{dl}{[\text{pc}]}, \quad (1)$$

where λ is the wavelength, n_e is the electron density, and B_{\parallel} is the magnetic field component parallel to the line of sight (LOS). The integral is evaluated over distance dl from the source (at distance 0) to the observer (at distance d). The Faraday depth is positive or negative if the average parallel component of the magnetic field is pointing towards or away from the observer, respectively.

[★] The movie associated to Appendix B is available at <https://www.aanda.org> and also at <https://data.fulir.irb.hr/islandora/object/irb:106>

In the simplest case of a background polarised source and a foreground Faraday rotating medium, the observed wavelength-dependent change of the polarisation angle is linear with λ^2 . The Faraday depth of the observed polarised emission is then equivalent to the rotation measure (RM), defined by the slope of the observed linear relation between θ and λ^2 (e.g. Manchester 1972; Ferrière et al. 2021).

The observed polarised emission can be disentangled into components according to the amount of Faraday rotation experienced by using the RM synthesis technique (Burn 1966; Brentjens & de Bruyn 2005). For a given location in the sky, this technique gives us a Faraday spectrum, that is to say a distribution of the observed polarised emission in Faraday depth. If RM synthesis is applied over a sky area, we can study the morphology of the observed polarised emission at different Faraday depths. Using this technique, we performed the so-called Faraday tomography, which allowed us to analyse complex distributions of magnetised and ionised gas along a LOS.

Rotation-measure synthesis has limitations which are defined by the following three parameters (Brentjens & de Bruyn 2005, see eq. 61-63): the maximum observable Faraday depth, Φ_{\max} , which is inversely proportional to the channel width of the observations, $\delta\lambda^2$; the resolution in Faraday depth, $\delta\Phi$, which is inversely proportional to the wavelength range the observation covers, $\Delta\lambda^2$; the largest scale in Faraday depth to which the observations are sensitive, $\Delta\Phi_{\max}$, which is inversely proportional to the minimum wavelength of the observation, λ_{\min}^2 . The wavelength dependence of both the resolution and the Faraday rotation (proportional to λ^2 , see Eq. 1) makes the power of RM synthesis at low radio frequencies twofold. We can study observed emission at high resolution in Faraday depth (up to 1 rad m^{-2}) and detect low column densities of magnetised and ionised gas. This is not possible at high radio frequencies ($\gtrsim 1 \text{ GHz}$) since the resolution is a few orders of magnitude lower than at low radio frequencies (Jelić et al. 2015; Van Eck 2018).

The structures seen in the Faraday spectrum can be either Faraday thin or thick (Brentjens & de Bruyn 2005). A structure is considered Faraday thin if $\lambda^2\Delta\Phi \ll 1$, where $\Delta\Phi$ is the extent of the source in Faraday depth. On the other hand, if $\lambda^2\Delta\Phi \gg 1$, the structure is called Faraday thick. Faraday thickness is wavelength-dependent, meaning that a structure, which is Faraday thick at low frequencies, becomes Faraday thin at higher frequencies.

Thus far, a number of authors have used RM synthesis to analyse Galactic polarised synchrotron emission in seven single field observations with LOFAR (Iacobelli et al. 2013; Jelić et al. 2014, 2015; Van Eck et al. 2017; Turić et al. 2021), each covering roughly 64 square degrees. These observations have revealed a plethora of structures, whose exact origin is still not fully understood. However, the multi-tracer analysis of the images has resulted in a clear association between neutral magnetised ISM components (dust and atomic hydrogen gas, HI) and structures seen in Faraday depths (Zaroubi et al. 2015; Kalberla & Kerp 2016; Jelić et al. 2018; Bracco et al. 2020). Van Eck et al. (2017) have even proposed that the observed emission originates from neutral regions in the ISM where Faraday depolarisation effects are small (e.g. see Sokoloff et al. 1998, and references therein). There are, however, still many uncertainties and the observed correlation between tracers of the multi-phase ISM is limited to only a few single fields. For example, many discovered structures extend outside a single field of view used in a particular study (Jelić et al. 2015), which again limits the interpretation and calls for analyses over larger areas of the sky.

This endeavour to significantly expand the coverage was made by Van Eck et al. (2019) who used LoTSS preliminary data. They performed Faraday tomography of 568 square degrees in the region of the Hobby-Eberly Telescope Dark Energy Experiment (HETDEX, Hill et al. 2008) spring field. In our work, we continue this effort by expanding the area of analysis even further. Our mosaic covers an area roughly 5.5 times larger than the one in Van Eck et al. (2019), making it the largest mosaic of the low-radio frequency polarised emission in the northern sky to date. Moreover, we are using data from LoTSS Data Release 2 (DR2, Shimwell et al. 2022), which were calibrated with a more comprehensive procedure than the one used for the preliminary data release (Shimwell et al. 2017). This resulted in better quality images that, for example, suffer from artefacts around bright sources less and have a lower amount of instrumental polarisation.

The goal of this paper is to present the first LoTSS-DR2 mosaic and highlight some of the main structures we see in this large sky area. While the large mosaic area allows us to gain better insight into the origin of observed structures, this paper serves as a first introduction to the LoTSS mosaics and as an in-depth analysis of the different structures found which will be a topic of follow-up papers. Here, we focus on a statistical analysis of the whole mosaic in an effort to shed light on the LOS structure of the diffuse ISM. We achieve this by comparing our Faraday tomographic results with results based on observations at higher frequencies (1.4 GHz) by Dickey et al. (2019) and with the total Galactic RM map produced by Hutschenreuter et al. (2022). The comparison was carried out through statistical Faraday moments, a statistical tool, which was first applied to Faraday spectra by Dickey et al. (2019), that makes it possible to analyse the complexity of Faraday spectra by taking multiple Faraday components weighted by their intensity into account. We used the moments in addition to simple inspection of the peak intensity and the corresponding depth in the Faraday cube (e.g. Jelić et al. 2015; Van Eck et al. 2017).

The paper is organised as follows. In Sect. 2, we describe the LoTSS-DR2 data used in the analyses, as well as the procedure we used to create the mosaic in Faraday depth. The resulting mosaics in equatorial (RA, Dec) and Galactic coordinates (l , b) are presented in Sect. 3, together with the results of Faraday tomography highlighting the polarised emission associated with Loop III. Faraday moments of the LoTSS-DR2 data are presented in Sect. 4. We discuss them and compare them with high-frequency polarisation data (DRAO GMIMS, Dickey et al. 2019) and the total Galactic RM map (Hutschenreuter et al. 2022) in Sect. 5. The paper finishes with a summary and conclusions presented in Sect. 6.

2. Data and processing

In this section, we describe the LoTSS-DR2 data and the derived data products used in this paper. We give an overview of the RM synthesis parameters and the produced Faraday cubes. Finally, we outline the procedure of combining the Faraday cubes into the mosaic cube.

2.1. LoTSS-DR2 very low resolution images

LoTSS (Shimwell et al. 2017, 2019) is an ongoing 120 – 168 MHz survey of the northern sky with the LOFAR High Band Antennas (HBA, van Haarlem et al. 2013). The DR2 of the survey (Shimwell et al. 2022) presents data from 841 individual fields that span a combined area of 5 634 square degrees. This is

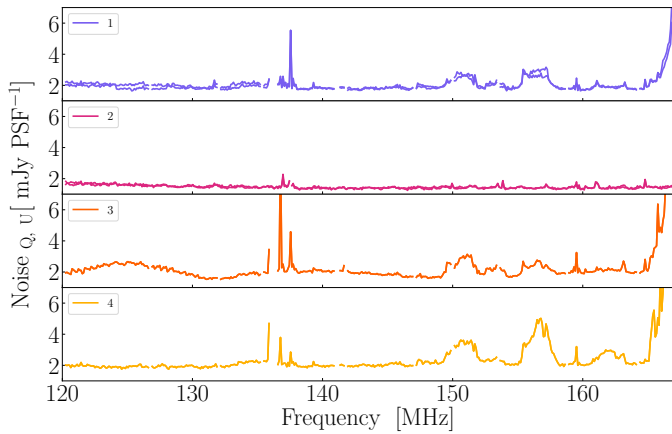


Fig. 1. Noise in both Q and U cubes not corrected for a primary beam, as a function of the frequency for four fields marked with respective colours and numbers in Fig. 5. Some of the missing channels or channels with excess noise are shared among several fields, while others are specific for a single field. The noise excess in the observations comes from the radio frequency interference. Noise in Q and U is comparable; therefore, the lines mostly overlap.

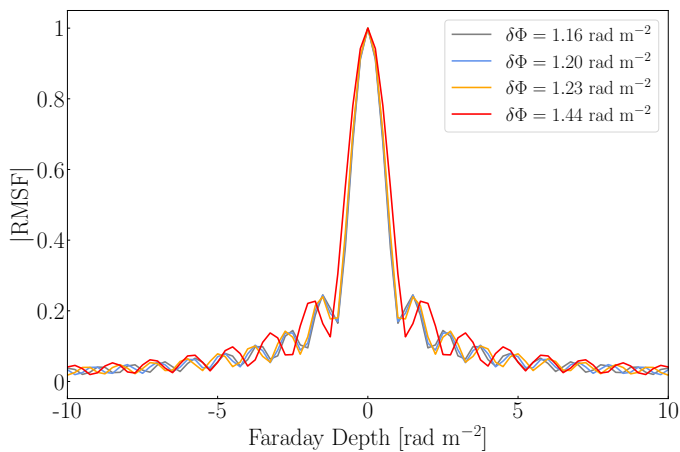


Fig. 2. RMSF functions of observations with different upper frequencies (see Table 2). While the main lobe of the red function (representing 0.5% of data) is visibly wider, other functions differ only marginally.

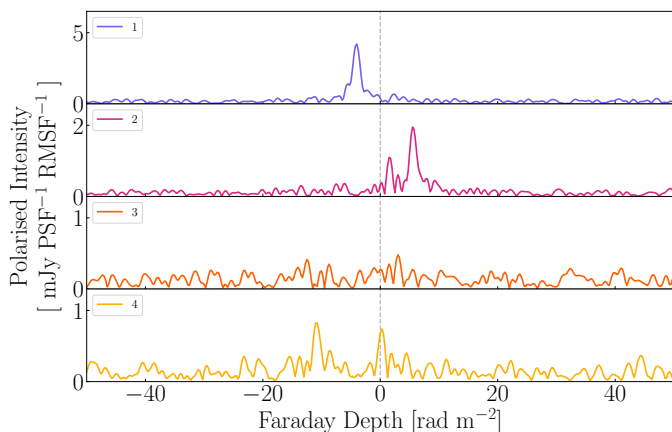


Fig. 3. Faraday spectra at four distinct locations in the Faraday cube mosaic. The locations are marked in Fig. 5 with respective colours and numbers. The Faraday spectra shown in this plot are chosen to probe some of the distinct features discussed in Sect. 3. Faraday spectra 1 and 4 probe Loop III while Faraday spectra 2 and 3 probe the zig-zag structure and the very low S/N area in the mosaic, respectively.

Table 1. Areas in the LoTSS mosaic that were previously studied.

Field	RA (deg)	Dec (deg)	Area (deg ²)	Reference
HETDEX	228.8 - 161.3	45 - 57	568	(4)
3C196	123.4	48.2	64	(2), (3), (5)
3C196 - B	123.4	40.4	64	(5), (6)
3C196 - C	131.2	33.9	64	(5), (6)
ELAIS - N1	242.8	55	64	(1)

References. (1) Jelić et al. (2014), (2) Jelić et al. (2015), (3) Jelić et al. (2018), (4) Van Eck et al. (2019); (5) Bracco et al. (2020), (6) Turić et al. (2021)

Table 2. Frequency range and RM synthesis parameters in different observations.

Frequency range (MHz)	$\delta\phi$ (rad m ⁻²)	$\Delta\Phi_{\max}$ (rad m ⁻²)	Field percentage (%)
120 - 167	1.16	0.97	92.4
120 - 165	1.20	0.95	6.4
120 - 163	1.23	0.93	0.7
120 - 153	1.44	0.82	0.5

Notes. This table shows the resolution in Faraday depth $\delta\phi$ and the largest scale in Faraday depth to which the observations are sensitive. The values change from field to field due to different frequency ranges in cubes (See Fig. 5). Here we included only the 440 fields used to make the final mosaic.

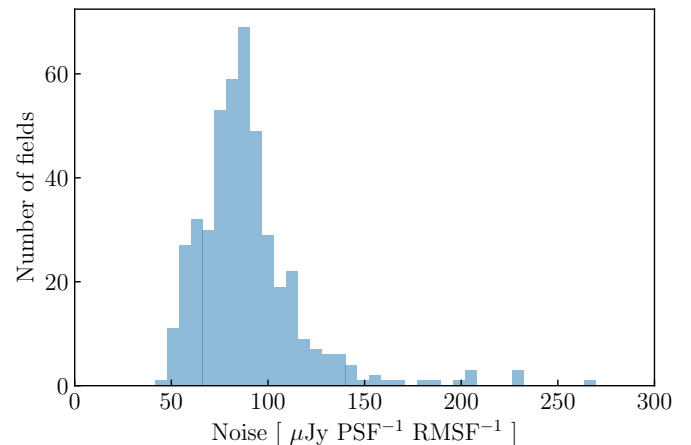


Fig. 4. Histogram of noise in each polarised intensity cube, approximated as a standard deviation multiplied by a factor of $\sqrt{2}$ over each cube at $\Phi = -50$ rad m⁻². The mean value of this distribution represents the mean value of noise in the produced polarised intensity cubes.

split between two regions, one centred at RA = 0^h and another at RA = 12^h.

The data have been processed in a two-step procedure. The first step was performed with the PreFactor pipeline¹ (van Weeren et al. 2016, de Gasperin et al. 2019), which corrects for direction-independent effects in the data, such as the XX-YY phase offset, the instrumental time delay associated with clocks, bandpass, and ionospheric Faraday rotation, before calibrating the data against a sky model derived from the Tata Institute of Fundamental Research GMRT Sky Survey (TGSS, Intema et al. 2017). This pipeline makes use of software packages such as the LOFAR Solution Tool (de Gasperin et al. 2019), Default

¹ <https://github.com/lofar-astron/prefactor>

Pre-Processing Pipeline (DPPP [Dijkema 2018](#)), and AOFlogger ([Offringa 2011](#)). For efficiency, the pipeline is deployed on the LOFAR archive compute facilities ([Mechev et al. 2017](#); [Drabent et al. 2019](#)).

The second, and more computationally expensive step was to perform direction-dependent calibration and imaging using the Direction Dependent Facet (DDF) pipeline², which has been revised for LoTSS-DR2 (and the LoTSS Deep Fields) to improve the dynamic range and image fidelity (see [Tasse et al. 2021](#) for a full description of the pipeline). This pipeline makes use of the Wirtinger derivative ([Tasse 2014](#); [Smirnov & Tasse 2015](#)) for direction-dependent calibration and DDF ([Tasse et al. 2018](#)) to apply these solutions whilst imaging. The processing was primarily performed on the LOFAR UK compute facilities³ in Hertfordshire with a small fraction also done in Hamburg, Leiden, and Bologna. The products from the DDF pipeline, which are stored in Leiden, include Stokes I , Q , U , and V images at different angular and frequency resolutions, as well as calibration solutions and compressed data sets to allow for re-imaging when necessary.

In this work, we analyse 461 calibrated pointings, covering around 3100 square degrees centred at RA = 12^h. This area covers previously studied areas, as listed in [Table 1](#). We use the LoTSS-DR2 Stokes Q and U very-low resolution (vlow) images ([Shimwell et al. 2022](#)), which are now publicly available through the LOFAR Surveys website⁴. The vlow images have an angular resolution which varies between 5.5 and 4 arcmin across observed frequencies from 120 MHz to 167 MHz (see [Table 2](#)). The frequency resolution of each of the 480 frequency channels is 97.6 kHz. To produce the mosaic, we used both the primary beam corrected and uncorrected images at a common resolution of 5.5 arcmin.

The data were taken over multiple ~8h observations during different LOFAR observing cycles. The noise is comparable in most of the observations. [Figure 1](#) shows the noise in Stokes Q and U images not corrected for the primary beam at different frequencies for four different observations. The noise was calculated as a standard deviation in the corner of the image, where the polarised emission is not present. Over the observed frequency range, there are some common frequency channels, which are affected by broad radio-frequency interference ([Offringa et al. 2013](#)). Each observation also has a few additional low-quality or missing frequency channels. To identify those, we used the criterion that the noise in each channel should not be higher than 4σ above the mean value of the noise over the full bandwidth, where σ is the standard deviation of the noise over the full bandwidth. It is important to note that we identified and flagged bad channels in each observation independently to avoid flagging a large amount of good quality channels.

2.2. RM synthesis

To produce the Faraday cubes based on the LOFAR observations, we performed RM synthesis using `pyrmsynth-lite`⁵. We did not weigh the data during this process as the noise is comparable across the selected frequency channels. The final cubes span a Faraday depth range from -50 rad m^{-2} to $+50 \text{ rad m}^{-2}$ in steps of 0.25 rad m^{-2} . Faraday spectra were not deconvolved. The sidelobes of the rotation measure spread function (RMSF)

are lower than 20% and the signal-to-noise ratio (S/N) is, in general, so low that deconvolution would have a very little effect (see [Fig. 2](#)). Four examples of Faraday spectra found in different areas of the mosaic are shown in [Fig. 3](#).

The resolution in Faraday depth, defined by the width of the RMSF function, is $\delta\Phi = 1.16 \text{ rad m}^{-2}$ for 92.4% of the observations (see [Table 2](#)). Some observations have marginally poorer resolution due to a slightly lower upper frequency in the observed range (see [Sect. 1](#) and [Fig. 2](#)). Similarly, there is also a small difference in the largest Faraday structure that can be resolved in some observations ($\Delta\Phi_{\text{max}}$, see [Table 2](#)). In all our observations, only Faraday thin structures can be detected, or the edges of Faraday thick structures (as described in [Brentjens & de Bruyn 2005](#); [Van Eck et al. 2017](#)), as the resolution in Faraday depth is comparable to the largest observable Faraday scale.

The histogram in [Fig. 4](#) shows the distribution of the noise estimated from the polarised intensity Faraday cube for each observation. The noise was calculated as the standard deviation of the polarised intensity at $\Phi = -50 \text{ rad m}^{-2}$ multiplied by a factor of $\sqrt{2}$. This factor comes from the noise in polarised intensity being distributed according to the Rician distribution and it is equivalent to the normally distributed noise in Q and U (e.g. [Brentjens & de Bruyn 2005](#); [Hales et al. 2012](#)). The image at this Faraday depth is dominated by noise and the noise value obtained from it is consistent with noise at other noise-dominated Faraday depths. The distribution has a mean value of $117 \mu\text{Jy PSF}^{-1} \text{ RMSF}^{-1}$, which is lower by roughly a square root of the number of frequency channels compared to the noise in the Stokes Q and U images given at different frequencies ($\sim 1.8 \text{ mJy PSF}^{-1}$), as expected. Some observations have much higher noise values and show systematic artefacts. The 21 cubes (out of the total 461) in which the noise exceeds $200 \mu\text{Jy PSF}^{-1} \text{ RMSF}^{-1}$ are excluded from further analyses. The total number of cubes used in [Sect. 3](#) to construct the mosaic is 440.

2.3. Mosaicing

We used `Montage`⁶, an Astronomical Image Mosaic Engine, to re-project and combine the Faraday cubes from different observations into a single mosaic cube. This software package has the functionality to deal with different projections while conserving the flux. When re-projecting on curved grids (in our case from a gnomonic sinusoidal projection to a curved Aitoff projection), pixel areas change and conservation of the flux needs to be taken into account by redistributing the flux from one grid to another. We used `Montage` modules `mProjExec` and `mAdd` for this purpose. The flux is redistributed by weighing each input pixel by the sky area of overlap with the output pixel. When combining multiple overlapping pixels, it assigns the area-weighted average of the pixels.

Additionally, we introduced a weighting scheme to account for the following: (i) variations of the noise across Faraday cubes of different observations and (ii) overlaps between them. We weighed each observation by its noise and by the primary beam attenuation factor (pb):

$$w_{\text{obs}} = \frac{1}{\sigma_{\text{obs}}^2} * \frac{1}{\text{pb}^2}, \quad (2)$$

where σ_{obs} is the standard deviation of the noise in each primary beam uncorrected Faraday cube, calculated at a Faraday depth

⁶ <http://montage.ipac.caltech.edu>

² <https://github.com/mhardcastle/ddf-pipeline>

³ <https://lofar-uk.org/lucf.html>

⁴ <https://lofar-surveys.org>

⁵ https://github.com/sabourke/pyrmsynth_lite

of -50 rad m^{-2} . The primary beam was assessed by dividing the primary beam corrected cube by the uncorrected cube.

Being a square root quantity, the noise in the polarised intensity Faraday cube does not have a normal distribution as the noise in Stokes Q and U Faraday cubes. Therefore, the mosaicing was done in Stokes Q and U after which we created the polarised intensity mosaic cube, as $P = \sqrt{Q^2 + U^2}$.

In practice, we first created a weighted mosaic of primary beam corrected images ($\text{img}_{\text{pbcorr}}^{Q,U}$) in Stokes Q and U at each Faraday depth Φ :

$$\text{Mosaic}^{Q,U}(\Phi) = \frac{\text{mosaic}(\text{img}_{\text{pbcorr}}^{Q,U}(\Phi) * w_{\text{obs}})}{\text{mosaic}(w_{\text{obs}})}. \quad (3)$$

The created 2D mosaics were then combined into a mosaic Faraday cube.

3. The LoTSS mosaic Faraday cube

The final mosaic spans an area from $8^{\text{h}}00^{\text{m}}$ to $16^{\text{h}}40^{\text{m}}$ in right ascension and from 30° to 70° in declination. Figure 5 gives an overview of all LoTSS observations in this area in equatorial coordinates. Filled-in circles correspond to the location of 440 observations used in the final mosaic. Different colours illustrate small variations in the Faraday depth resolution in different fields. Empty circles are observations that were removed due to high noise or simply missing observations.

The central positions of observations are typically separated by 2.58° . Each pointing has six nearest neighbours within 2.80° . The primary beam full width half maximum (FWHM) of each observation ranges from 3.40° to 4.75° over the observed frequencies (Shimwell et al. 2019), so that the LoTSS survey has a very good coverage. Thus, the removal of 21 observations from the final mosaic cube did not affect the coverage greatly, except in places where several neighbouring pointings were removed. In these areas none of the surrounding primary beams overlap within their FWHM, so we excluded them from our further analysis.

The noise across the mosaic is represented by polarised intensity at $\Phi = -50 \text{ rad m}^{-2}$, whose distribution is shown in Fig. 6. A typical value for the noise, that is the width of distribution in Fig. 6, is $50 \mu\text{Jy PSF}^{-1} \text{ RMSF}^{-1}$. This was calculated excluding the regions where the noise is boosted by the primary beam (marked with a red contour in Fig. 7). These regions are mostly at boundaries of the mosaic and in the aforementioned areas with the excluded observations. The mask marked with red contours in Fig. 7 is used for statistical analysis of the data throughout the paper. There is a positive polarised intensity bias of $66 \mu\text{Jy PSF}^{-1} \text{ RMSF}^{-1}$. We did not correct the data for this bias as it did not affect the qualitative analysis that is the focus of this paper.

Figures 8 and 9 summarise the overall results of Faraday tomography in the mosaic area. They give the maximum intensity of Faraday spectra for each pixel in the mosaic, presented in equatorial and Galactic coordinates, respectively. Each presented projection has some advantages for the analysis of the observed structures. Different colours in Figs. 8 and 9 illustrate the emission observed at different Faraday depth ranges and the colour brightness indicates intensity of the emission. We chose the Faraday depth range from -30 to 30 rad m^{-2} as most of the emission is found there (see Appendix B). The colour bins were chosen to best present large structures visible in the mosaic since the full complexity of a 3D Faraday cube is difficult to represent

in a single 2D image. The binning is finer at negative Faraday depths, where we see more emission peaks than at positive Faraday depths. This choice of binning is not necessarily optimal for every region of the mosaic; some local features might be better represented with a different binning. In the following subsections, we further discuss the emission features.

3.1. Polarised emission associated with Loop III

The mosaic viewed in Galactic coordinates (Figs. 8, 10) reveals a striking loop-like structure dominating a large area in the bottom part of the mosaic. This structure is in close proximity and follows the shape of the radio Loop III, centred at $l = 124^\circ$ and $b = 15.5^\circ$ in total intensity (Berkhuijsen 1971). The polarised emission of the loop is also seen at higher radio frequencies (Vidal et al. 2015; Planck Collaboration XXV 2016, Peel et. al, in prep.); however, it is located several degrees in latitude higher than the total intensity emission. In the LoTSS data, at low frequencies, the loop-like emission mostly overlaps with the Loop III polarised emission at higher frequencies; however, its emission peaks at latitudes 5 to 10 degrees higher and extends to latitudes several degrees further up. We therefore associate the loop-like structure observed in the bottom part of the mosaic with the polarised emission of radio Loop III. The distance to Loop III was estimated to be between 150 pc and 250 pc (Spoelstra 1972; Lallement et al. 2003; Kun 2007), which is in agreement with the observed large angular size of tens of degrees across the sky.

Towards the edge of Loop III, we found continuous depolarisation canals following the loop curvature and stretching over tens of degrees. Depolarisation canals are narrow and extended regions in the image where the emission is significantly reduced, which we mostly associate with beam depolarisation in areas showing discontinuity in polarisation angles (Haverkorn & Heitsch 2004; Jelić et al. 2015). There are also depolarisation canals which are perpendicular to the direction of the loop. They are less prominent, shorter (several degrees in length), and more densely distributed compared to the aforementioned depolarisation canals. The observed structures are evidently not completely disordered. Their morphology suggests connection with a large-scale shell, which was possibly formed by one or more supernovae at the centre of the loop (Berkhuijsen 1971; Kun 2007). One has to bear in mind that the shortest baselines used in LoTSS observations (100 m) allow our mosaic to be sensitive to emission on an angular scale up to $\sim 1^\circ$ (Shimwell et al. 2017). Therefore, in the mosaic we might be missing the contribution from angular scales larger than $\sim 1^\circ$. Nevertheless, in some regions of the mosaic, we see structures spanning over several single field observations. Continuous organisation of these small-scale structures points to a common underlying large-scale morphology.

At different Faraday depths, polarised emission associated with the loop seems to ‘travel’ from the loop centre outwards, creating a gradient from -30 rad m^{-2} at lower Galactic latitudes to $+6 \text{ rad m}^{-2}$ at higher Galactic latitudes (see Faraday depth mosaic movie and Fig. 8). The gradient is characterised by changes of $\sim 0.5 - 1 \text{ rad m}^{-2} \text{ deg}^{-1}$ mostly in the direction parallel to the loop edge. However, due to the complex morphology of this emission, the gradient direction is perpendicular to the loop in some areas (e.g. westernmost part of the loop, around $l = 100^\circ$). A more detailed analysis of the observed Loop III emission gradient is out of the scope of this paper. At Faraday depths higher than $+6 \text{ rad m}^{-2}$, there is almost no emission associated with the loop. The mean polarised intensity of emission in the loop area is $2 \text{ mJy PSF}^{-1} \text{ RMSF}^{-1}$. Although not recognised

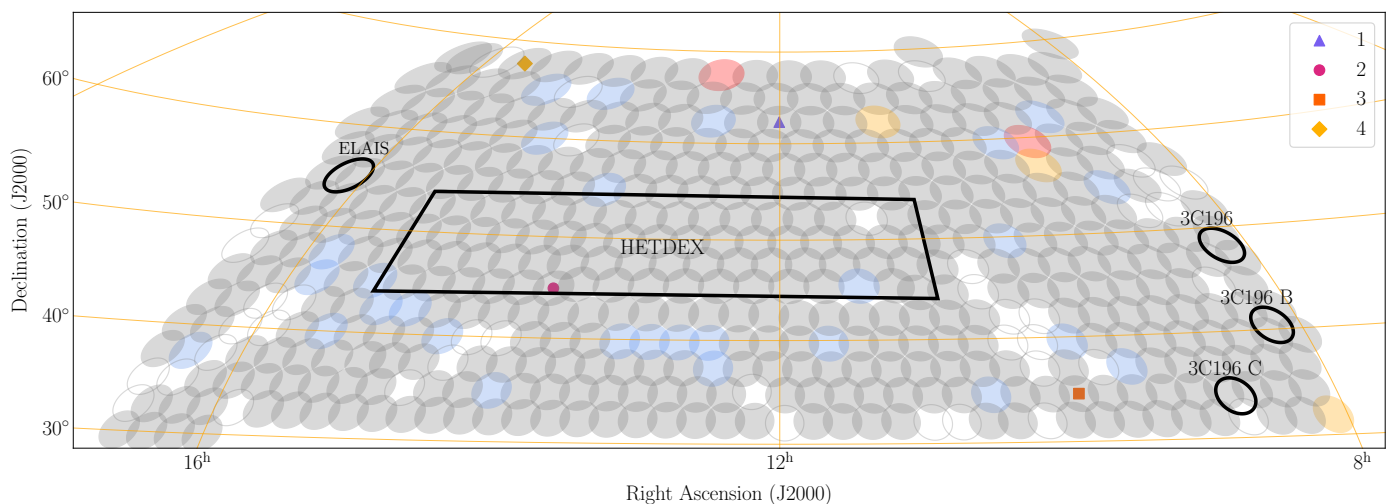


Fig. 5. Mosaic coverage shown in equatorial coordinates. Radii of the circles correspond to the largest primary beam FWHM of the LoTSS survey (4.75°). Red, orange, blue, and grey circles mark Faraday space resolution of 1.44 , 1.23 , 1.20 , and 1.16 rad m^{-2} , respectively (see Table 2). Areas previously studied by different authors are outlined in black (see Table 1 for more information). Symbols in the legend mark fields whose noise and spectra are shown in Figs. 1 and 3, where they are drawn with a corresponding colour and marked with numbers 1 through 4. Empty circles outlined in grey mark bad quality or missing observations.

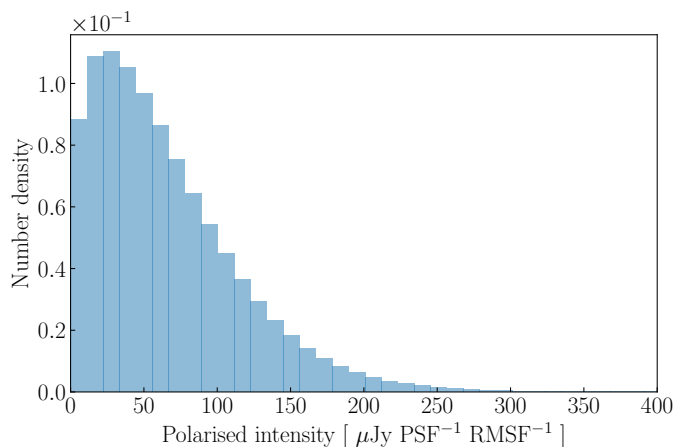


Fig. 6. Histogram of polarised intensity of the mosaic at Faraday depth $\Phi = -50$ rad m^{-2} (Fig. 7). The width of this distribution, approximated by the standard deviation multiplied by $\sqrt{2}$, gives an estimate of the noise level in the mosaic, 71 $\mu\text{Jy PSF}^{-1} \text{RMSF}^{-1}$, while its mean gives the polarisation bias, 66 $\mu\text{Jy PSF}^{-1} \text{RMSF}^{-1}$.

as such, a small part of the loop was already seen in the LoTSS-PDR mosaic that covered the HETDEX spring field region and was analysed by Van Eck et al. (2019).

3.2. Other morphological features of polarised emission

Due to projection effects present in Galactic coordinates, an equatorial projection (Fig. 9) is used to better highlight other structures in the area surrounding Loop III. While most of the emission unrelated to the loop is patchy and faint, one structure is clearly present at positive Faraday depths in the south-eastern area of the mosaic. This zig-zag structure is located between RA $13^{\text{h}}00^{\text{m}}$ and $15^{\text{h}}00^{\text{m}}$ and Dec 30° and 55° . The emission associated with this structure first appears at around $+2$ rad m^{-2} and then builds up towards higher Dec creating a gradient up to $\sim +10$ rad m^{-2} . The structure is best seen at $+8$ rad m^{-2} (see Appen-

dices A, B, and the Faraday cube movie). The mean polarised intensity of this structure is 1.2 $\text{mJy PSF}^{-1} \text{RMSF}^{-1}$.

The emission coming from the zig-zag structure is very hard to disentangle from Loop III emission in the Faraday depth range from 0 to 6 rad m^{-2} . It could be a separate structure as it shows no clear morphological connection to the loop at lower or higher Faraday depths, and it has a distinctive configuration at Faraday depths higher than roughly 6.5 rad m^{-2} . However, we cannot exclude the possibility that it is connected to Loop III emission. The zig-zag structure seems to be connected to the south-west filament from the LoTSS-PDR polarisation images of the HETDEX field (Van Eck et al. 2019), where it is not fully visible, in part because it extends outside of the field of view, but mainly because it is in the area of a big artefact around the source 3C 295. Due to significant improvements (Tasse et al. 2021; Shimwell et al. 2022) in the data calibration since the preliminary data release (Shimwell et al. 2017), the artefact is no longer present in our data. We discuss the zig-zag structure again in Section 4.

The central part of the south-western quarter of the mosaic is characterised by consistently low polarised intensity of 0.8 $\text{mJy PSF}^{-1} \text{RMSF}^{-1}$, on average, which is two times lower than the mosaic average of 1.6 $\text{mJy PSF}^{-1} \text{RMSF}^{-1}$. Part of this area (west from 9^{h}) is in the vicinity of the 3C 196 radio source and it has been previously studied by Jelić et al. (2015); Zaroubi et al. (2015); Jelić et al. (2018); Bracco et al. (2020); Turić et al. (2021). The LoTSS mosaic shows that this westernmost region, as well as the easternmost region of the mosaic, has many more depolarisation canals that are seen to extend well beyond the fields in which they were observed up until now. The characteristics of the depolarisation canals found in the mosaic will be investigated in future work.

4. Faraday moments

Faraday moments are a useful alternative tool for statistical analysis of Faraday tomographic cubes, giving us information similar to the maximum polarised intensity and the corresponding Faraday depth in images presented in the previous subsection (Figs. 8, 9). Both of these methods are a way to represent 3D

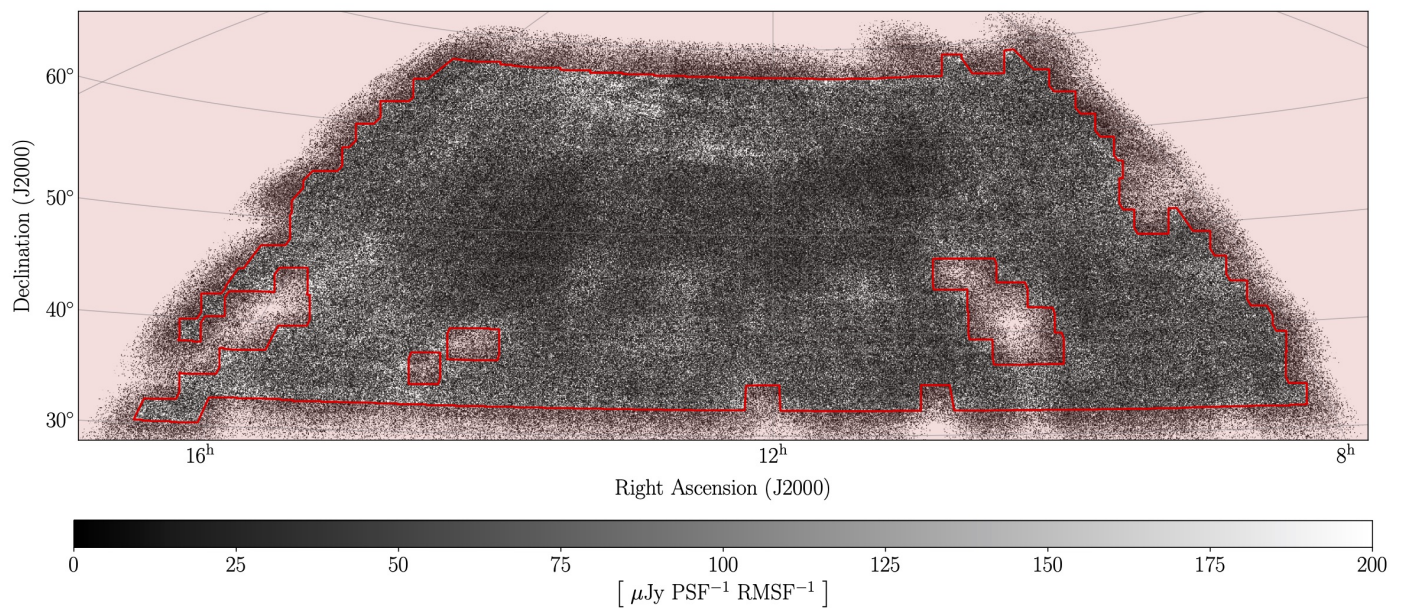


Fig. 7. Polarised intensity image of the mosaic at Faraday depth $\Phi = -50 \text{ rad m}^{-2}$, corresponding to the noise level across the mosaic. The red contour marks the mask used in analyses throughout the paper to exclude areas shaded in red.

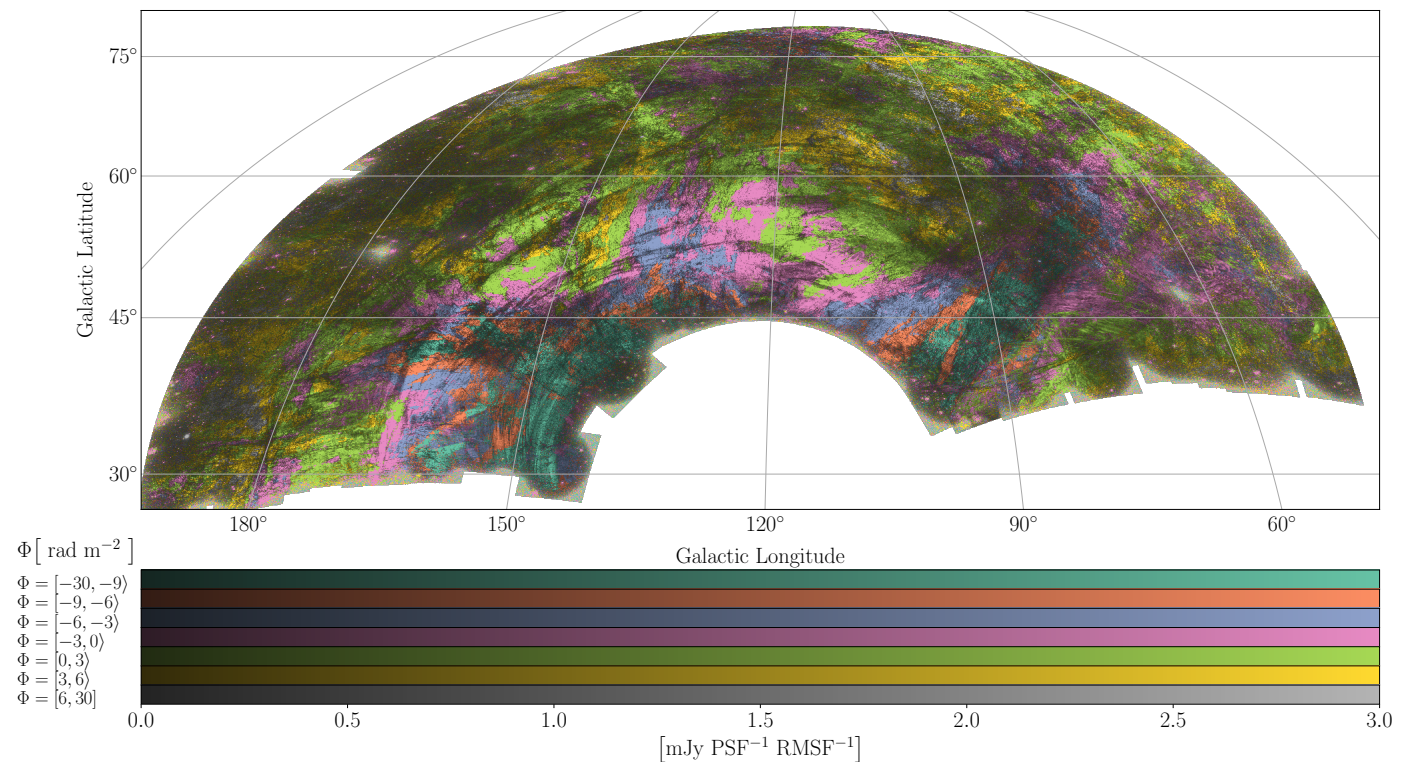


Fig. 8. Maximum polarised intensity per Faraday depth range in the LoTSS mosaic in Galactic coordinates (Mollweide projection), coloured based on the Faraday depth range at which the peak of the emission is found. The intensity of $1 \text{ mJy PSF}^{-1} \text{ RMSF}^{-1}$ corresponds to $\sim 0.5 \text{ K RMSF}^{-1}$.

spectral information from a Faraday cube in 2D images. The advantage of using statistical moments, over simply finding the maximum peak in the spectra, is the ability to take the complexity of spectra containing more than one Faraday structure into account, as is discussed in the appendix of [Dickey et al. \(2019\)](#). Following [Dickey et al. \(2019\)](#), we calculated the three moments of the lowest order.

The zeroth Faraday moment, M_0 , is the polarised intensity integrated over the full Faraday depth range, given in units of

$\text{Jy PSF}^{-1} \text{ RMSF}^{-1} \text{ rad m}^{-2}$. The zeroth moment is similar to the maximum polarised intensity image, particularly in areas where Faraday spectra are dominated by a single component. Differences occur in areas where Faraday spectra have multiple components, which have a similar polarised intensity.

The first Faraday moment, M_1 , is the polarised intensity weighted mean of Faraday spectra in units of rad m^{-2} . It gives similar information to the colour in [Figs. 8, 9](#), showing Faraday depth of the maximum polarised intensity. However, it gives

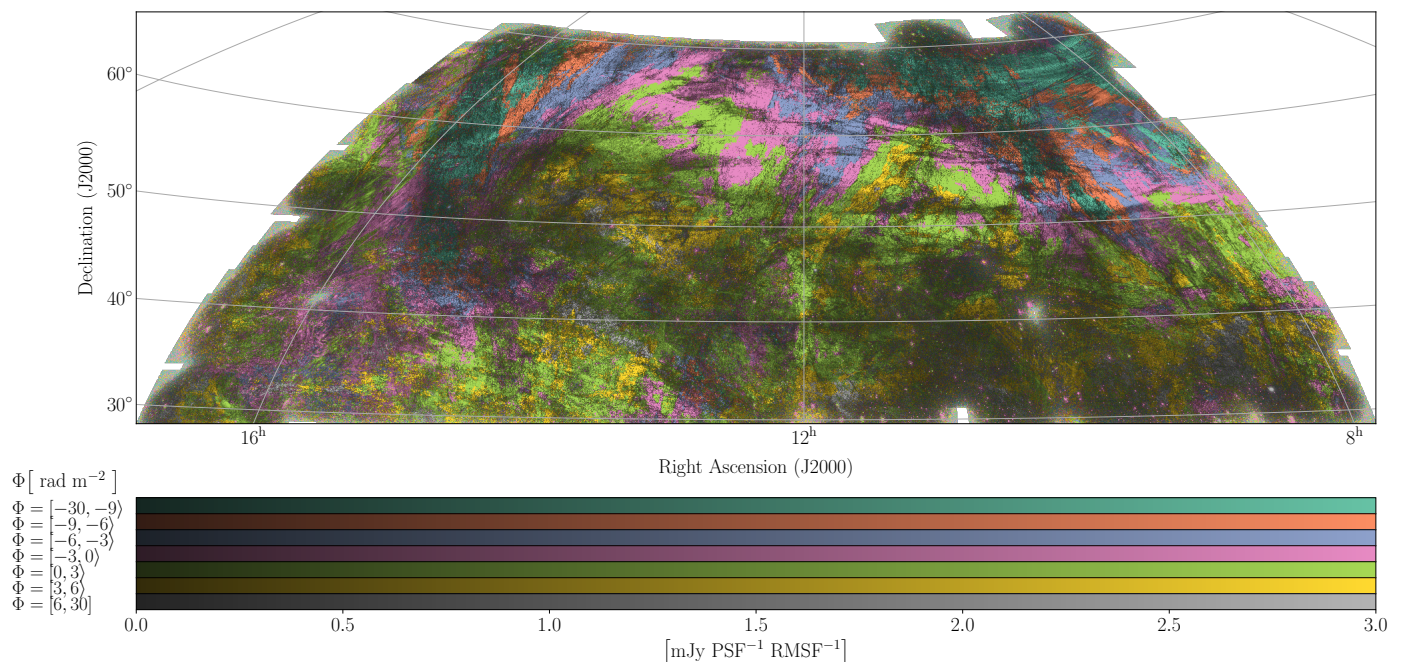


Fig. 9. Maximum polarised intensity per Faraday depth range in the LoTSS mosaic in equatorial coordinates, coloured based on the Faraday depth range at which the peak of the emission is found. The intensity of 1 mJy PSF⁻¹ RMSF⁻¹ corresponds to ~ 0.5 K RMSF⁻¹.

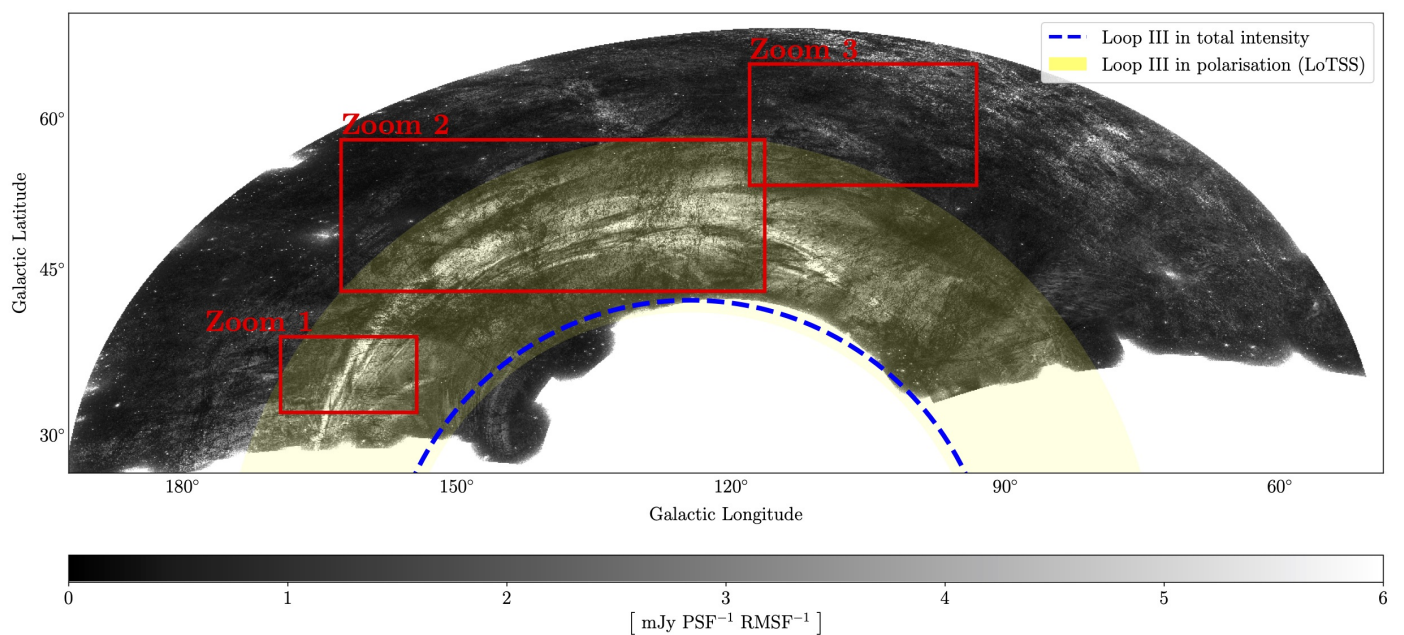


Fig. 10. Maximum polarised intensity image given in Galactic coordinates (Mollweide projection) with some of the interesting features outlined. The area shaded in yellow is the area in which we see Loop III in LoTSS data. The blue dashed line represents the location of Loop III in total intensity as seen by Berkhuijsen (1971). Red rectangles mark areas that are magnified in Appendix A, Figs. A.1, A.2, A.3 .

a better estimate of the mean Faraday depth, Φ_{mean} , as it takes multiple components present in complex Faraday spectra into account.

The second Faraday moment, M_2 , is the intensity weighted variance of Faraday spectra. The square root of the second moment gives the spread of the Faraday spectrum in units of rad m⁻². This variable quantifies the complexity of Faraday spectra – low values were obtained for spectra dominated by one component and high values were obtained for multi-component spectra. It can also be interpreted as the width of the Faraday depth range within which the polarised emission is observed.

When calculating Faraday moments, one has to exclude noise-dominated areas in the data, otherwise these areas would give rise to large errors. This is especially true for the second moment image, where adding in quadrature increases the effect of noise. In our analysis, we use a threshold of 460 $\mu\text{Jy PSF}^{-1} \text{RMSF}^{-1}$, which is around six times the typical level of noise in polarised intensity, and we exclude all pixels with lower values. This condition completely masks regions with Faraday spectra such as the one represented by Faraday spectrum 3 in Fig. 3. We also exclude the masked area shown in Fig. 7, where the noise is boosted by the primary beam either at the

boundaries of the mosaic or in the regions where we removed bad quality observations. In total, around 40% of the original data are not used in our Faraday moment analysis.

Calculated Faraday moment images (M_0 , M_1 , and M_2) are presented in equatorial coordinates in Fig. 11. The zeroth moment shows Loop III as the dominating feature. We also see small-scale emission in the south-eastern quarter of the mosaic, as mentioned in the previous section. In the first moment image (Fig. 11, middle panel), the blue colour corresponds to structures at negative Faraday depths, and the red colour corresponds to structures at positive Faraday depths. A large-scale structure at negative Faraday depths in the upper part of the mosaic is connected with Loop III. Consistent, negative Faraday depth implies that the average parallel component of the magnetic field in the loop area is pointing away from us. Below Loop III, the mosaic is dominated by structures at positive Faraday depths. The fact that Loop III remains as striking in zeroth and first moment images as in Fig. 9, means that it is the dominant feature along these LOSs, contributing the most to the moments.

The second moment image (Fig. 11, bottom panel) shows that many regions across the mosaic have complex Faraday spectra. However, in the region of Loop III, we do not see a distinct structure. Values in this region are mostly low, indicating simple Faraday spectra with Loop III emission dominating over other emission along the same LOS. The most distinguished structure seen in the image is the zig-zag structure, which was previously described in Section 3.2. High values for the second moment along the zig-zag structure indicate complex Faraday spectra, composed of multiple Faraday structures along the Faraday depth. An example of such a spectrum is given in Fig. 3 (spectrum 2), in which two peaks are clearly visible – the one closer to zero comes from emission connected to the loop and the other one comes from the zig-zag structure. Such Faraday spectra can arise from two different physical scenarios. The first is associated with the presence of two or more Faraday thin structures of similar intensities along the LOS. The second is associated with the edges of a Faraday thick structure at these frequencies. To distinguish between the two scenarios, one can use observations at higher frequencies, where structures which are Faraday thick at low radio frequencies, will become Faraday thin. In the case of a Faraday thick structure (at low frequencies), we expect the first and the second moments found at the two radio-frequency regimes to be comparable. This comes from the fact that at low frequencies, we observe the edges of the Faraday thick structure (Brentjens & de Bruyn 2005; Van Eck et al. 2017). The same structure observed at high frequencies will become Faraday thin, and found at a Faraday depth corresponding to the average Faraday depth of the edges observed at low frequencies. Another possibility to discriminate between the two aforementioned physical scenarios is to use distance estimations for the structures in Faraday spectra as was done in Van Eck et al. (2017); Thomson et al. (2019).

5. Comparison with DRAO GMIMS data and the Galactic Faraday Sky map

We compared our results with the Faraday moment maps presented by Dickey et al. (2019), with an angular resolution of 40 arcmin, derived from the preliminary data of DRAO Global Magneto-Ionic Medium Survey (GMIMS) polarisation data set. This polarisation data set is now public through the data release described by Wolleben et al. (2021). The Faraday depth resolution of the used DRAO GMIMS moments is 140 rad m^{-2} (Dickey et al. 2019). Structures at the scale of $\sim 1 \text{ rad m}^{-2}$ that

are seen in LoTSS data are resolved out in the DRAO data. On the other hand, some of the Faraday thick structures for LOFAR at these frequencies become Faraday thin and observable. Comparing the two data sets allows us to obtain a deeper understanding of the Faraday thickness of the observed structures and the effect of depolarisation on the observed volume of the ISM, both of which are frequency dependent.

Additionally, we compared our results with the Galactic Faraday Sky map (Hutschenreuter & Enßlin 2020; Hutschenreuter et al. 2022), representing the total RM produced by the Galaxy. As such, this map complements both LOFAR and DRAO GMIMS first moment images in the analysis. The Galactic Faraday Sky was reconstructed using extragalactic sources including, amongst others, the catalogue of polarised sources from the LoTSS survey (O’Sullivan et al. in prep.). We used the publicly available version of the map⁷, with a resolution of 8.6 arcmin (Hutschenreuter et al. 2022).

In order to compare different data sets, we smoothed all data to the resolution of 40 arcmin, matching the resolution of DRAO GMIMS moment images. While smoothing, we used the mask from Section 4. The smoothing was done in Q and U mosaic cubes, after which the moments with the new resolution were calculated. To compare other data sets with DRAO GMIMS data, we excluded additional regions, which were originally masked in DRAO GMIMS moment images (see bottom panel of Fig. 13).

5.1. Visual comparison

We performed a visual comparison of the LoTSS and DRAO GMIMS moment images and the Galactic Faraday Sky map. All the images in this subsection are shown in Galactic coordinates to emphasise Loop III.

Visually comparing LoTSS and DRAO GMIMS zeroth moment images, we find some indications of emission in DRAO GMIMS data that could be connected to Loop III in the areas marked with black circles in Fig. 12. In the circled area on the left of the DRAO GMIMS image (Fig. 12, bottom panel), we see structures that seem to follow the shape of the loop, while the same area in the LoTSS zeroth moment image has an intensity two times lower than the loop average intensity. Both DRAO GMIMS and LoTSS first moment values in this area are negative and have comparable values (Fig. 13). This result suggests that Loop III is also visible in the DRAO GMIMS data. The reason for the differences in what we see in the two frequency regimes may lie either in different Faraday thicknesses of observed structures or frequency-dependent depolarisation effects. If the structure we are seeing is Faraday thin in both regimes, it could have a lower intensity at low frequencies due to a stronger effect of depolarisation. We discuss this in more detail in the following subsection.

In the circled area on the right (Fig. 12), we observe some emission in the DRAO GMIMS zeroth moment. This area again shows lower-than-average intensity in the LoTSS zeroth moment image; however, the morphology does not coincide with the morphology seen in the DRAO GMIMS image. Furthermore, we do not see any visual correspondence between the first moment images of DRAO GMIMS and LoTSS in the area of the circle on the right shown in Fig. 13. DRAO GMIMS values are mostly positive, LoTSS values are mostly negative, and the morphology of detected structures is different. We conclude that the loop is not detected in this part of the DRAO GMIMS image.

⁷ <https://wwwmpa.mpa-garching.mpg.de/~enssln/research/data/faraday2020.html>

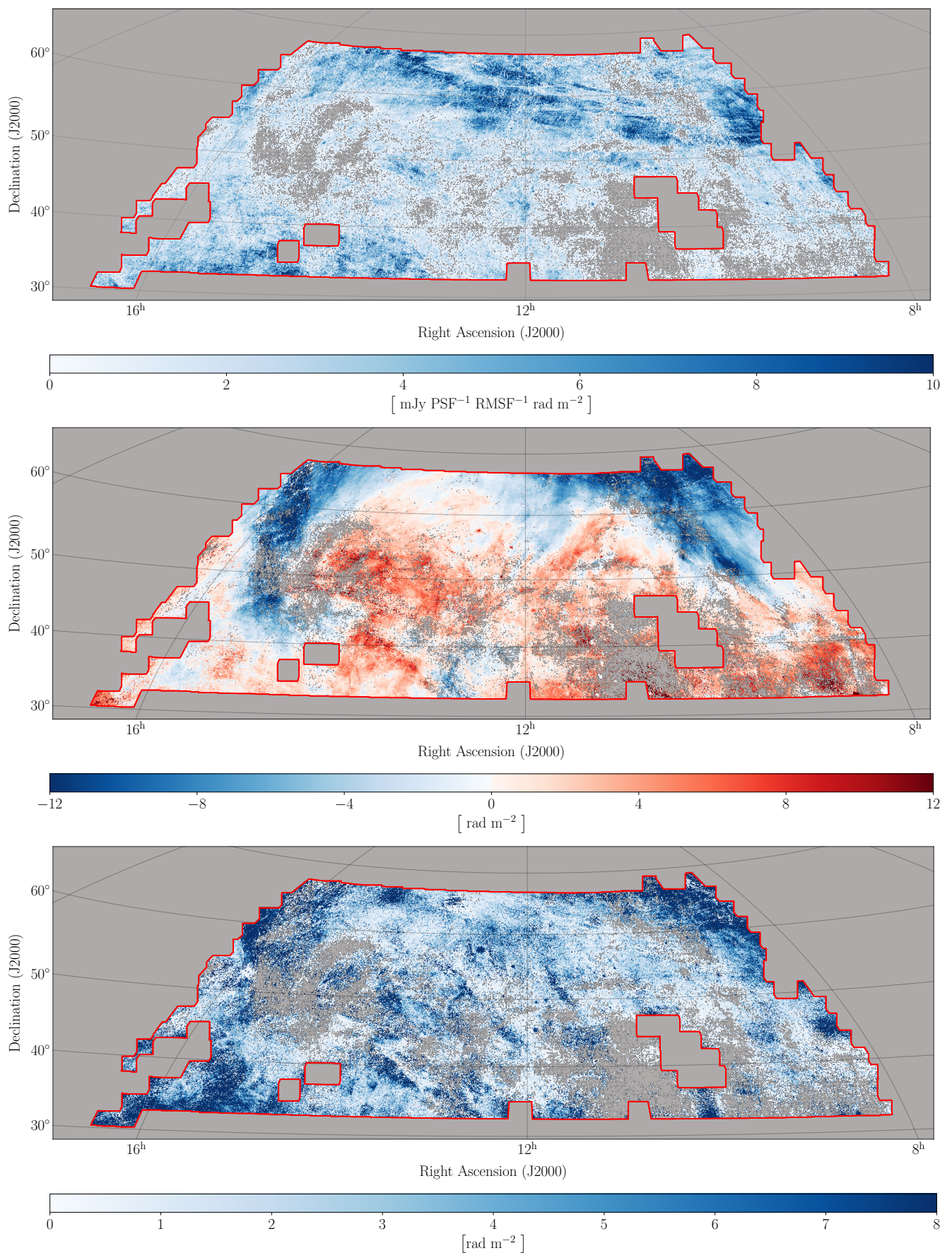


Fig. 11. Moments of the Faraday cubes. The top panel shows the zeroth moment image representing the total polarised intensity. The middle panel shows the first moment image representing the intensity weighted mean Faraday depth value. The bottom panel shows the square root of the second moment image representing the spread of spectra around first moment values. All images are in equatorial coordinates. The red line outlines mask edges.

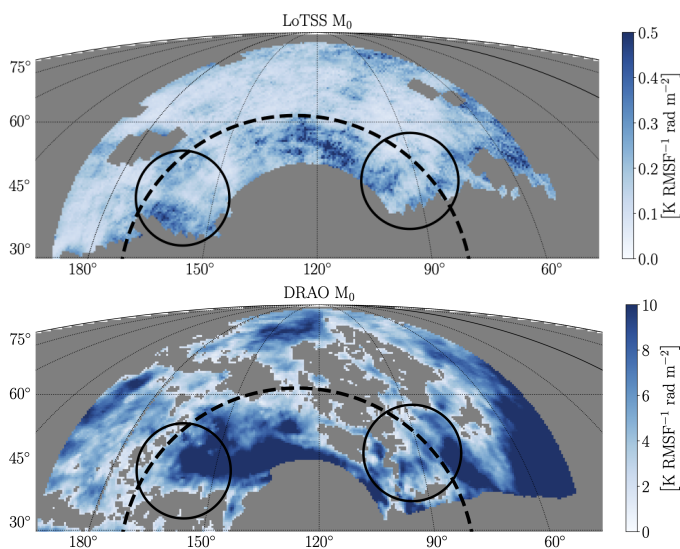


Fig. 12. LoTSS and DRAO GMIMS zeroth moment images in Galactic coordinates with the same projection as in Fig. 8 and they have a resolution of 40 arcmin. Circles mark areas discussed in Section 5.1. The units for the LoTSS zeroth moment were converted to $\text{K RMSF}^{-1} \text{ rad m}^{-2}$ to simplify the comparison with DRAO GMIMS data. The intensity of $1 \text{ mJy PSF}^{-1} \text{ RMSF}^{-1} \text{ rad m}^{-2}$ corresponds to $\sim 0.5 \text{ K RMSF}^{-1} \text{ rad m}^{-2}$.

There are several possibilities that could explain why the structure detected in DRAO GMIMS is not seen in LoTSS. The structure detected in the DRAO GMIMS images could be further away and depolarised in the LoTSS data. Alternatively, it could be a structure with low brightness and one that is Faraday thick for LoTSS, which would contribute to the LoTSS first moment values negligibly because of the intensity weighting.

As shown in the middle panel of Fig. 13, the map of the Galactic Faraday Sky has negative values of RM in the circled area on the left. The feature has a shape similar to the structure of Loop III seen in the LoTSS first moment image (upper panel of Fig. 13). However, the circle on the right contains an interesting shape stretching over the north-western area of the loop. This shape is roughly centred at Galactic coordinates $l = 117^\circ$, $b = 50^\circ$ and it has high positive RM values, with a mean around $+25 \text{ rad m}^{-2}$. The same structure was also present in the first Faraday Sky map by Oppermann et al. (2012), where it was associated with an intermediate-velocity arch of HI spectroscopic data. This area in the DRAO GMIMS first moment image has a very low S/N due to depolarisation. In LoTSS, this structure is also not present, which is probably also due to depolarisation.

5.2. Statistical comparison

To make a quantitative comparison between different data sets, we represent the data in the form of 2D histograms and calculate the Pearson correlation coefficient. In Fig. 14 we show a 2D histogram of DRAO GMIMS versus LoTSS first moment images in the left panel, DRAO GMIMS versus Galactic Faraday Sky map in the middle panel, and the Galactic Faraday Sky map versus LoTSS in the right panel. The strongest correlation is found between LoTSS and the Galactic Faraday Sky, with a correlation coefficient of $R = 0.39$. In the other two cases, we did not find a significant correlation between the compared data sets.

The lack of correlation between DRAO GMIMS and LoTSS first moment images ($R = 0.20$) can be understood as a result of frequency-dependent Faraday depth resolution and depolarisation.

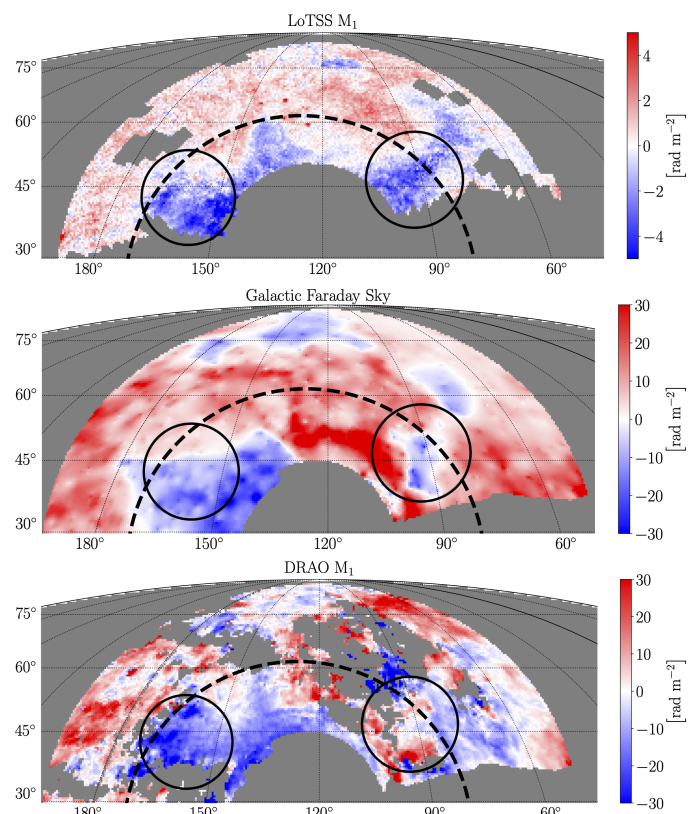


Fig. 13. First moment images of LoTSS, Galactic Faraday Sky, and DRAO GMIMS are shown in the upper, middle, and lower panels, respectively. The dashed line illustrates the boundary between the lower and upper regions of the shown maps. All images are in Galactic coordinates with the same projection as in Fig. 8, and they have resolution of 40 arcmin. Circled areas are the same as in Fig. 12.

Faraday depth resolution at LOFAR frequencies is two orders of magnitude higher than at DRAO GMIMS frequencies. This makes low-frequency data sensitive to many Faraday thin structures that are not resolved by the RMSF function at higher frequencies due to poor resolution. In addition, depolarisation associated with Faraday rotation is stronger at low frequencies than at high frequencies. Therefore, we are most likely not probing the same volume of the Galaxy in the LoTSS and DRAO GMIMS surveys. Differences between the two data sets may also arise from the different angular scales to which the two telescopes are sensitive. DRAO GMIMS data have poorer angular resolution, which can result in stronger beam depolarisation. On the other hand, DRAO GMIMS data were observed using a single dish telescope that can detect larger scales to which LOFAR is not sensitive.

In the case of DRAO GMIMS and Galactic Faraday Sky, one would expect to see a correlation, as indicated by the results of Dickey et al. (2019) and Ordog et al. (2019). As mentioned before, depolarisation is not expected to be significant at high frequencies. The volume probed should be more similar to the total volume probed by extragalactic sources. However, in this specific region of the sky, the dominating structure (Loop III) is considered to be fairly nearby and it is only partially visible in the DRAO GMIMS data. This is likely due to confusion with other Faraday structures present in the spectra and poor Faraday resolution at higher frequencies and/or beam depolarisation. This could explain the lack of correlation in this specific region ($R = 0.22$).

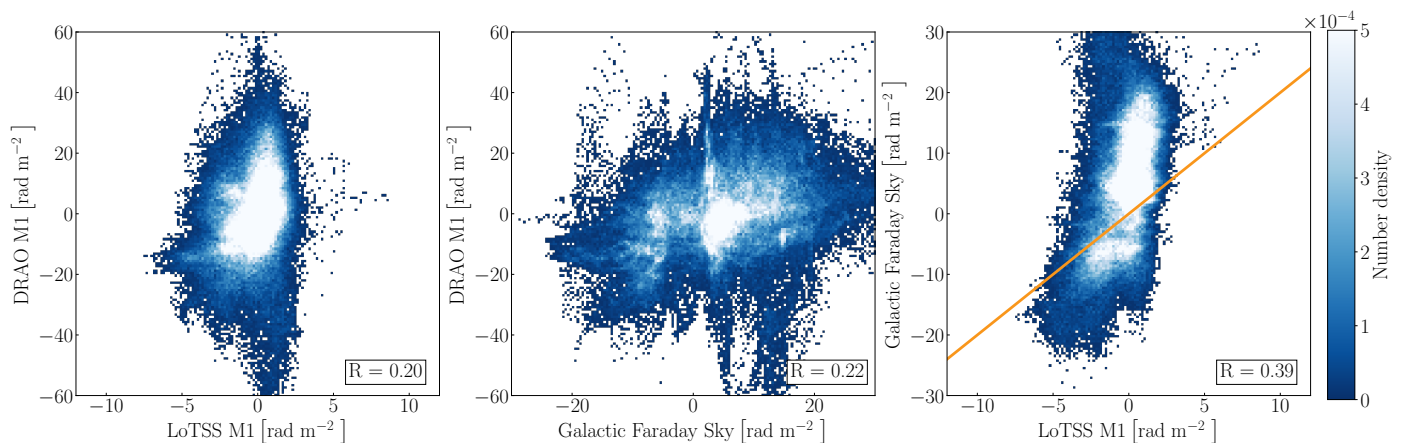


Fig. 14. 2D histograms of DRAO first moment versus LoTSS first moment (left), DRAO GMIMS first moment versus Galactic Faraday Sky values (middle), and Galactic Faraday Sky values versus LoTSS first moment (right). Light blue bins indicate a high number density. The Pearson correlation coefficient, R , is given at the bottom right of each panel. The histograms were made with data at a resolution of 40 arcmin. In the making of all of the histograms, the same area was used.

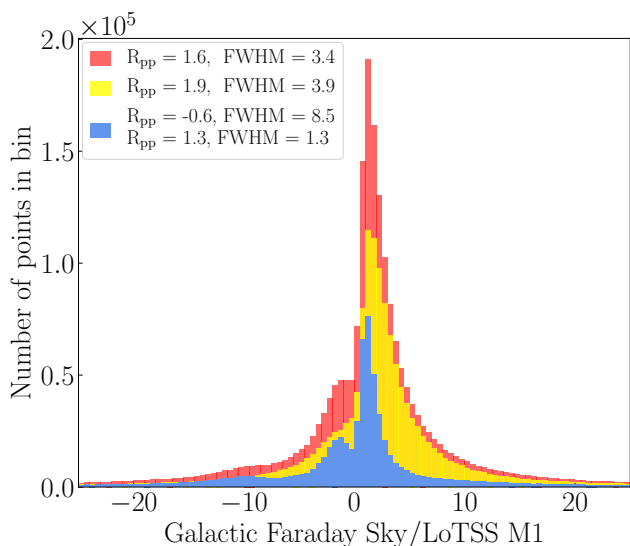


Fig. 15. Histogram of the Galactic Faraday Sky to LoTSS first moment ratio in different regions. Blue and yellow histograms display the lower and the upper region, respectively. The red histogram displays both regions combined. We used a Lorentzian fit to characterise the histograms; the obtained ratio peak positions (R_{pp}) and FWHMs are given in the legend above the plot.

We note that when smoothing to 40 arcmin, we lost a considerable amount of LoTSS data. To test if the correlation between LoTSS M1 and the Galactic Faraday Sky persists at a LoTSS native resolution, we oversampled the Galactic Faraday Sky and repeated the analysis. We obtained a Pearson correlation coefficient of 0.43, which shows that smoothing the data does not change the correlation significantly. Nevertheless, we continued to investigate this correlation at a LoTSS native resolution.

To quantify this correlation, we plotted a histogram of the ratio between the Galactic Faraday Sky and the LoTSS first moment (see Fig. 15). The peak of the distribution, R_{pp} , represents the average ratio found in the analysed part of the sky and is found to be at 1.6, while the FWHM represents the spread of the distribution, and it is 3.4. Although the spread is rather large, this value is similar to the value of 2, expected for the ‘Burn

slab model’ (Burn 1966). This model assumes a uniform magnetic field and electron density throughout the slab, where each layer of the slab is emitting and Faraday rotating synchrotron emission. As a result of depth depolarisation, the expected Faraday depth values are half that of the total RM through the slab. The observed discrepancy suggests more complex physical conditions than assumed in this simple model.

We separated the mosaic in two parts to examine the ratios in two distinct regions. The lower region mostly contains the polarised emission associated to Loop III and the upper region contains the polarised emission at higher Galactic latitudes, above the loop. The boundary between the two regions is illustrated with a dashed line in Fig. 13. The histograms of the Galactic Faraday Sky to the LoTSS first moment ratio for the lower and upper region are given in Fig. 15. The ratio distribution in the lower region shows two peaks, a higher one with a positive value and a lower one with a negative value corresponding to areas where the compared data have opposite signs. The positive and the negative peaks can be described by two Lorentzians centred at 1.3 and -0.6, respectively, with FWHMs of 1.3 and 8.5, respectively. The negative peak comes from the areas that do not correlate – the Faraday depths of structures seen there have opposite signs. In the upper region, we found a peak at 1.9, with a FWHM of 3.9.

5.3. Insights from simple toy models

To understand the ratios in different regions, we ran synthetic observations of LOFAR data with a few simple toy models (variations of the Burn model) of different physical scenarios. In the models, we assumed that the Faraday rotation is present along the full LOS and that the magnetic field and electron density are uniform. Models are distinguished by the location and thickness of the emitting regions (for details see Appendix C.). Similar toy models were considered by Ordog et al. (2019). An important difference between our simple toy models and LoTSS data is that the models represent a single LOS, while LoTSS data come from multiple lines of sight that could be probing very different ISM configurations which correspond to different models (i.e. the double peaked distribution of Fig. 15).

The first toy model (Model A) is a Burn slab with emission and rotation along the full LOS, which is the same as that in Burn (1966). In this limit, we obtained a ratio of 2 between the

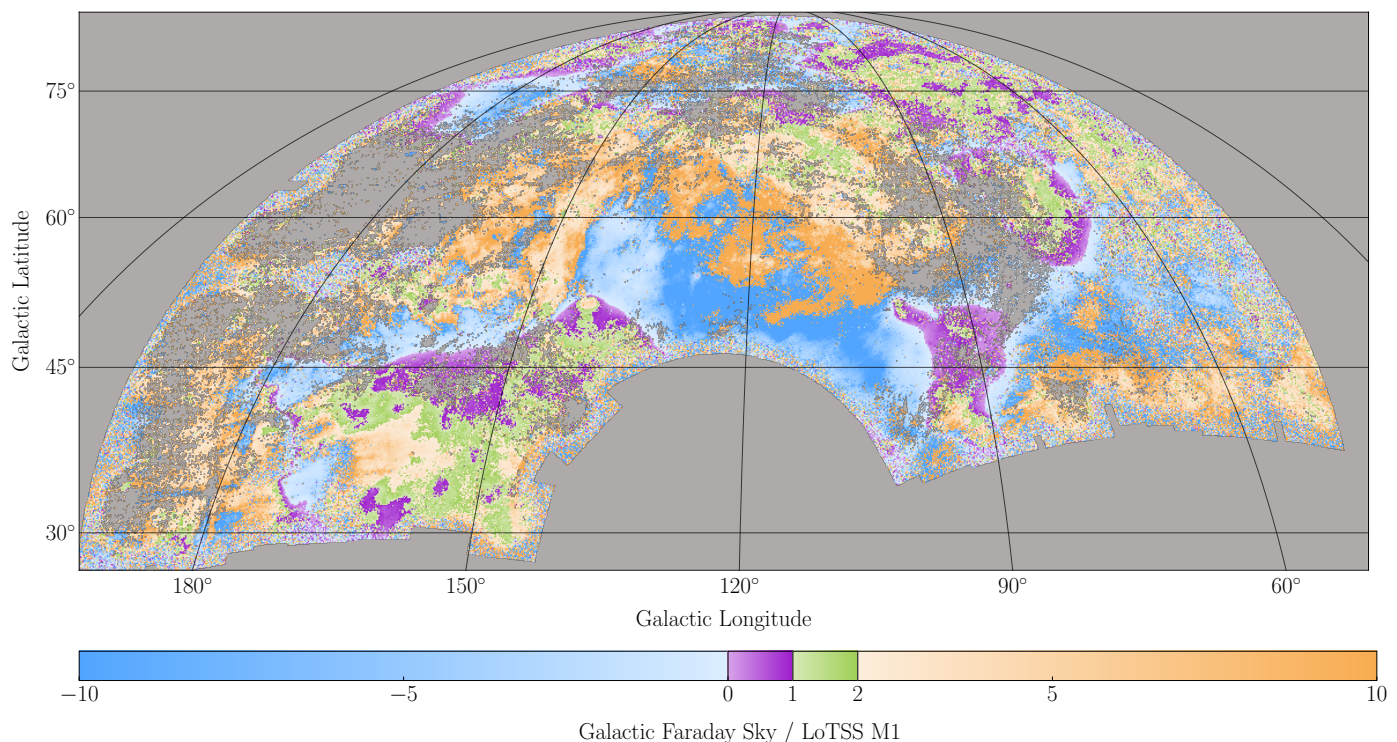


Fig. 16. Map of the Galactic Faraday Sky to LoTSS first moment ratio. The blue colour marks the area where the two data sets trace different structures. Purple marks ratios lower than 1, green represents ratios in range from 1 to 2, and orange marks ratios higher than 2.

modelled total Galactic RM, as it would be probed by extragalactic sources, and the observed polarised emission. In the second model (Model B), we distributed one or more synchrotron emitting layers along the LOS with the Faraday rotating medium in between, acting as Faraday screens – in this case, there is no differential Faraday rotation. We further expanded this model into three cases regarding the location of the emitting layers. In Model B.0, we considered a single emitting layer followed by a rotating volume acting as a single screen. The first moment value is then the same as the total RM value, and the ratio is equal to 1. In Model B.1, multiple emitting layers are distributed along the full LOS and we got ratios between 1 and 2. In Model B.2, the emitting layers are distributed in the closer half of the LOS, and the ratios obtained are higher than 2. In the third model (Model C), we attenuated the emission in the Burn slab with increasing distance from the observer. In this case, the ratio obtained exceeds the value of 2 and grows higher with a decreasing amount of the LOS being affected by differential Faraday rotation.

These toy models help us to develop an intuition on the variation of the Galactic Faraday Sky to LoTSS first moment ratios seen in the data. The positive ratios obtained for the full mosaic area and its lower and upper parts could correspond to model B.1. However, in the context of a large distribution spread, the results could correspond to any of the toy models presented here, or a combination of them.

Since averaging over large areas of the data, with more than one distinct feature, may be too crude, we present a map of the Galactic Faraday Sky to LoTSS M_1 ratios in Fig. 16. From this map, we can understand the presence of a negative peak found in the lower region of the mosaic as a signature of the intermediate velocity cloud seen at high positive latitudes only in the Galactic Faraday Sky map. Negative ratios (blue in Fig. 16) can also be attributed to a flip in the magnetic field direction along the LOS – the local magnetic field can have a sign opposite from the av-

erage along the full Galaxy. The flip in magnetic field direction can also produce ratios from 0 to 1 (purple in Fig. 16), magnetic fields along the full LOS can average out to low values, while the nearby magnetic field is stronger. Ratios from 1 to 2 are marked in green and indicate our model B.1. Orange areas of the map show positive ratios, higher than 2. Along the LOS where the ratios are much higher than 2, there is much more depolarisation than is predicted by the Burn slab model.

Our toy models suggest that these ratios could carry information about the relative distribution of synchrotron emitting and Faraday rotating regions along the sight line. Actual observations, however, may be the composite result of multiple scenarios at play which reflect the complexity of the Faraday sky. Further analysis, which is beyond the scope of this first paper, will be done in order to reach an in-depth understanding of the different regions under study.

6. Summary and conclusions

In this paper, we have produced a mosaic Faraday cube combining 440 observations from the LOFAR Two-metre Sky Survey DR2. The mosaic covers around 3100 square degrees in the high-latitude outer Galaxy, which makes it the biggest low-frequency polarisation mosaic in the northern sky to date. The mosaic has an angular resolution of 4.3 arcmin and a Faraday depth resolution of $\sim 1 \text{ rad m}^{-2}$.

The mosaic revealed the richness of diffuse polarised emission morphology. Depolarisation canals of different lengths, widths, and orientations fill the area of the mosaic. Lower Galactic latitudes are dominated by large angular scale (tens of degrees) polarised emission associated with Loop III, while higher Galactic latitudes show patchy and more diffuse polarised emission, organised in features on smaller angular scales of 1 degree.

The big gradient in Faraday depth spreads over 30 rad m^{-2} in the direction outward from the centre of Loop III, covering tens of degrees. This gradient is probably associated with a shock front that could have been formed by one or more supernova explosions in the Galactic disk (Berkhuijsen 1971; Kun 2007).

We have further analysed polarised emission by using zeroth, first, and second Faraday moment images and we compared them to moments produced from the DRAO GMIMS data set at 1.4 GHz (Dickey et al. 2019) and to the Galactic Faraday Sky map (Hutschenreuter et al. 2022). We see some morphological similarities between zeroth moment DRAO GMIMS and LoTSS images in the region of Loop III. In other areas, we see no such correlation, which can be explained by a different Faraday depth resolution and a different maximum Faraday scale to which each survey is sensitive.

We have found a correlation between the LoTSS first Faraday moment image and the Galactic Faraday Sky. We have studied this correlation by inspecting histograms of the ratio of the two data sets and by testing several toy models in an effort to explain the obtained ratios. The area dominated by the loop shows high complexity and cannot be properly described by the simple models we present. Areas not dominated by Loop III emission indicate depolarisation of emission coming from great distances.

From the map of ratios (Fig. 16), we can conclude that in the low frequency data, not many lines of sight can be described by the Burn slab model, although this does not seem to apply to higher frequency data (Ordog et al. 2019). A high sensitivity and strong effect of Faraday rotation at low frequencies result in highly complex Faraday structures along different LOSs. Additionally, this map reveals areas that have negative ratios and do not correlate, meaning that the compared data sets are probing different structures (e.g. the aforementioned region in the Galactic Faraday Sky map associated to an intermediate-velocity arch of atomic hydrogen gas). Alternatively, since the two data sets do not probe the same volume, negative ratios and positive ratios lower than 1 can be caused by a magnetic field reversal along the LOS in these specific areas.

This paper only scratches the surface of understanding the observed diffuse polarised emission morphology in the LoTSS data and the complexity of the Faraday spectra. To understand the underlying processes in the ISM, multi-tracer analysis is needed. While such analyses of Faraday tomographic data at low-radio frequencies in smaller areas of the sky have already found connections between different phases of the ISM and the magnetic field (Zaroubi et al. 2015; Lenc et al. 2016; Van Eck et al. 2017; Jelić et al. 2018; Bracco et al. 2020; Turić et al. 2021), the next step to be taken is testing these findings over larger sky areas. A multi-frequency analysis of the LoTSS data set will be presented in a follow-up paper.

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Appendix A: Zoom-ins

In this section we present the selected zoom-ins on the mosaic in Galactic coordinates.

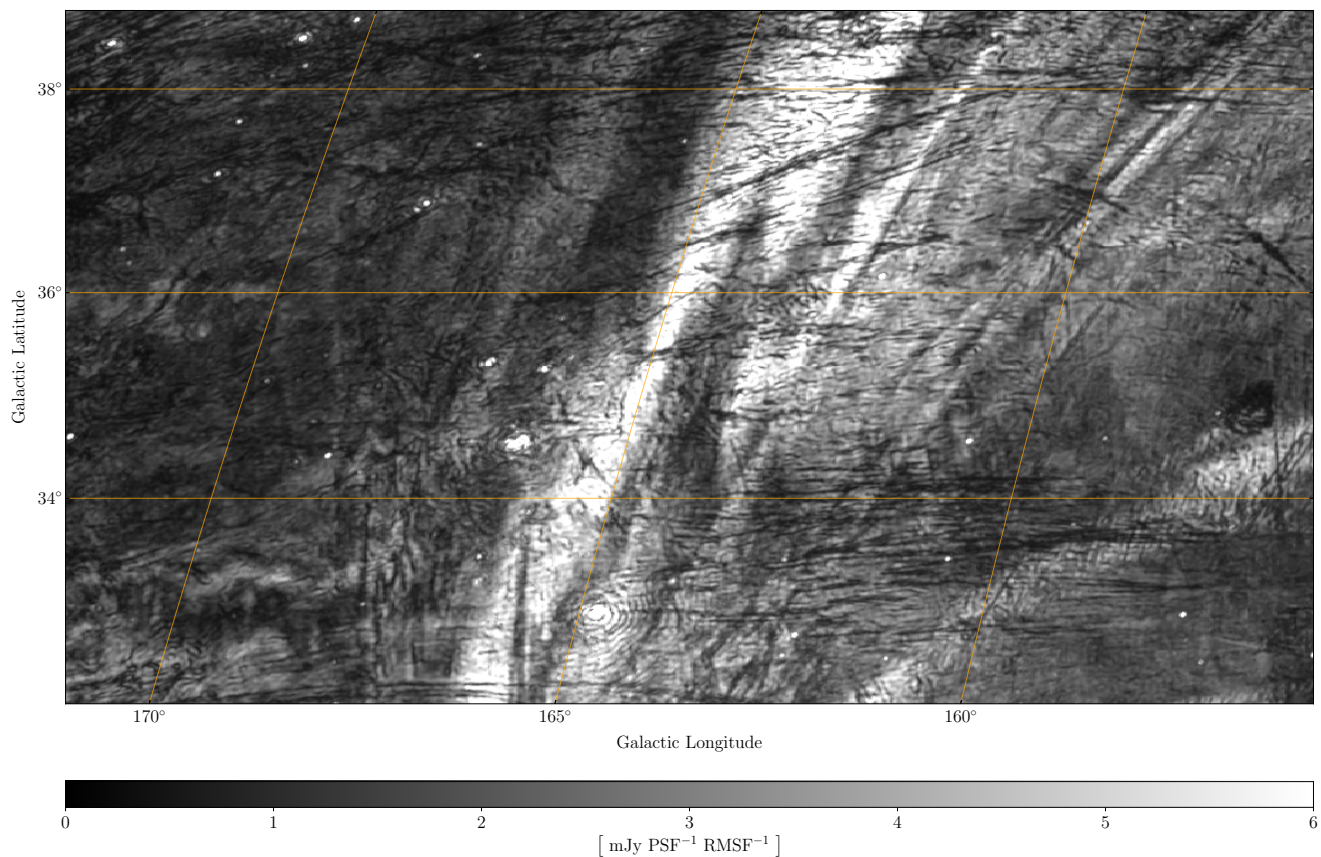


Fig. A.1. Zoom 1. Magnified maximum polarised intensity image, covering 3% of total mosaic area. This image zooms in on depolarisation canals following Loop III, as well as the ones perpendicular to the loop.

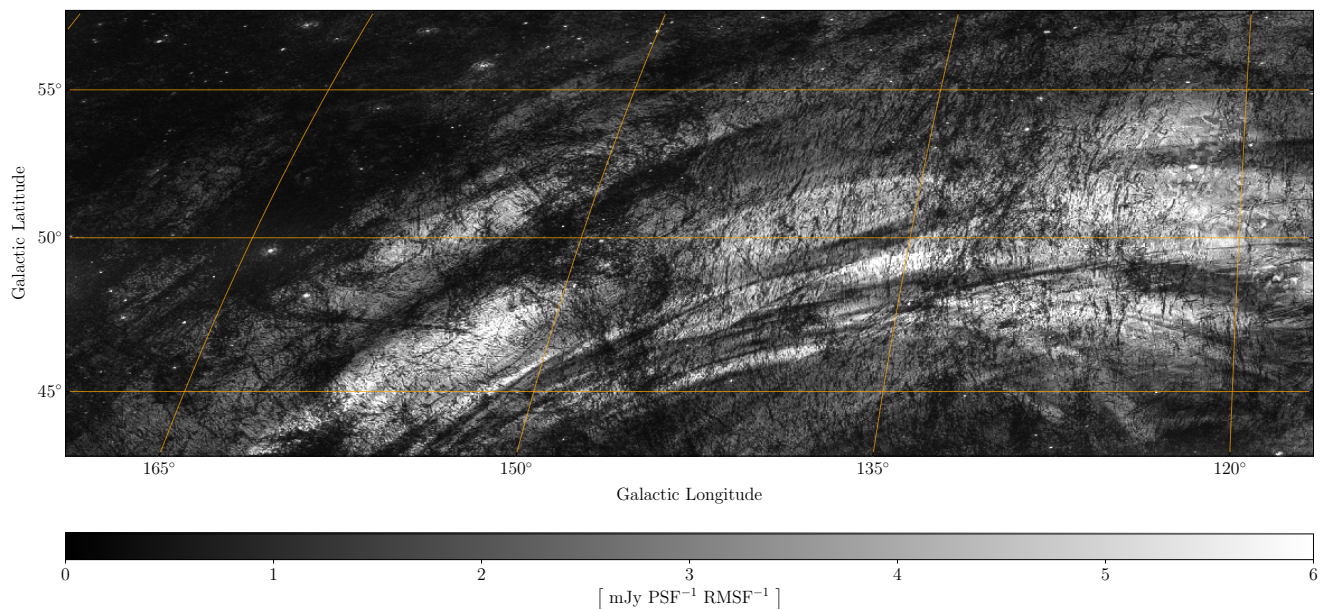


Fig. A.2. Zoom 2. Magnified maximum polarised intensity image, covering 17% of total mosaic area. This image shows depolarisation canals stretching along Loop III.

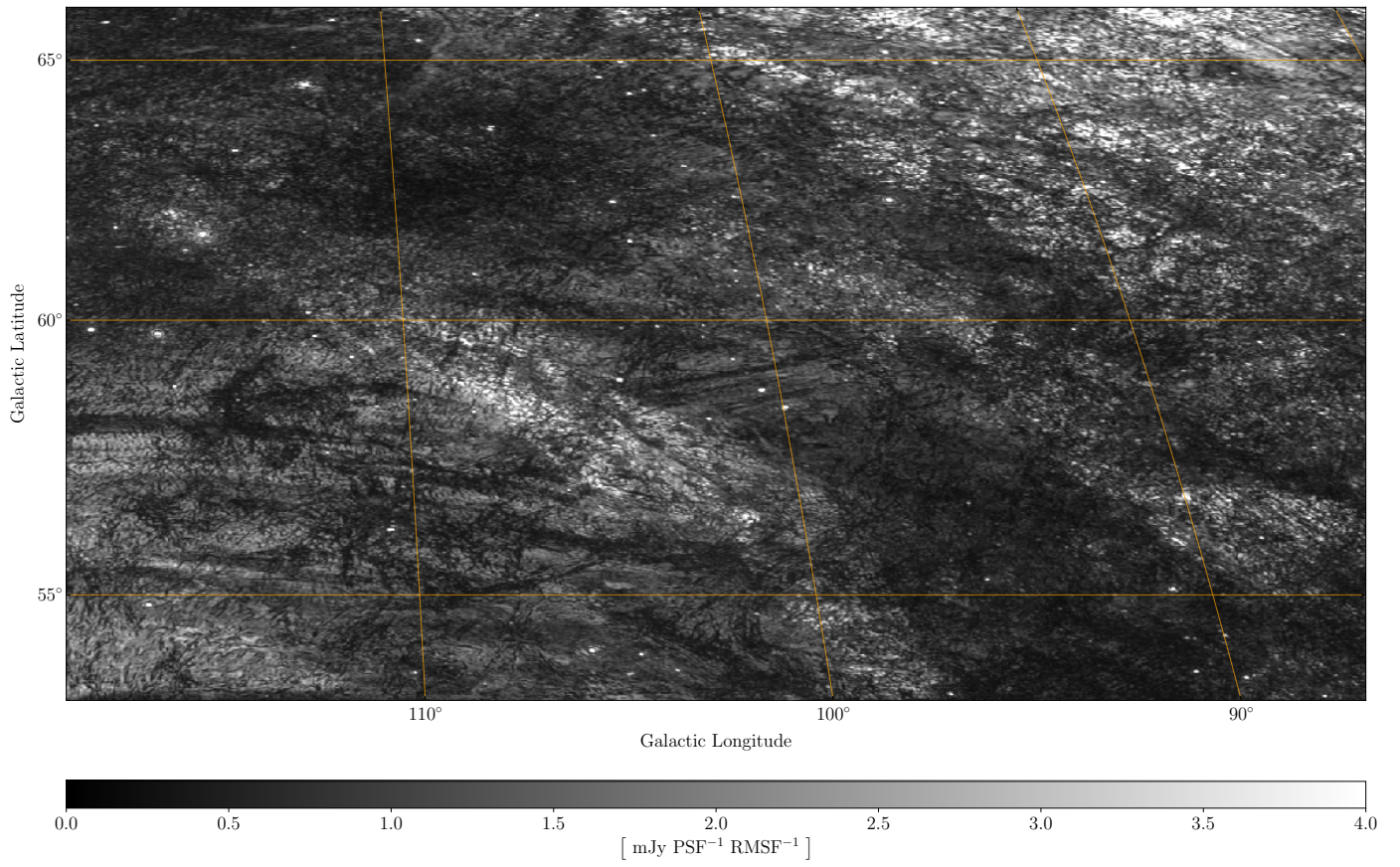


Fig. A.3. Zoom 3. Magnified maximum polarised intensity image, covering 7% of total mosaic area. The image shows the emission coming from the zig-zag structure mixed with Loop III emission (coming from the bottom left corner).

Appendix B: Mosaic at chosen Faraday depths

In this appendix, we present the selected slices from the mosaic Faraday cube. We show only the images at Faraday depths from -25 rad m^{-2} to $+15 \text{ rad m}^{-2}$, since there is almost no emission outside of this range. Figures B.1 and B.2 mainly show the Loop III emission. The zig-zag structure discussed in Sect. 3.2 can best be seen in images at 5 and 10 rad m^{-2} in Fig. B.3.

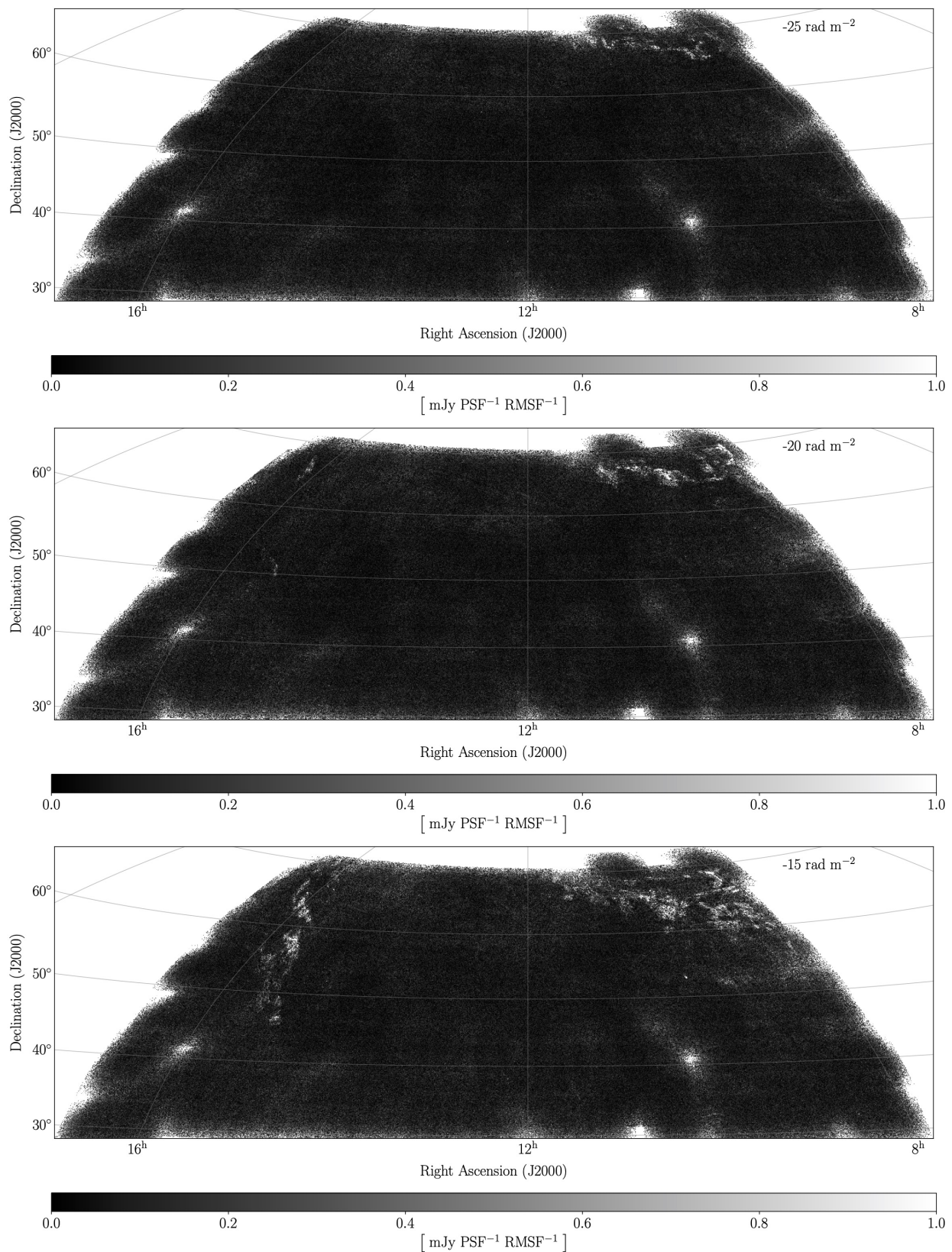


Fig. B.1. Slices from the mosaic Faraday cube at Faraday depths -25 , -20 , -15 rad m^{-2} . The images are dominated by Loop III emission.

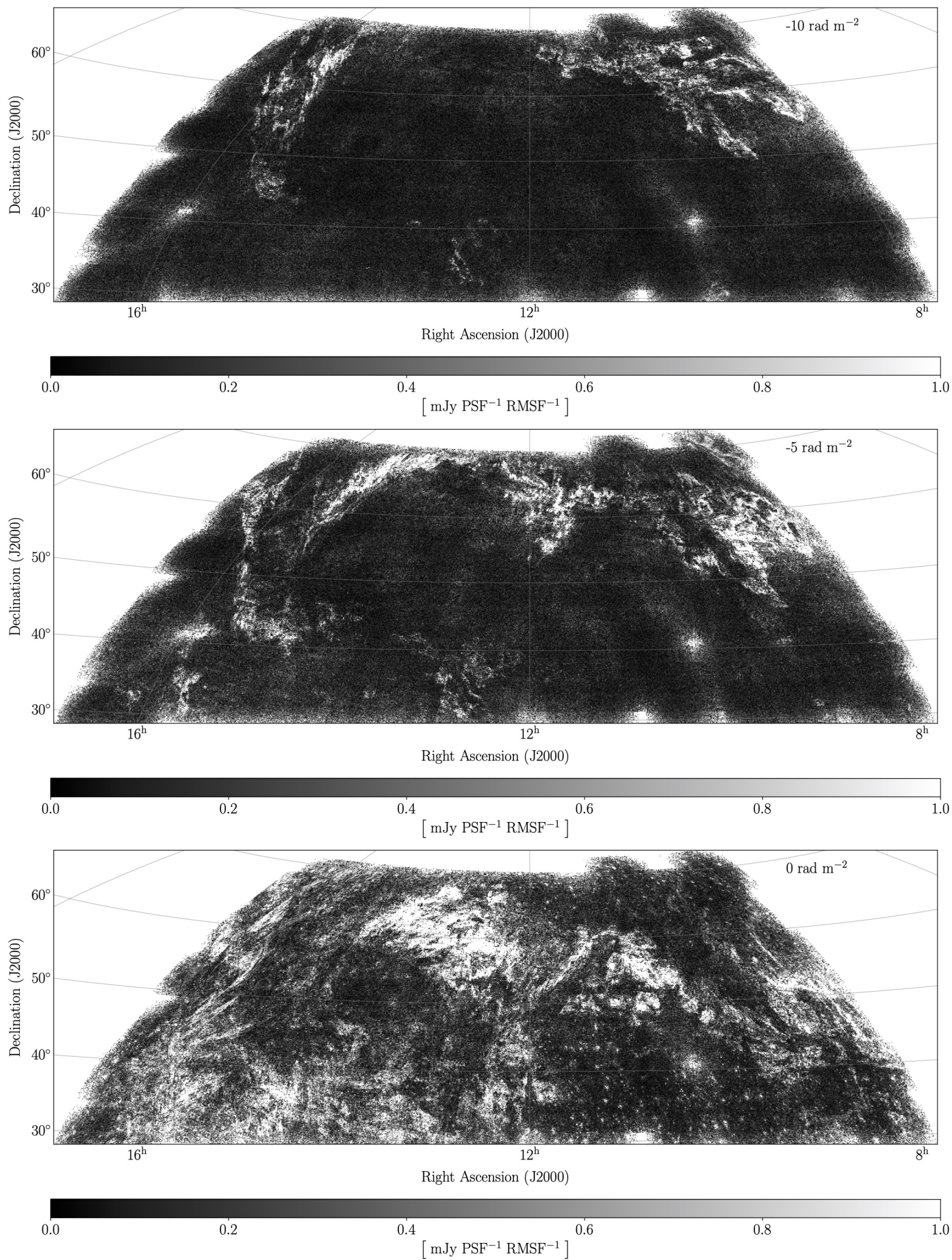


Fig. B.2. Slices from the mosaic Faraday cube at Faraday depths -10 , -5 , 0 rad m^{-2} . The images are dominated by Loop III emission.

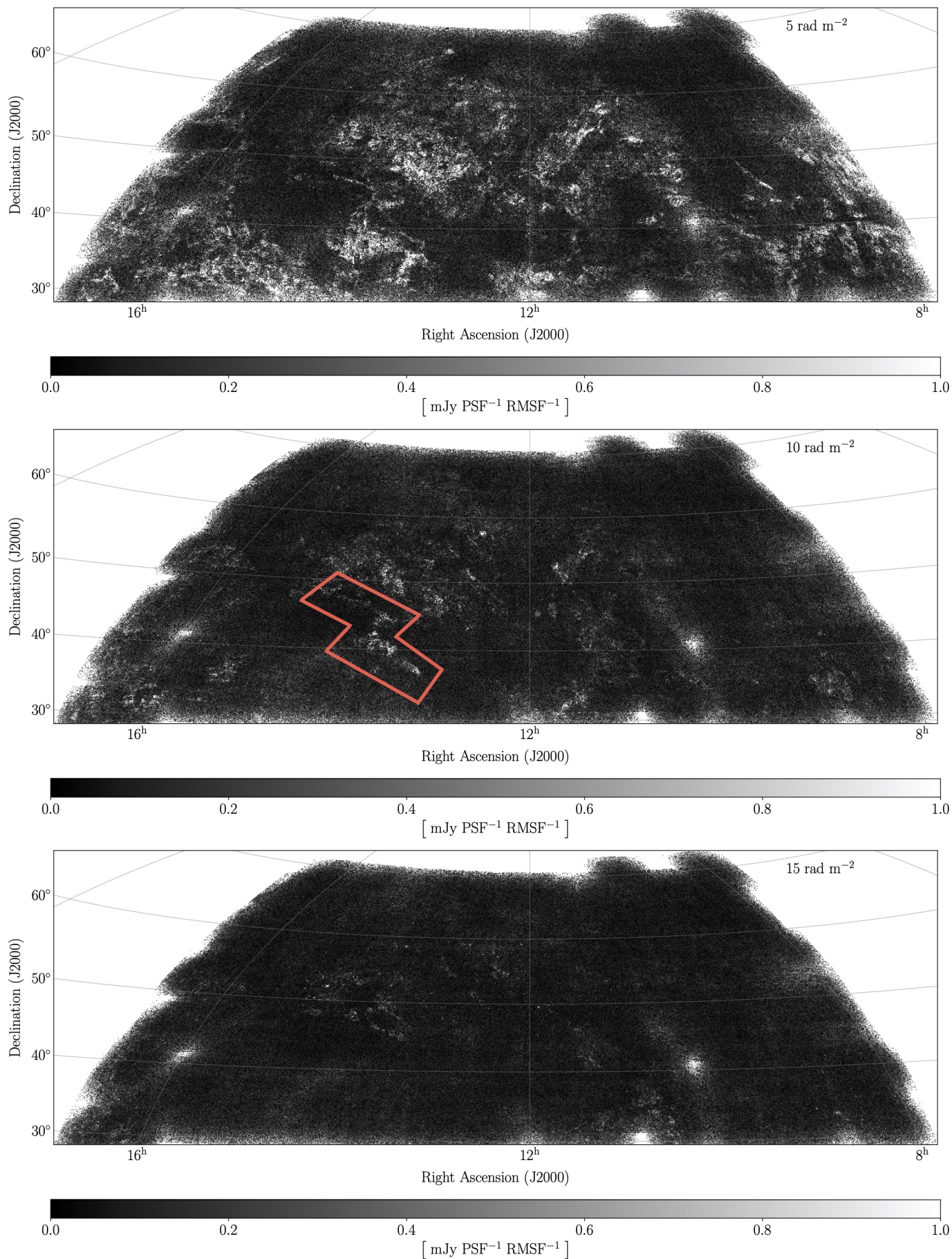


Fig. B.3. Slices from the mosaic Faraday cube at Faraday depths 5, 10, 15 rad m^{-2} . Loop III emission in traces is seen at 5 rad m^{-2} . While a part of the zig-zag structure can be seen in all of the panels, the area in which the zig-zag structure is best seen (at 10 rad m^{-2}) is roughly outlined in red. At Faraday depths higher than 15 rad m^{-2} , we see no emission.

Appendix C: Toy models probing the multi-frequency comparison

In this appendix, we describe the toy models used to interpret the correlations found in Sect. 5 between data sets at different frequencies. In particular, we focus on the correlation between our LOFAR data and the total Galactic RM. For a given LOS, we consider three distinct cases, as shown by the sketches in Fig. C.1.

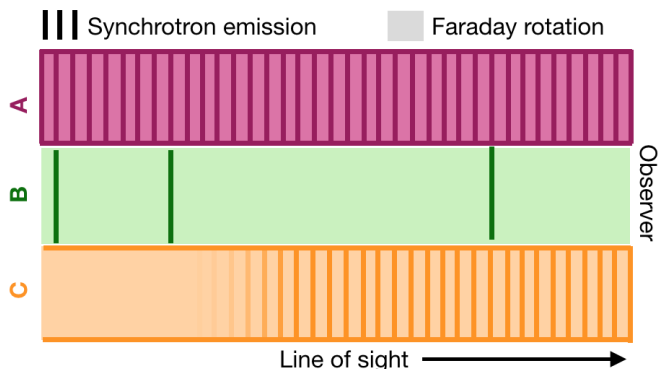


Fig. C.1. Sketches showing the three models (case A, B, and C) considered in our analysis to interpret the multi-frequency correlations discussed in Sect. 5.

Case A is a Burn slab in which the full length of the LOS is affected by differential Faraday rotation as the result of a mixture of uniform synchrotron-emitting and Faraday-rotating media. We assumed that we observe along the mean magnetic field component, such that the equivalent value of the modelled Galactic RM (MGRM) is 20 rad m^{-2} . This value of MGRM is arbitrary, but large enough to certainly be a Faraday thick structure at the observed frequencies of LOFAR. The cosmic-ray electron density, the magnetic-field structure and strength, and the free-electron density are all homogeneous and uniform quantities along the LOS.

Case B has the same MGRM as case A, but a different distribution of emission along the LOS. In this case we considered the synchrotron emission to be confined to one layer, or several distinct layers, so that emission and Faraday rotation are two separated processes. Each Faraday rotating medium between two different synchrotron emitting layers represents a Faraday screen. In this case we distinguish between three configurations. In the first one, B.0, one single emitting layer is affected by the full length of the Faraday rotating medium, or one single Faraday screen. In B.1, one or multiple discrete emitting layers are distributed across the full length of the Faraday rotating medium. In B.2, one or multiple discrete emitting layers are only distributed in the first half of the Faraday rotating medium towards the observer.

Finally, case C is a modified version of case A in which the synchrotron emission is attenuated as a function of the distance from the observer. The MGRM in case C is the same as in the other two cases.

In all three cases, we simulated LOFAR polarisation observations in the same range of frequencies as the one described in this paper and we performed Faraday tomography using `rm-synthesis`⁸ (Brentjens & de Bruyn 2005). Thus, we produced Faraday spectra similar to those in Fig. C.2, where cases A

and C show two different configurations of Faraday thick structures of which we can only observe the edges (e.g. Van Eck et al. 2017), and all the B cases show the position in Faraday space of each synchrotron emitting layer. From such spectra, we computed the first moments (M_1) and compared them to the value of MGRM.

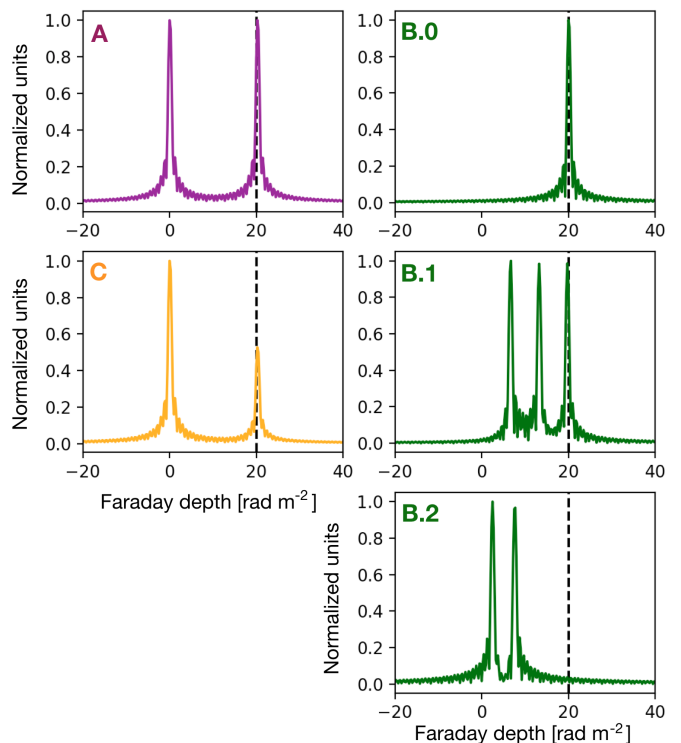


Fig. C.2. Modelled Faraday spectra of the three cases A, B, and C discussed in the main text. The vertical dashed line represents the value of MGRM = 20 rad m^{-2} .

Figure C.3 illustrates the ratios between MGRM and M_1 for each model. Only in case B.0 is $\text{MGRM}/M_1 = 1$, while $\text{MGRM}/M_1 = 2$ was obtained, as expected, in case A, where uniform differential Faraday rotation was modelled. The B.1 configuration produced values of MGRM/M_1 between 1 and 2, while both cases B.2 and C returned values of $\text{MGRM}/M_1 > 2$. Departures from the value of 2 are generally related to cases in which the Faraday rotating medium significantly extends over a longer portion of the LOS compared to the synchrotron emitting regions.

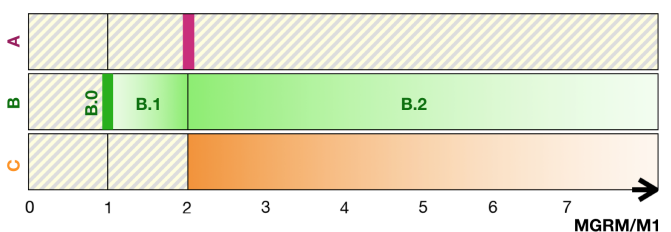


Fig. C.3. Diagram showing the ratio between the modelled Galactic RM and the value of the first moment for the simulated Faraday-tomographic data in the three cases (A, B, and C) described in the main text. Grey-shaded areas represent forbidden regions for each model.

⁸ <http://github.com/brentjens/rm-synthesis>