# Astrometric and photometric initial mass functions from the UKIDSS Galactic Clusters Survey - II. The Alpha Persei open cluster* 

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#### Abstract

We present the results of a deep ( $J=19.1 \mathrm{mag}$ ) infrared $(Z Y J H K)$ survey over the full $\alpha$ Per open cluster extracted from the Data Release 9 of the United Kingdom Infrared Telescope Infrared Deep Sky Survey Galactic Clusters Survey (UKIDSS). We have selected $\sim 700$ cluster member candidates in $\sim 56$ square degrees in $\alpha$ Per by combining photometry in five nearinfrared passbands and proper motions derived from the multiple epochs provided by the UKIDSS Galactic Clusters Survey (GCS) Data Release 9 (DR9). We also provide revised membership for all previously published $\alpha$ Per low-mass stars and brown dwarfs recovered in GCS based on the new photometry and astrometry provided by DR9. We find no evidence of $K$-band variability in members of $\alpha$ Per with dispersion less than $0.06-0.09 \mathrm{mag}$. We employed two independent but complementary methods to derive the cluster luminosity and mass functions: a probabilistic analysis and a more standard approach consisting of stricter astrometric and photometric cuts. We find that the resulting luminosity and mass functions obtained from both methods are consistent. We find that the shape of the $\alpha$ Per mass function is similar to that of the Pleiades although the characteristic mass may be higher after including higher mass data from earlier studies (the dispersion is comparable). We conclude that the mass functions of $\alpha$ Per, the Pleiades and Praesepe are best reproduced by a log-normal representation similar to the system field mass function although with some variation in the characteristic mass and dispersion values.


Key words: Techniques: photometric - brown dwarfs - stars: low-mass - stars: luminosity function, mass function - open clusters and associations: individual (Alpha Per) - infrared: stars.

## 1 INTRODUCTION

The shape of the initial mass function (IMF) is of prime importance to understand the processes responsible for the formation of stars and brown dwarfs. The definition and the first estimate of the IMF was presented in Salpeter (1955). Our knowledge of the IMF has now improved both at the high-mass and low-mass ends. The mass spectrum in open clusters and in the field, defined as $\mathrm{d} N / \mathrm{d} M \propto M^{-\alpha}$ ( $\alpha$ is the exponent of the power law and equivalent to $x+1$, where $x$ is the slope of the logarithmic mass function), is currently best fitted by a three-segment power law with $\alpha=2.7$ for stars more massive than $1 \mathrm{M}_{\odot}, \alpha=2.2$ between 1 and $0.5 \mathrm{M}_{\odot}$ and $\alpha=1.3 \pm$

[^0]0.5 in the $0.5-0.08 \mathrm{M}_{\odot}$ mass range (Kroupa 2002). Alternatively, a log-normal function with a characteristic mass around $0.2-0.25$ $\mathrm{M}_{\odot}$ and dispersion $\sim 0.55$ (Chabrier 2003, 2005) provides a good match to current observations for the system mass function in the field. The advent of large-scale optical and near-infrared surveys towards open clusters extended the mass spectrum to the substellar regime but a consensus has yet to emerge on the detailed shape.
$\alpha$ Per is one of the few open star clusters within 200 pc of the Sun and younger than 200 Myr . The cluster is located to the north-east of the F5V supergiant Alpha Persei at a distance of $\sim 175-190 \mathrm{pc}$ (Pinsonneault et al. 1998; Robichon et al. 1999) with a revised distance of $172.4 \pm 2.7 \mathrm{pc}$ from the re-reduction of the Hipparcos data (van Leeuwen 2009). The cluster members have solar metallicity (Boesgaard \& Friel 1990) and the extinction along the line of sight is estimated as $\mathrm{A}_{V}=0.30 \mathrm{mag}$ with a possible differential extinction (Prosser 1992). It has been well studied, though less frequently than the Pleiades due to a smaller proper motion
$\left(\left(\mu_{\alpha} \cos \delta, \mu_{\delta}\right)=(+22.73,-26.51)\right.$ mas $^{\mathrm{yr}}{ }^{-1}$; van Leeuwen 2009) and a much lower galactic latitude ( $b=-7^{\circ}$ versus $-24^{\circ}$ ). Despite being further away than the Pleiades ( 170 pc versus 120 pc ), $\alpha$ Per is a good target for substellar studies because it is younger than the Pleiades $(85 \pm 10 \mathrm{Myr}$ versus $125 \pm 8 \mathrm{Myr})$, placing the lithium depletion boundary at $I_{c} \sim 17.7-17.8 \mathrm{mag}$ for both clusters.

Multi-wavelength surveys and spectroscopic follow-up observations have been performed in $\alpha$ Per to extract a clean sequence of cluster members from high-mass stars down to brown dwarfs. The first proper motion survey in the cluster was performed by Heckmann, Dieckvoss \& Kox (1956) and complemented by photometry from Mitchell (1960), yielding about 60 probable members (HE objects) whose final membership was revised by Prosser (1992). The membership of additional candidates proposed by Fresneau (1980) was subsequently established by Prosser (1992). Lower mass members (AP sources) were extracted by Stauffer et al. (1985) and Stauffer, Hartmann \& Jones (1989) on the basis of their proper motion, photometry and spectral characteristics. Prosser (1992) examined the Palomar photographic plates to extract new low-mass proper motion and photometric members down to a spectral type of M4 over a $6^{\circ}$ by $6^{\circ}$ field. Additional low-mass photometric candidates were reported from a deeper optical survey in a smaller area (Prosser 1994) as well as from X-rays observations with ROSAT (Prosser, Randich \& Stauffer 1996; Randich et al. 1996; Prosser \& Randich 1998; Prosser, Randich \& Simon 1998). The first brown dwarf candidates were spectroscopically confirmed by Stauffer et al. (1999), yielding a lithium age of $90 \pm 10 \mathrm{Myr}$, twice the turn-off main-sequence age ( 50 Myr ; Mermilliod 1981). A revised value of the age derived from the lithium method was published by Barrado y Navascués et al. (2004), estimated to $85 \pm 10 \mathrm{Myr}$. A deep optical survey complemented by near-infrared photometry extended the cluster sequence down to $0.03 \mathrm{M}_{\odot}$ (Barrado y Navascués et al. 2002). The best fit of the slope of the mass function was obtained for a power law index $\alpha=0.59 \pm 0.05$ over the $0.3-0.035 \mathrm{M}_{\odot}$ mass range, in agreement with estimates in the Pleiades (Dobbie et al. 2002a; Moraux et al. 2003) at that time. A wider survey based on photographic plates by Deacon \& Hambly (2004) derived a power law index $\alpha$ of $0.86(0.67-1.00)$ over the $1.0-0.2 \mathrm{M}_{\odot}$ range from a sample of high-probability members over $\sim 250$ square degrees. Finally, Lodieu et al. (2005) extracted about 20 new infrared photometric candidates from a deep $K$-band survey of 0.7 square degree previously covered in the optical by Barrado y Navascués et al. (2002). Additionally, 24 probable candidates from Barrado y Navascués et al. (2002) were confirmed as spectroscopic members with masses between 0.4 and $0.12 \mathrm{M}_{\odot}$.

The United Kingdom infrared telescope (UKIRT) Infrared Deep Sky Survey (UKIDSS; Lawrence et al. 2007) is a deep large-scale infrared survey conducted with the wide-field camera (WFCAM) (Casali et al. 2007) on UKIRT (Mauna Kea, Hawaii). The survey is subdivided into five components: the Large Area Survey, the Galactic Clusters Survey (hereafter GCS), the Galactic Plane Survey, the Deep Extragalactic Survey and the Ultra-Deep Survey. The GCS aims at covering $\sim 1000$ square degrees in 10 star-forming regions and open clusters down to $K=18.4$ mag at two epochs. The main scientific driver of the survey is to study the IMF and its dependence with environment in the substellar regime using a homogeneous set of low-mass stars and brown dwarfs over a large area in several regions.

In this paper we present the $\alpha$ Per mass function over $\sim 56$ square degrees derived from the UKIDSS GCS Data Release 9 (DR9). This is the second paper of its kind after the analysis of the Pleiades cluster presented in Lodieu, Deacon \& Hambly (2012). In Section 2
we present the photometric and astrometric data set employed to extract member candidates in $\alpha$ Per. In Section 3 we review the list of previously published members recovered by the UKIDSS GCS DR9 and revise their membership. In Section 4 we outline two methods for deriving the cluster luminosity function. One method relies on a relatively conservative photometric selection followed by the calculation of formal membership probabilities based on object positions in the proper motion vector point diagram (Section 4.1). The second method applies a more stringent colour cut followed by an astrometric selection based on the formal errors on the proper motions for each photometric candidate compared to that of the cluster (Section 4.2) for which we test the level of contamination (Section 5). In Section 6 we discuss the $K$-band variability of cluster member candidates in $\alpha$ Per. In Section 7 we derive the cluster luminosity and (system) mass function and compare it to other clusters studied as part of the GCS (Pleiades and Praesepe), and the field.

## 2 THE UKIDSS GCS IN $\alpha$ Per

The UKIDSS GCS DR9 released $~ 56$ square degrees observed in five passbands ( $Z Y J H K$; Hewett et al. 2006) in the $\alpha$ Per open cluster over a region defined by $\mathrm{RA}=44^{\circ}-60^{\circ}$ and Dec. $=44^{\circ}-54^{\circ}$.

We have selected all good quality point sources in $\alpha$ Per detected in at least $J H K 1$ (where $K 1$ stands for the first $K$-band epoch) and, where available, in $Z, Y$ and $K 2$ (second $K$-band epoch). We imposed a request on point sources only in $J H K$ and pushed the completeness towards the faint end by imposing limits on the ClassStat parameters (between -3 and +3 ) which classify the point-likeness of an image. The Structured Query Language (SQL) query used to select sources along the line of sight of the $\alpha$ Per is identical to the query used for the Pleiades (Lodieu et al. 2012). The SQL query includes the cross-matches with Two Micron All Sky Survey (2MASS; Cutri et al. 2003; Skrutskie et al. 2006) to compute proper motions for all sources brighter than the 2MASS $5 \sigma$ completeness limit at $J=15.8$ mag as well as the selection of proper motions from multiple epochs provided by the GCS. We used the GCS proper motion measurements in this work as they are more accurate due to the homogeneous coverage, completeness and spatial resolution of the UKIDSS images and the detailed relative astrometric mapping employed (Collins \& Hambly 2012), and of course the GCS proper motions are available for objects that are too faint for 2MASS. We limited our selection to sources fainter than $Z=11.6, Y=11.4, J=$ $11.0, H=11.5, K 1=10.0, K 2=10.4$ mag to avoid saturated point sources. The completeness limits, taken as the magnitude where the straight line fitting the shape of the number of sources as a function of magnitude falls off, are $Z=20.0, Y=19.6, J=19.1, H=18.4$, $K 1=17.6$ and $K 2=18.1 \mathrm{mag}$ (Fig. 1).

The query returned 2643045 sources with $J=11.0-21.2 \mathrm{mag}$ over $\sim 56$ square degrees towards the $\alpha$ Per cluster. The full coverage is displayed in Fig. 2 and the resulting $(Z-J, Z)$ colour-magnitude diagram is shown in Fig. 3 along with previously published member candidates (black filled dots). Note that theoretical isochrones plotted in this paper were specifically computed for the WFCAM set of filters at an age of 90 Myr (downloaded from France Allard's webpage). ${ }^{1}$ We combined the NextGen and DUSTY isochrones for effective temperatures above and below 2700 K , respectively, to convert magnitudes into masses (Section 7).

[^1]

Figure 1. Completeness of the GCS DR9 data set in the $\alpha$ Per cluster in each of the six filters. The polynomial fit of order 2 is shown as a red line and defines the 100 per cent completeness limit of the GCS DR9 in each passband.


Figure 2. Coverage from the UKIDSS GCS DR9 in the $\alpha$ Per open cluster in the standard angular plane coordinates $(\xi, \eta)$ choosing (RA, Dec. $)=\left(51^{\circ}\right.$, $49^{\circ}$ ) as the cluster centre. The total area covered is about 56 square degrees. The holes present in the coverage are due to the rejection of some tiles after quality control. GCS DR9 member candidates identified in this work are overplotted as black filled dots.

## 3 CROSS-MATCH WITH PREVIOUS SURVEYS

There are 455 probable members known in $\alpha$ Per extracted from previous proper motion and optical surveys (Heckmann et al. 1956; Mitchell 1960; Fresneau 1980; Stauffer et al. 1985, 1989, 1999; Prosser 1992, 1994; Prosser \& Randich 1998; Prosser et al. 1998;


Figure 3. $(Z-J, Z)$ CMD for $\sim 56$ square degrees in the $\alpha$ Per extracted from the UKIDSS Galactic Cluster Survey Data Release 9. Previously published member candidates in $\alpha$ Per are overplotted as filled dots. The mass scale is shown on the right-hand side of the diagrams and extends down to $0.03 \mathrm{M}_{\odot}$, according to the NextGen and DUSTY models assuming an age of 90 Myr and a distance of 172.4 pc (Baraffe et al. 1998; Chabrier et al. 2000).

Barrado y Navascués et al. 2002; Lodieu et al. 2005), and an additional 300 high-probability ( $p \geq 60$ per cent) member candidates from Deacon \& Hambly (2004).

We cross-matched catalogues from earlier studies with our full sample of over $\sim 2.5$ million sources retrieved from GCS DR9 to locate the cluster sequence in various colour-magnitude diagrams. We recovered a total of 426 known members in $\alpha$ Per after removing multiple detections present in various catalogues (Table A1). The numbers and percentages in brackets in the second and sixth column of Table 1 consider previously published sources lying in the magnitude range probed by the GCS. We also made a detailed analysis of the 629 previously known members not recovered by our SQL query. The numbers are given in the fourth column of Table A1 which is divided into five sub-columns. Most of these sources are either missing an image in $J, H$ or $K 1$, are not covered by the GCS ( 223 or 35.5 per cent), are brighter than the saturation limits set in our query ( 205 or 32.6 per cent) or are very likely proper motion non-members ( 48 or 7.6 per cent).

## 4 NEW SUBSTELLAR MEMBERS IN $\alpha$ Per

### 4.1 Probabilistic approach

### 4.1.1 Method

In this section we outline the probabilistic approach we employed to select low-mass stars and brown dwarf member candidates in $\alpha$ Per using photometry and astrometry from the UKIDSS GCS DR9. This method is described in detail in Deacon \& Hambly (2004) and Lodieu et al. (2007). The main steps are as follows.

Table 1. Updated membership of member candidates identified in $\alpha$ Per by earlier studies and recovered in the GCS DR9 sample. Papers studying $\alpha$ Per over the past decades and considered in this work are: Heckmann et al. 1956; Mitchell 1960; Fresneau 1980; Stauffer et al. 1985, 1989, 1999; Prosser 1992, 1994; Prosser \& Randich 1998; Prosser et al. 1998; Barrado y Navascués et al. 2002; Deacon \& Hambly 2004; Lodieu et al. 2005. Columns 2 and 3 give the numbers of sources published by the reference given in Column 1 and the numbers of sources recovered in GCS DR9, respectively. Column 4 (named No_DR9) is subdivided into several columns to give the reasons why some of the sources from earlier studies are not covered: 'Bright' stands for objects brighter than the GCS saturation limits, 'Outside' stands for sources outside the GCS DR9 coverage, 'No_mag' stands for sources missing at least one of the $J$, $H$ or $K$ magnitudes, ' $>3^{\prime \prime \prime}$ ' stands for sources beyond the 3 arcsec matching radius used in our study and 'Flag' stands for sources whose GCS flags are too bad to be included in our catalogue of point sources. Columns 5 and 6 give the numbers of high-probability members ( $p \geq 40$ per cent) and non-members (NM) according to our probabilistic approach (first number) and method 2 (second number). The last column gives the percentages of sources recovered in the GCS DR9 (ratio DR9/All).

| Survey | All | DR9 | No_DR9 |  |  |  |  | Members | NM | Per cent |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Bright | Outside | No_mag | $>3^{\prime \prime}$ | Flag |  |  |  |
| Heckmann1956 | 144 (78) | 7 | 65 | 1 | 71 | 0 | 0 | 0/0 | 0/7 | 4.9 (9.0) |
| Fresneau1980 | 56 (26) | 2 | 28 | 0 | 26 | 0 | 0 | 0/0 | 0/2 | 3.6 (46.4) |
| Prosser 1992 | 148 (96) | 44 | 34 | 18 | 24 | 25 | 1 | 28/31 | 16/13 | 29.7 (45.8) |
| Prosser 1994 | 31 (30) | 23 | 0 | 1 | 2 | 3 | 2 | 12/14 | 11/9 | 74.2 (76.7) |
| Prosser1998a | 89 (62) | 43 | 27 | 0 | 12 | 2 | 5 | 15/11 | 28/32 | 48.3 (69.4) |
| Prosser1998b | 70 (41) | 28 | 28 | 2 | 11 | 2 | 0 | 10/15 | 18/13 | 40.0 (68.3) |
| Stauffer1999 | 28 (28) | 23 | 0 | 0 | 0 | 0 | 0 | 9/10 | 14/13 | 82.1 (82.1) |
| Barrado2002_prob | 56 (56) | 48 | 0 | 0 | 6 | 6 | 0 | 25/32 | 23/16 | 85.7 (85.7) |
| Barrado2002_poss | 13 (13) | 7 | 0 | 1 | 1 | 3 | 1 | 4/4 | 3/3 | 53.8 (53.8) |
| Barrado2002_NM | 29 (29) | 15 | 0 | 1 | 2 | 3 | 0 | 3/3 | 12/12 | 51.7 (51.7) |
| Deacon2004 | 302 (258) | 244 | 24 | 20 | 8 | 0 | 6 | 154/149 | 90/95 | 80.8 (94.6) |
| Lodieu2005 | 39 (18) | 5 | 0 | 16 | 8 | 9 | 1 | 2/4 | 3/1 | 12.8 (27.8) |

(i) Define the cluster sequence using candidates published in the literature within the area covered by the GCS DR9.
(ii) Make a conservative cut in the $(Z-J, Z)$ diagram to include known members and any new cluster member candidates defined as $Z \geq 16.5$ and $Z \leq(11.5+5.0 \times(Z-J))$ OR $Z \leq 16.5$ and $Z \leq$ $(8.5+8.0 \times(Z-J))$ displayed as solid black lines in the top-left panel of Fig. 5.
(iii) Analyse the vector point diagram in a probabilistic manner to assign a membership probability for each photometric candidate with a proper motion measurement (Section 4.1.2).
(iv) Derive the luminosity and mass function by summation of membership probabilities to provide a statistically complete sample.

### 4.1.2 Membership probabilities

In order to calculate formal membership probabilities we have used the same technique as in Lodieu et al. (2012) to fit distribution functions to proper motion vector point diagrams (Hambly et al. 1995). The technique differs slightly from the original method presented in Deacon \& Hambly (2004) and Lodieu et al. (2007) in that the value of sigma $(\sigma)$ is fixed by the formal astrometric errors propagated from the centroiding errors given by the source extraction software employed upstream of the WFCAM Science Archive (Hambly et al. 2008), the main repository of UKIDSS data.

We refer the reader to the above-cited papers for more details and additional equations. First, we rotate the vector point diagram so that the cluster lies on the $y$ axis, assuming a proper motion of (22.73,-26.51) mas $\mathrm{yr}^{-1}$ for $\alpha$ Per (van Leeuwen 2009) after applying a very conservative photometric selection in the ( $Z-J, Z$ ) colour-magnitude diagram. We also note that we used the following rotation for the vector point diagram:
(i) $\mu_{x^{\prime}}=\cos (0.77 \times \mathrm{PI}) \times \mu_{x}-\sin (0.77 \times \mathrm{PI}) \times \mu_{y}$
(ii) $\mu_{\prime}^{\prime}=\cos (0.77 \times \mathrm{PI}) \times \mu_{x}+\sin (0.77 \times \mathrm{PI}) \times \mu_{y}$.

We have assumed that there are two contributions to the total distribution $\phi\left(\mu_{x}, \mu_{y}\right)$, one from the cluster, $\phi_{\mathrm{c}}\left(\mu_{x}, \mu_{y}\right)$, and one
from the field stars, $\phi_{\mathrm{f}}\left(\mu_{x}, \mu_{y}\right)$. The fitting region was delineated
 were added by means of a field star fraction $f$.
We characterized the cluster distribution as a bivariate Gaussian with a single standard deviation $\sigma$ and mean proper motion values in each axis $\mu_{x c}$ and $\mu_{y c}$. The field star distribution was fitted by a univariate Gaussian in the $x$ axis (with standard deviation $\Sigma_{x}$ and mean $\mu_{x f}$ ) and a declining exponential in the $y$ axis with a scale length $\tau$. The use of a declining exponential is a standard method (e.g. Jones \& Stauffer 1991) and is justified in that the field star distribution is not simply a circularly symmetric error distribution (i.e. capable of being modelled as a 2D Gaussian) rather there is a preferred direction of real field star motions resulting in a characteristic velocity ellipsoidal signature, i.e. a non-Gaussian tail, in the vector point diagram. This is best modelled (away from the central error-dominated distribution) as an exponential in the direction of the antapex (of the solar motion).
The best-fitting set of parameters were chosen using a maximum likelihood method (see Deacon \& Hambly 2004). However in a deviation from this method we did not fit for the standard deviation of the cluster proper motions $(\sigma)$. Instead we calculated the mean astrometric error for all objects in each magnitude range and used this as our cluster standard deviation. This fitting process was tested by Deacon \& Hambly (2004) where simulated data sets were created and run through the fitting process to recover the input parameters. These tests produced no significant offsets in the parameter values (see table 3 and appendix A of Deacon \& Hambly 2004, for results and more details on the procedure). Hence, we calculated the formal membership probabilities as
$p=\frac{\phi_{\mathrm{c}}}{f \phi_{\mathrm{f}}+(1-f) \phi_{\mathrm{c}}}$.
We split the sample into eight intervals of magnitudes because astrometric errors are a function of magnitude and also to improve the contrast between the field stars and the cluster. Each band is one magnitude wide and was fitted with all seven parameters in the same way as described in Deacon \& Hambly (2004). There was

Table 2. Summary of the results after running the program to derive membership probabilities. For each $Z$ magnitude range, we list the number of stars used in the fit $(\mathrm{Nb})$, the field star fraction $f$ and parameters describing the cluster and field star distribution. Units are in mas $\mathrm{yr}^{-1}$ except for the number of stars and the field star fraction $f$. The cluster star distribution is described by the mean proper motions in the $x$ and $y$ directions ( $\mu_{x_{c}}$ and $\mu_{y_{c}}$ ) and a standard deviation $\sigma$. Similarly, the field star distribution is characterized by a scale length for the $y$ axis $(\tau)$, a standard deviation $\Sigma_{x}$ and a mean proper motion in the $x$ direction $\left(\mu_{x_{\mathrm{f}}}\right)$. Note that the value of sigma $(\sigma)$ is fixed by the formal astrometric errors.

| $Z$ | Nb | $f$ | $\sigma$ | $\mu_{x_{c}}$ | $\mu_{y_{c}}$ | $\tau$ | $\Sigma_{x}$ | $\mu_{x_{\mathrm{f}}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | ---: |
| $12-13$ | 206 | 0.84 | 2.84 | -1.64 | 33.24 | 16.56 | 21.67 | 4.76 |
| $13-14$ | 488 | 0.75 | 2.82 | -1.98 | 33.91 | 21.32 | 16.27 | 0.78 |
| $14-15$ | 720 | 0.77 | 2.78 | -1.73 | 33.99 | 16.83 | 16.21 | 0.60 |
| $15-16$ | 913 | 0.83 | 2.85 | -1.74 | 33.47 | 14.69 | 15.05 | -0.50 |
| $16-17$ | 877 | 0.86 | 2.88 | -2.15 | 34.30 | 14.68 | 14.66 | 0.21 |
| $17-18$ | 503 | 0.92 | 3.05 | -1.42 | 33.35 | 13.71 | 14.27 | 0.08 |
| $18-19$ | 224 | 0.89 | 3.52 | -2.39 | 31.24 | 17.35 | 15.38 | 0.98 |
| $19-20$ | 203 | 0.90 | 5.12 | -3.12 | 31.62 | 12.39 | 14.81 | -0.39 |

no fit possible for the 20-21 magnitude bins because of the small number of sources in this bin. A summary of the fitted parameters from the probabilistic analysis described above is given in Table 2.

### 4.1.3 Probabilistic sample

The probabilistic approach yielded a total sample of 10176 sources with membership probabilities assigned to each of them. This sample contains 728 sources with membership probabilities higher than 40 per cent (including known ones previously published) listed in Table B1. Tightening this probability threshold to 50 and 60 per cent yields samples of 573 ( $\sim 27$ per cent less) and 431 ( $\sim 69$ per cent less) member candidates in $\alpha$ Per, respectively. These high-probability members are displayed in Fig. 5 with previously published candidates in $\alpha$ Per plotted in black.

### 4.2 Photometry and proper motion selection

In this section we outline a more widely used method (referred to as method 2 in the rest of the paper) that we applied to select low-mass and substellar member candidates in $\alpha$ Per. This procedure consists of selecting cluster candidates by applying proper motion selection followed by strict photometric cuts in various colour-magnitude diagrams. This alternative method provides an independent test of the probabilistic approach presented in the previous section.

The first step was to select all sources with formal errors on the proper motion within $3 \sigma$ of the mean proper motion of the cluster (Fig. 4), yielding a completeness better than 99 per cent assuming normally distributed errors. The main advantage of this method is that it does not rely on a single radius for the proper motion selection but rather takes into account the increasing uncertainty on the proper motion measurements between the GCS epochs with decreasing brightness.

Secondly, we plotted several colour-magnitude diagrams (Fig. 5) to define a series of lines based on the position of known $\alpha$ Per members identified in earlier studies and published over the past decades (Table 1). Those lines detailed below are plotted in Fig. 6 and improve on the pure proper motion selection. We note that those criteria are similar to those used for the Pleiades (Lodieu et al. 2012) because the younger age of $\alpha$ Per compared to the Pleiades is compensated by its larger distance.


Figure 4. Vector point diagram showing the proper motion in right ascension ( $x$ axis) and declination ( $y$ axis) for previously known member candidates recovered by the GCS DR9 (black dots) and the new member candidates selected with method 2 (red dots).
(i) $(Z-J, Z)=(0.60,12.0)$ to $(1.20,16.5)$
(ii) $(Z-J, Z)=(1.20,16.5)$ to $(2.00,20.0)$
(iii) $(Z-K, Z)=(1.20,11.5)$ to $(1.95,17.0)$
(iv) $(Z-K, Z)=(1.95,17.0)$ to $(4.00,21.5)$
(v) $(Y-J, Y)=(0.30,11.5)$ to $(0.55,16.5)$
(vi) $(Y-J, Y)=(0.55,16.0)$ to $(1.40,20.5)$
(vii) $(J-K, J)=(0.75,11.0)$ to $(0.75,16.5)$
(viii) $(J-K, J)=(0.75,16.5)$ to $(1.70,19.0)$.

This selection returned a total of 685 low-mass stars and brown dwarfs with $Z$ magnitude ranging from 12 to 21.5 , including known ones recovered by the GCS (Table C1). This total number is similar to the number of high-probability member candidates - 728 (431) with $p>40$ (60) per cent - in $\alpha$ Per identified via the probabilistic approach.

### 4.3 Search for lower mass members

In this section we search for fainter and cooler substellar members in $\alpha$ Per by dropping the constraint on the $Z$-band detection and later the $Z+Y$ bands.

### 4.3.1 YJHK detections

To extend the $\alpha$ Per cluster sequence to fainter brown dwarfs and cooler temperatures, we searched for potential candidate members undetected in $Z$. We imposed similar photometric and astrometric criteria as those detailed in Section 4.2 but analysed $Z$ drop-outs as follows:
(i) $Y \geq 18$ and $J \leq 19.1$ mag.
(ii) Candidates should lie above the line defined by $(Y-J, Y)=$ $(0.55,16.0)$ and $(1.40,20.5)$.


Figure 5. Colour-magnitude diagrams showing the member candidates previously reported in $\alpha$ Per (black dots) and all candidates extracted from our probabilistic analysis, including known ones (red dots). Upper-left: $(Z-J, Z)$; upper-right: $(Z-K, Z)$; lower-left: $(Y-J, Y)$; lower-right: $(J-K$, $J)$. Overplotted are the 90 Myr NextGen (solid line; Baraffe et al. 1998) and DUSTY (dashed line; Chabrier et al. 2000) isochrones shifted to a distance of 120 pc. The mass scale is shown on the right-hand side of the diagrams and spans $0.60-0.03 \mathrm{M}_{\odot}$, according to the 90 Myr isochrone models. The solid black lines in the upper-left diagram represent our conservative photometric cuts used for the probabilistic approach.
(iii) Candidates should lie above the line defined by $(J-K, J)=$ $(0.75,16.5)$ and $(1.70,19.0)$.
(iv) The position on the proper motion vector point diagram of each candidate should not deviate from the assumed cluster proper motion by more than $3 \sigma$.

This selection returned 13 additional member candidates in $\alpha$ Per (Table D1). All but four of them are indeed undetected in the $Z$-band images and look well detected in the other bands after checking the GCS DR9 images. Thus we are left with nine bona-fide member candidates.



### 4.3.2 JHK detections

We repeated the procedure described above looking for $Z$ and $Y$ non-detections. We additionally applied the following criteria:
(i) $J=18-19.1 \mathrm{mag}$.
(ii) Candidates should lie above the line defined by $(J-K, J)=$ $(0.75,16.5)$ and $(1.70,19.0)$.
(iii) The position on the proper motion vector point diagram of each candidate should not deviate from the assumed cluster proper motion by more than $3 \sigma$.


Figure 6. Same as Fig. 5 but only for member candidates in $\alpha$ Per selected using method 2. The $Y J H K$ - and $J H K$-only detections have been added too for completeness.

This query returned 36 new candidate members in $\alpha$ Per. After checking the GCS images, we retained only eight of them as bonafide candidates because the others actually appear in the $Z$ and/or $Y$ images (although detections are not reported in the GCS DR9 catalogue) or have no $Z$ and/or $Y$ images. The reasons for the rejection of 28 of the 36 candidates is given in the last column of Table D1.

## 5 ESTIMATION OF THE CONTAMINATION

In this section we estimate the level contamination present in our photometric and astrometric selection (method 2).

The number density of field objects in our final list of candidates as a function of mass is obtained in a similar way as in Boudreault
et al. (2012). We obtained the radial profile of our cluster candidates in three mass ranges: above $0.3 \mathrm{M}_{\odot}$, between 0.072 and $0.3 \mathrm{M}_{\odot}$ and below the hydrogen-burning limit at $0.072 \mathrm{M}_{\odot}$ (Fig. 8).

However, considering the incomplete coverage of the UKIDSS GCS DR9 towards $\alpha$ Per (holes present in the coverage due to quality control, see Fig. 2), all data points must be considered as lower limits: we are only partly complete up to the tidal radius of $\alpha$ Per at 2.91 ( 9.7 pc ; Makarov 2006) and up to 3.5 ( 95 per cent complete in coverage). Consequently, the estimated contamination represents an upper limit.

We used only the number of objects between $3^{\circ}$ and 3.5 (outside the estimated tidal radius) at each mass range to obtain an upper limit of contamination. This gives 2.92 objects per square degree for candidates with masses above $0.3 \mathrm{M}_{\odot}, 1.57$ between 0.072
and $0.3 \mathrm{M}_{\odot}$ and 0.62 objects per square degree for our substellar candidates. Within $3^{\circ}$ from the cluster centre, this gives a contamination of $35.1,15.9$ and 50.6 per cent for the same mass range, respectively, or 26.3 per cent for the whole $\alpha$ Per sample within $3^{\circ}$. This level of contamination brings into agreement within a factor of 2 the luminosity functions derived from both selection methods highlighted in this paper (left-hand side panel of Fig. 9).

These numbers appear quite large. We stress again that these are upper limits, since the coverage is not complete. However, we can claim the completeness higher than 90 per cent for our cluster candidate list and the determination of our mass function. This is justified by the fact that our astrometric selection includes all objects within $3 \sigma$ of the cluster's mean proper motion (completeness of $>99$ per cent) and that the lines used in our photometric selection go at least $2 \sigma$ bluer from the cluster main sequence in all the colour-magnitude diagrams used for the photometric selection (completeness of $\sim 95.4$ per cent).
Most of the contaminants of our cluster candidates with masses above $0.1 \mathrm{M}_{\odot}$ would be Galactic disc late-type and giant stars, while most of the contaminants of candidates less massive than 0.1 $\mathrm{M}_{\odot}$ would include Galactic disc late-type and giant stars, but also unresolved galaxies.

## 6 VARIABILITY AT 90 Myr

In this section we discuss the $K$-band variability of the low-mass stars and brown dwarfs in $\alpha$ Per using the two epochs provided by the GCS. First we considered the candidates extracted with method 2 , several of them being already published in the literature (Tables A1).
Fig. 7 shows ( $K 1-K 2$ ) versus $K 1$ for all candidate members in $\alpha$ Per from method 2 . The brightening in the $K 1=11-12$ mag range is due to the difference in depth between the first and second


Figure 7. Difference in the $K$ magnitude $(K 1-K 2)$ as a function of the $K 1$ magnitude for all member candidates in $\alpha$ Per selected with method 2. The $Y J H K$ - and $J H K$-only detections have been added too (dots with open squares and open triangles, respectively). Typical error bars on the $K 1-K 2$ colours as a function of magnitude are displayed as dotted lines.
epoch, around 0.5 mag both in the saturation and completeness limit. This is understandable because the exposure times have been doubled for the second epoch with relaxed constraints on the seeing requirement and weather conditions. We excluded those objects from our variability study. Overall, the sequence is very well defined and very few objects appear variable in the $K$ band.
We selected variable objects by looking at the standard deviation, robustly estimated as $1.48 \times$ the median absolute deviation which is the median of the sorted set of absolute values of


Figure 8. Radial density plots of our candidate members of $\alpha$ Per in three mass ranges: above $0.3 \mathrm{M}_{\odot}$ (top panel), between 0.72 and $0.3 \mathrm{M}_{\odot}$ (middle panel) and below the stellar/substellar limit at $0.072 \mathrm{M}_{\odot}$ (bottom panel). The error bars on each data point are Poissonian arising from the number of objects in each bin. The dotted horizontal line is the estimated contamination per square degree for each mass range.
deviation from the central value of the $K 1-K 2$ colour. We identified one potential variable object in the $K 1=11-12$ and $12-13 \mathrm{mag}$ range with differences in the $K$ band larger than $3 \sigma$ above the standard deviation. No additional variable source was picked up beyond $3 \sigma$ down to $K 1=16.5 \mathrm{mag}$. The candidate selected in the brightest bin appears saturated in the second epoch image, suggesting that the variability may be caused by the inaccurate photometry derived from saturated sources. The other source does not look saturated: its variability may be attributed to the presence of a faint companion located south-east at $\sim 1.2$ arcsec best visible in the $K 2$ image due to the greater depth of the second epoch. This variability analysis is not feasible for $K 1 \geq 16.5$ mag due to the small number of $\alpha$ Per candidate members beyond that magnitude range.

We conclude that the level of variability at 90 Myr is small, with standard deviations in the $0.06-0.09 \mathrm{mag}$ range, suggesting that it cannot account for the dispersion in the cluster sequence. The same conclusions are drawn from the high-probability sample and are consistent with our analysis of the Pleiades (Lodieu et al. 2012) and Praesepe (Boudreault et al. 2012) samples although we should point out that a handful of members are found to be variable.

## 7 THE LUMINOSITY AND INITIAL MASS FUNCTIONS

In this section we discuss the cluster luminosity and mass functions derived from the samples of member candidates in $\alpha$ Per extracted from both methods described in the previous section. We did not attempt to correct the mass function for binaries; hence, we compare our results to 'system' mass functions. Note that contrary to our work in the Pleiades and Praesepe, we are unable to estimate the substellar multiplicity due to larger scatter in the single-star and binary sequences due to crowding.

### 7.1 Age and distance of $\boldsymbol{\alpha}$ Per

Age determinations in open clusters can vary by up to a factor of 2 (Jeffries \& Naylor 2001): fitting of the upper main-sequence and giant branch (Mermilliod 1981) comparing with models including some convective overshoot (Maeder \& Mermilliod 1981) tend to yield younger ages than the lithium test (Rebolo, Martín \& Magazzù 1992). In the case of $\alpha$ Per, the former method gives 51 Myr whereas the latter suggests an age between $85 \pm 10$ (Barrado y Navascués, Stauffer \& Jayawardhana 2004) and $90 \pm$ 10 Myr (Stauffer et al. 1999). A similar discrepancy has been observed for the Pleiades ( 77 Myr versus 120 Myr ; Mermilliod 1981; Stauffer, Schultz \& Kirkpatrick 1998). Moreover, Meynet, Mermilliod \& Maeder (1993) revised the ages of 30 galactic open clusters based on an updated set of solar-metallicity isochrones (at that time) taking into account mass loss and moderate overshooting, yielding 52 and 100 Myr for the $\alpha$ Per and the Pleiades, respectively. The latter age for the Pleiades is favoured by the fitting technique of the main-sequence evolution developed by Naylor (2009) which quoted a 68 per cent confidence interval of $104-117 \mathrm{Myr}$ (mean value of 115 Myr ), in agreement with the careful comparison of model isochrones to the Pleiades photometric sequence by Bell et al. (2012). Other clusters with ages derived by the lithium depletion boundary tend to agree with older age estimates although with a possible trend towards slightly older ages, e.g. IC 4665 ( 36 Myr versus $28 \pm 4$ Myr Mermilliod 1981; Manzi et al. 2008), IC 2602 (3067 Myr versus $46 \pm 6$ Myr; Kharchenko et al. 2005; Dobbie, Lodieu \& Sharp 2010), NGC 2547 (20-35 Myr versus 34-36 Myr; Naylor
et al. 2002; Jeffries \& Oliveira 2005) or M35 (200 ${ }_{-100}^{+200}$ Myr versus 175 Myr; Sung \& Bessell 1999; Barrado y Navascués, Deliyannis \& Stauffer 2001c). We will employ the isochrones for the lithium test age of 90 Myr in the case of $\alpha$ Per, bearing in mind the current uncertainty on its age of the order of 10 Myr .

Several distance estimates have been published for $\alpha$ Per: $190.5_{-6.7}^{+7.2} \mathrm{pc}$ by Robichon et al. (1999), $176.2 \pm 5.0 \mathrm{pc}$ by Pinsonneault et al. (1998) and Makarov (2006). The latest value derived from a revised reduction of the Hipparcos data by van Leeuwen (2009) suggests a distance of $172.4 \pm 2.7 \mathrm{pc}$ which we adopt in this work.

To summarize, we adopt in this work a distance of 172.4 pc (van Leeuwen 2009) and employed the Lyon group NextGen (Baraffe et al. 1998) and DUSTY (Chabrier et al. 2000) models at an age of 90 Myr to convert the luminosity function into a mass function. We should point out that the lowest mass brown dwarfs in $\alpha$ Per are warmer than 1400 K , the upper limit where the COND models should be used (Baraffe et al. 2002).

### 7.2 The luminosity function

In this section, we construct two luminosity functions: (i) we used the sample of 10176 stars in $\alpha$ Per with computed membership probabilities (Section 4.1) and (ii) the 685 candidates identified with method 2 (Section 4.2). The luminosity function of the former method is derived by summing membership probabilities of all stars fitted to distribution functions in the vector point diagram, whereas the luminosity function of the latter is derived simply by summing the number of member candidates.

Both luminosity functions, i.e. the number of stars and brown dwarfs as a function of magnitude plotted per 0.5 mag bin, are displayed in Fig. 9. Both luminosity functions look very similar and match each other within the error bars. The numbers of objects per 0.5 mag bin increase quickly to reach a peak around $Z=14.5-15$ and drop off afterwards down to the completeness of our survey with a possible peak around $Z=19.5-20 \mathrm{mag}$ (Tables 3 and 4).The brightest bin is a lower limit due to the saturation limit of the GCS survey. The last four bins included in method 2 are not present in the probabilistic approach because the broad cluster distribution and low separation from the field causes the probabilities to be washed out. All bins in the probabilistic luminosity function are complete while the last two bins from method 2 are incomplete due to the constraints imposed on the $Z$-band detection. Moreover, the $\alpha$ Per luminosity function is very similar to the Pleiades one derived in a similar manner using the same homogeneous survey (Lodieu et al. 2012) although less populated mainly because of the smaller areal coverage.

### 7.3 The mass function

In this section we adopt the logarithmic form of the IMF as originally proposed by Salpeter (1955): $\xi\left(\log _{10} m\right)=\mathrm{d} n / \mathrm{d} \log _{10}(m) \propto m^{-x}$ where the exponent of the mass spectrum $\alpha=x+1$ following the formulation of Chabrier (2003). The $Z=12-21$ mag range translates into masses between $\sim 0.74$ and $\sim 0.03 \mathrm{M}_{\odot}$ ( 19 mag and $0.046 \mathrm{M}_{\odot}$ in the case of the probabilistic approach), assuming a revised distance of 172.4 pc (van Leeuwen 2009) and an age of 90 Myr for which the models are computed.

We included in Fig. 9 errors in both the $x$ axis $(\log M)$ and $y$ axis $(\mathrm{d} N / \mathrm{d} \log M)$ as follows. For the error bars on the masses, we considered three times the uncertainties on the age $(90 \pm 10 \mathrm{Myr}$;


Figure 9. Luminosity (left) and system mass (right) functions derived from our analysis of the UKIDSS GCS DR9 sample of member candidates in $\alpha$ Per. Error bars are Gehrels errors. The brightest bin and the last bins are very likely contaminated because of saturation and incompleteness, respectively. The left-hand side panel compares the luminosity function obtained from the probabilistic approach (black symbols and black line) and the luminosity function derived from the selection outlined by method 2 (red colour). Note that the sample of method 2 extends two magnitude bins fainter but they are incomplete as is the brightest bin due to saturation. The right-hand side panel compares the $\alpha$ Per mass function derived from this probabilistic approach (filled black dots linked by a solid line) and the mass function derived from method 2 (red symbols and red line). Error bars on the mass ( $x$ axis) are $3 \sigma$ uncertainties considering the errors on the age and distance of $\alpha$ Per. The Pleiades mass function derived in a similar manner is overplotted in green for comparison along with the field (system) mass functions in blue (Chabrier 2005).

Table 3. Values for the luminosity and mass functions (both in linear and logarithmic scales) per magnitude and mass bin for the $\alpha$ Per open cluster from the probabilistic approach. We assumed a distance of 172.4 pc and employed the NextGen and DUSTY 90 Myr theoretical isochrones.

| Mag range | Mass range | Mid-mass | $\mathrm{d} N$ | errH | errL | $\mathrm{d} N / \mathrm{d} M$ | errH | errL | $\mathrm{d} N / \mathrm{d} \log M$ | errH | errL |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $12.0-12.5$ | $0.7380-0.6420$ | 0.6900 | 6.01 | 3.60 | 2.40 | 62.60 | 37.50 | 25.00 | 2.00 | 0.47 | 0.51 |
| $12.5-13.0$ | $0.6420-0.5750$ | 0.6085 | 19.49 | 5.50 | 4.39 | 290.90 | 82.07 | 65.47 | 2.61 | 0.25 | 0.25 |
| $13.0-13.5$ | $0.5750-0.5070$ | 0.5410 | 48.33 | 8.01 | 6.93 | 710.74 | 117.73 | 101.97 | 2.95 | 0.15 | 0.15 |
| $13.5-14.0$ | $0.5070-0.4200$ | 0.4635 | 63.98 | 9.05 | 7.98 | 735.40 | 103.97 | 91.76 | 2.89 | 0.13 | 0.13 |
| $14.0-14.5$ | $0.4200-0.3260$ | 0.3730 | 66.16 | 9.18 | 8.12 | 703.83 | 97.66 | 86.37 | 2.78 | 0.13 | 0.13 |
| $14.5-15.0$ | $0.3260-0.2440$ | 0.2850 | 89.67 | 10.51 | 9.46 | 1093.54 | 128.16 | 115.32 | 2.85 | 0.11 | 0.11 |
| $15.0-15.5$ | $0.2440-0.1830$ | 0.2135 | 77.31 | 9.84 | 8.78 | 1267.38 | 161.23 | 143.91 | 2.79 | 0.12 | 0.12 |
| $15.5-16.0$ | $0.1830-0.1390$ | 0.1610 | 70.11 | 9.42 | 8.36 | 1593.41 | 214.04 | 189.96 | 2.77 | 0.13 | 0.13 |
| $16.0-16.5$ | $0.1390-0.1085$ | 0.1237 | 51.75 | 8.25 | 7.18 | 1696.72 | 270.35 | 235.29 | 2.68 | 0.15 | 0.15 |
| $16.5-17.0$ | $0.1085-0.0869$ | 0.0977 | 50.93 | 8.19 | 7.12 | 2357.87 | 379.11 | 329.58 | 2.72 | 0.15 | 0.15 |
| $17.0-17.5$ | $0.0869-0.0703$ | 0.0786 | 19.14 | 5.46 | 4.35 | 1153.01 | 328.90 | 261.82 | 2.32 | 0.25 | 0.26 |
| $17.5-18.0$ | $0.0703-0.0591$ | 0.0647 | 8.26 | 4.00 | 2.83 | 737.50 | 357.29 | 252.70 | 2.04 | 0.40 | 0.42 |
| $18.0-18.5$ | $0.0591-0.0514$ | 0.0553 | 8.79 | 4.09 | 2.92 | 1141.56 | 531.00 | 379.52 | 2.16 | 0.38 | 0.40 |
| $18.5-19.0$ | $0.0514-0.0459$ | 0.0486 | 6.50 | 3.69 | 2.50 | 1181.82 | 671.38 | 454.55 | 2.12 | 0.45 | 0.49 |

Stauffer et al. 1999) and distance ( $172.4 \pm 2.7 \mathrm{pc}$; van Leeuwen 2009) of $\alpha$ Per given us a validity range of $3 \sigma$ on the $x$ axis. Hence, we computed the masses with the 60 Myr NextGen and DUSTY isochrones shifted at a distance of 164.3 pc to define the lower limit and repeated the procedure with the 120 Myr isochrones for a distance of 180.5 pc as upper limits. The uncertainties on the $y$ axis, i.e. the $\mathrm{d} N / \mathrm{d} \log M$ values, are simply Gehrels error bars. This $\alpha$ Per mass function, directly compared to the Pleiades (Lodieu et al. 2012) and the field (Chabrier 2005) mass functions, agree within the error bars. We should point out the recent mass function of the field published by Kroupa et al. (2011) and described as a power law is almost identical to the log-normal form of Chabrier (2005).

In Fig. 10 we show a log-normal fit for $\alpha$ Per incorporating higher mass data points from Prosser (1992) in order to provide constraint on the parameters of the fit, in particular the characteristic mass which requires sufficient points on both sides of the peak in the function. We translated the 'corrected' luminosity function values making a small update to the absolute magnitudes for the distance modulus used here (6.18) over the value of 6.1 in Prosser (1992) The visual band mass-luminosity relation used comes from Marigo et al. (2008) evolutionary models. ${ }^{2}$ We include in the fit only those

[^2]Table 4. Same as Table 3 but for the sample identified with method 2.

| Mag range | Mass range | Mid-mass | $\mathrm{d} N$ | errH | errL | $\mathrm{d} N / \mathrm{d} M$ | errH | errL | $\mathrm{d} N / \mathrm{d} \log M$ | errH | errL |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $12.0-12.5$ | $0.7380-0.6420$ | 0.6900 | 4.00 | 3.18 | 1.94 | 41.67 | 33.12 | 20.17 | 1.82 | 0.58 | 0.66 |
| $12.5-13.0$ | $0.6420-0.5750$ | 0.6085 | 28.00 | 6.36 | 5.27 | 417.91 | 94.95 | 78.62 | 2.77 | 0.20 | 0.21 |
| $13.0-13.5$ | $0.5750-0.5070$ | 0.5410 | 61.00 | 8.86 | 7.79 | 897.06 | 130.27 | 114.62 | 3.05 | 0.14 | 0.14 |
| $13.5-14.0$ | $0.5070-0.4200$ | 0.4635 | 78.00 | 9.87 | 8.82 | 896.55 | 113.50 | 101.35 | 2.98 | 0.12 | 0.12 |
| $14.0-14.5$ | $0.4200-0.3260$ | 0.3730 | 79.00 | 9.93 | 8.87 | 840.43 | 105.64 | 94.41 | 2.86 | 0.12 | 0.12 |
| $14.5-15.0$ | $0.3260-0.2440$ | 0.2850 | 104.00 | 11.23 | 10.19 | 1268.29 | 137.01 | 124.22 | 2.92 | 0.10 | 0.10 |
| $15.0-15.5$ | $0.2440-0.1830$ | 0.2135 | 97.00 | 10.89 | 9.84 | 1590.16 | 178.47 | 161.25 | 2.89 | 0.11 | 0.11 |
| $15.5-16.0$ | $0.1830-0.1390$ | 0.1610 | 68.00 | 9.29 | 8.23 | 1545.45 | 211.17 | 187.07 | 2.76 | 0.13 | 0.13 |
| $16.0-16.5$ | $0.1390-0.1085$ | 0.1237 | 52.00 | 8.26 | 7.19 | 1704.92 | 270.92 | 235.86 | 2.68 | 0.15 | 0.15 |
| $16.5-17.0$ | $0.1085-0.0869$ | 0.0977 | 42.00 | 7.54 | 6.46 | 1944.44 | 349.00 | 299.14 | 2.64 | 0.17 | 0.17 |
| $17.0-17.5$ | $0.0869-0.0703$ | 0.0786 | 26.00 | 6.17 | 5.07 | 1566.27 | 371.81 | 305.69 | 2.45 | 0.21 | 0.22 |
| $17.5-18.0$ | $0.0703-0.0591$ | 0.0647 | 9.00 | 4.12 | 2.96 | 803.57 | 368.08 | 264.11 | 2.08 | 0.38 | 0.40 |
| $18.0-18.5$ | $0.0591-0.0514$ | 0.0553 | 7.00 | 3.78 | 2.60 | 909.09 | 491.41 | 337.41 | 2.06 | 0.43 | 0.46 |
| $18.5-19.0$ | $0.0514-0.0459$ | 0.0486 | 8.00 | 3.96 | 2.78 | 1454.55 | 719.64 | 506.16 | 2.21 | 0.40 | 0.43 |
| $19.0-19.5$ | $0.0459-0.0408$ | 0.0433 | 7.00 | 3.78 | 2.60 | 1372.55 | 741.94 | 509.43 | 2.14 | 0.43 | 0.46 |
| $19.5-20.0$ | $0.0408-0.0369$ | 0.0389 | 11.00 | 4.43 | 3.28 | 2820.51 | 1135.34 | 840.70 | 2.40 | 0.34 | 0.35 |
| $20.0-20.5$ | $0.0369-0.0331$ | 0.0350 | 3.00 | 2.94 | 1.66 | 789.47 | 772.76 | 436.40 | 1.80 | 0.68 | 0.80 |
| $20.5-21.0$ | $0.0331-0.0296$ | 0.0314 | 1.00 | 2.32 | 0.87 | 285.71 | 663.68 | 247.44 | 1.31 | 1.20 | 2.01 |

AlphaPer: $\mathrm{m}_{\mathrm{c}}=0.344 \pm 0.045 ; \sigma=0.458 \pm 0.019 ; \chi_{\nu}^{2}=2.275$


Figure 10. Log-normal fit to the GCS DR9 data (method 2; triangles with error bars) in conjunction with higher mass data points (stars with error bars) taken from Prosser (1992). The least-squares fit to the data points is the solid line with the shaded region corresponding to a formal $1 \sigma$ uncertainty.
higher mass points that are complete, i.e. for $M_{V}<+5$ from Prosser (1992), and excluding our own highest mass point from the GCS luminosity function, but we include the four lowest mass points from the GCS since excluding them does not significantly alter the fit. The mass function appears to be well represented by a log-normal with goodness of fit $\chi_{v}^{2} \approx 2.3$ which indicates some systematic fluctuations over and above the assumed sampling errors that could easily be due to sample contamination and/or systematic errors resulting from the assumed models.

It is interesting to compare this mass function with those from the Pleiades (Lodieu et al. 2012) and Praesepe (Boudreault et al. 2012), with similar higher mass constraints from optical photographic plate surveys - see Fig. 11. In the case of the Pleiades and $\alpha$ Per, the higher mass luminosity functions have been taken as complete and no normalization has been performed relative to the GCS luminosity functions, whereas for Praesepe we found that the mass function
resulting from the Jones \& Stauffer (1991) luminosity function is discontinuous with the GCS mass function from Boudreault et al. (2012). We determined a relative normalization of 0.447 in the $\log$ (a factor 2.8 ) for a minimal chi-squared in the log-normal fit for Praesepe.

In Table 5 we compare the log-normal fit parameters to the field system mass function parametrized by Chabrier $(2003,2005)$. There is some marginal evidence here for a variation in characteristic mass at the 1 to $2 \sigma$ level between $\alpha$ Per and Praesepe and the Pleiades, but this must be treated with caution given the range of goodness of fits obtained $\left(1.0<\chi_{v}^{2}<4.4\right)$ and particularly the significant departure from the fit for the Pleiades at the low-mass end. There is a clear statistically significant difference between the dispersion values of the field and $\alpha$ Per mass functions, not unexpected due to the difference in age. While we caution that the fitted values can be sensitive to the relative normalization between the GCS and higher mass data, changes in the relative offsets tend to narrow the log-normal fit rather than broaden it. In any case, it is interesting to note the general log-normal trend in these wide mass range mass functions.

Assuming that the observed lithium depletion boundary is at $M \sim 0.075 \mathrm{M}_{\odot}\left(M_{Z}=11.155\right.$; Stauffer et al. 1999; Barrado y Navascués et al. 2004) and a distance of 172.4 pc , the sample extracted by method 2 contains $685 \alpha$ Per member candidates, divided up into 632 stars ( 92.3 per cent) and 53 brown dwarfs ( 7.7 per cent). Lower percentages of brown dwarfs are obtained considering the sample of 431-728 high-probability members ( $p \geq 40-60$ per cent) identified in the probabilistic approach, because of larger uncertainties on the probabilities at the faint end. Hence, the star $(\sim 0.6-0.08$ $\mathrm{M}_{\odot}$ ) to brown dwarf ( $0.08-0.04 \mathrm{M}_{\odot}$ ) ratio in $\alpha$ Per spans 11.9 (10.4-12.7; $3 \sigma$ limits using the lower and upper distance estimates) to $16.8_{+2.5}^{-2.0}-33.3_{-1.9}^{+4.6}$, in agreement with measurements in IC 348 (8.3-11.6; Luhman et al. 2003; Andersen et al. 2006) but higher than other open clusters like M35 (4.5; Barrado y Navascués et al. 2001a) or the Pleiades ( 3.7 and 5.7-8.8; Bouvier et al. 1998; Lodieu et al. 2012), young star-forming regions (3.0-6.4 for the Trapezium Cluster; 3.8-4.3 for $\sigma$ Orionis; 3.8 for Chamaeleon; Hillenbrand \& Carpenter 2000; Muench et al. 2002; Andersen et al. 2006; Luhman 2007; Lodieu et al. 2009), the field (1.7-5.3; Kroupa 2002; Chabrier


Figure 11. Log-normal fit to the GCS DR9 data (triangles with error bars) in conjunction with higher mass data points (stars with error bars) taken for the Pleiades [Lodieu, Deacon \& Hambly 2012, excluding the three lowest mass bins; higher mass points from the unpublished compilations of Prosser and Stauffer, see for example Hambly et al. (1999) and references therein]; $\alpha$ Per (this work) and Praesepe [Boudreault et al. (2012); higher mass points from Jones \& Stauffer (1991)]. In each case, least-squares fits to the data points are the solid line with the shaded region corresponding to a formal $1 \sigma$ uncertainty.

Table 5. Comparison between log-normal mass function parameters for the $\alpha$ Per, Pleiades and Praesepe clusters as determined from GCS DR9 data in conjunction with higher mass bin data from optical photographic proper motion surveys, compared with the field system mass function parameters quoted by Chabrier $(2003,2005)$.

| Population | Characteristic <br> mass $m_{\mathrm{C}}\left(\mathrm{M}_{\odot}\right)$ | Dispersion <br> $\sigma$ | $\chi_{v}^{2}$ |
| :---: | :---: | :---: | :---: |
| $\alpha$ Per | $0.344 \pm 0.045$ | $0.458 \pm 0.019$ | 2.275 |
| Pleiades | $0.247 \pm 0.047$ | $0.456 \pm 0.023$ | 4.382 |
| Praesepe | $0.328 \pm 0.035$ | $0.434 \pm 0.015$ | 0.962 |
| Field (Chabrier 2003) | 0.22 | 0.57 |  |
| Field (Chabrier 2005) | 0.25 | 0.55 |  |

2005; Andersen et al. 2006) and hydrodynamical simulations of star clusters (3.8-5.0; Bate 2009, 2012). We list the ranges of the ratios because the stellar and substellar intervals differ slightly from study to study.

## 8 SUMMARY

We have presented the outcome of a wide ( $\sim 56$ square degrees) and deep ( $J \sim 19.1 \mathrm{mag}$ ) survey in the $\alpha$ Per open cluster as part of the UKIDSS GCS DR9. The main results of our study can be summarized as follows.
(i) We recovered member candidates in $\alpha$ Per previously published and updated their membership assignations.
(ii) We selected photometrically and astrometrically potential $\alpha$ Per member candidates using two independent but complementary methods: the probabilistic analysis and a more standard method combining photometry and proper motion cuts.
(iii) We investigated the $K$-band variability of $\alpha$ Per cluster members and found virtually no variability at the level of $0.06-0.09 \mathrm{mag}$.
(iv) We derived the luminosity function from both selection methods and found no difference within the error bars.
(v) We derived the $\alpha$ Per mass function over the $0.5-0.04 \mathrm{M}_{\odot}$ mass range: its shape is similar to the Pleiades mass function and best represented by a log-normal form with a characteristic mass of $0.34 \mathrm{M}_{\odot}$ and a dispersion of 0.46 .

This paper represents a significant improvement in our census of the $\alpha$ Per low-mass and substellar population as well as our knowledge of the mass function across the hydrogen-burning limit over the entire cluster. We believe that this paper will represent a reference for many more years to come in $\alpha$ Per. We will now extend this study to other regions surveyed by the GCS to address the question of the universality of the mass function using a homogeneous set of photometric and astrometric data. Future work to constrain current models of star formation includes the search for companions to investigate their multiplicity properties, the determination of the radial velocities of $\alpha$ Per members and deeper surveys to test the theory of the fragmentation limit.

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## APPENDIX A: TABLE OF KNOWN MEMBER CANDIDATES PREVIOUSLY PUBLISHED IN $\alpha$ Per AND RECOVERED IN THE UKIDSS GCS DR9

Table A1. Sample of known member candidates previously published in $\alpha$ Per and recovered in GCS DR9. We list the equatorial coordinates (J2000), GCS ZYJHK $1 K 2$ photometry, proper motions (in mas $\mathrm{yr}^{-1}$ ) and their errors, reduced chi-squared statistic of the astrometric fit for each source ( $\chi^{2}$ value), membership probabilities when available from our probabilistic study, and names from the literature. A '-' in the probability column means that the object lacks measurement $\alpha$ Per member candidates are ordered by increasing right ascension. This table is available electronically as Supporting Information with the online version of the journal.

| RA | Dec. | Z | Y | $J$ | H | K1 | K2 | $\mu_{\alpha} \cos \delta \pm$ err | $\mu_{\delta} \pm \mathrm{err}$ | $\chi^{2}$ | Prob | Name |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 025817.66 | +48 2800.4 | 16.152 | 15.700 | 15.071 | 14.531 | 14.187 | 14.175 | $23.07 \pm 2.91$ | $-14.86 \pm 2.91$ | 0.59 | - | DH12_Prob73.7 |
| 030121.38 | +4835 23.3 | 13.971 | 13.664 | 13.142 | 12.494 | 12.257 | 12.267 | $24.39 \pm 2.86$ | $-21.71 \pm 2.86$ | 0.11 | 0.77 | DH15_Prob70.8 |
| $\ldots$ | ... | ... | ... | ... | ... | ... | ... | ... | $\ldots$ | ... | $\ldots$ | ... |
| 035037.08 | +48 1231.4 | 14.124 | 13.621 | 13.079 | 12.534 | 12.234 | 12.226 | $21.45 \pm 2.03$ | $-35.54 \pm 2.03$ | 6.38 | - | AP265_M9.9_Y? |
| 035037.08 | +48 1231.4 | 14.124 | 13.621 | 13.079 | 12.534 | 12.234 | 12.226 | $21.45 \pm 2.03$ | $-35.54 \pm 2.03$ | 6.38 | - | DH302_Prob79.1 |

## APPENDIX B: TABLE OF NEW MEMBER CANDIDATES IN $\alpha$ Per IDENTIFIED IN THE PROBABILISTIC APPROACH

Table B1. Coordinates (J2000), near-infrared (ZYJHK1K2) photometry and proper motions (in mas $\mathrm{yr}^{-1}$ ) for all highprobability ( $p \geq 40$ per cent) members in $\alpha$ Per identified in the UKIDSS GCS DR9 using the probabilistic approach. The last column gives the membership probability. Sources are ordered by increasing right ascension. This table is available electronically as Supporting Information with the online version of the journal.

| RA | Dec. | $Z$ | $Y$ | $J$ | $H$ | $K 1$ | $K 2$ | $\mu_{\alpha} \cos \delta$ | $\mu_{\delta}$ | Prob |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 025852.52 | +494032.6 | 14.543 | - | 13.655 | 12.993 | 12.761 | 12.748 | 26.74 | -22.66 | 0.71 |
| 025857.10 | +504441.4 | 15.074 | 14.759 | 14.213 | 13.590 | 13.335 | 13.344 | 23.90 | -20.86 | 0.61 |
| $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| 035001.17 | +482057.3 | 16.587 | 16.104 | 15.490 | 14.812 | 14.494 | 14.462 | 20.58 | -26.20 | 0.46 |
| 035020.08 | +481354.8 | 15.402 | 15.029 | 14.504 | 13.940 | 13.645 | 13.617 | 25.02 | -19.56 | 0.43 |

## APPENDIX C: TABLE OF NEW MEMBER CANDIDATES IN $\alpha$ Per SELECTED WITH METHOD 2

Table C1. Coordinates (J2000), near-infrared (ZYJHK1K2) photometry and proper motions (in mas $\mathrm{yr}^{-1}$ ) for all member candidates in $\alpha$ Per identified in the UKIDSS GCS DR9 with the standard method (method 2), including known members from earlier studies. Sources are ordered by increasing right ascension. This table is available electronically as Supporting Information with the online version of the journal.

| RA | Dec. | $Z$ | $Y$ | $J$ | $H$ | $K 1$ | $K 2$ | $\mu_{\alpha} \cos \delta$ | $\mu_{\delta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 025751.18 | +480829.0 | 16.810 | 16.101 | 15.536 | 14.900 | 14.598 | 14.632 | $17.56 \pm 2.96$ | $-29.20 \pm 2.96$ |
| 025752.10 | +482358.8 | 17.175 | 16.459 | 15.810 | 15.192 | 14.851 | 14.828 | $22.12 \pm 3.05$ | $-17.13 \pm 3.05$ |
| $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| 035018.91 | +482459.1 | 18.766 | 17.618 | 16.684 | 16.108 | 15.610 | 15.542 | $18.12 \pm 2.54$ | $-25.55 \pm 2.54$ |
| 035035.47 | +472556.3 | 17.188 | 16.424 | 15.716 | 15.156 | 14.728 | 14.730 | $22.78 \pm 2.59$ | $-29.06 \pm 2.59$ |

## APPENDIX D: TABLE OF MEMBER CANDIDATES IN $\alpha$ Per WITH YJHK- AND JHK-ONLY DETECTIONS

Table D1. Coordinates (J2000), near-infrared (ZYJHK1K2) photometry and proper motions (in mas $\mathrm{yr}^{-1}$ ) for $Y J H K$-only (top) and $J H K$-only (bottom) detections.

| RA | Dec. | Z | $Y$ | $J$ | H | K1 | K2 | $\mu_{\alpha} \cos \delta$ | $\mu_{\delta}$ | Comments |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 031626.24 | +49 0012.2 | - | 20.314 | 18.797 | 17.849 | 16.993 | 17.030 | $14.76 \pm 4.60$ | $-40.10 \pm 4.60$ |  |
| 032114.97 | +49 1423.2 | - | 19.548 | 18.220 | 17.410 | 16.673 | 16.713 | $21.93 \pm 3.59$ | $-18.70 \pm 3.59$ |  |
| 032309.75 | +5020 03.3 | - | 19.319 | 18.017 | 17.307 | 16.591 | 16.658 | $18.62 \pm 4.84$ | $-36.35 \pm 4.84$ |  |
| 032401.62 | +464852.7 | - | 19.291 | 18.038 | 17.273 | 16.596 | 16.720 | $11.99 \pm 5.96$ | $-14.60 \pm 5.96$ |  |
| 032749.28 | +50 4226.3 | - | 18.483 | 17.404 | 16.771 | 16.191 | 16.127 | $13.76 \pm 4.35$ | $-21.26 \pm 4.35$ | Detected in $Z$ |
| 032811.64 | +514650.6 | - | 18.138 | 15.299 | 14.980 | 14.781 | 14.804 | $28.61 \pm 3.04$ | $-22.53 \pm 3.04$ | Detected in $Z$ |
| 032838.15 | +485951.1 | - | 20.508 | 18.738 | 17.845 | 16.997 | 16.853 | $26.30 \pm 4.44$ | $-29.45 \pm 4.44$ |  |
| 032949.62 | +483505.3 | - | 20.112 | 18.739 | 17.846 | 16.998 | 16.978 | $17.76 \pm 5.21$ | $-35.06 \pm 5.21$ |  |
| 033052.69 | +502834.7 | - | 19.908 | 18.498 | 17.390 | 16.481 | 16.424 | $28.15 \pm 4.34$ | $-30.99 \pm 4.34$ |  |
| 033227.13 | +480054.3 | - | 19.428 | 18.138 | 17.338 | 16.629 | 16.546 | $31.10 \pm 4.60$ | $-23.63 \pm 4.60$ |  |
| 033242.65 | +500139.8 | - | 20.449 | 19.026 | 17.926 | 16.966 | 17.130 | $20.66 \pm 6.40$ | $-34.40 \pm 6.40$ |  |
| 033603.86 | +50 3957.7 | - | 20.269 | 18.899 | 17.680 | 17.017 | 17.059 | $5.34 \pm 6.87$ | $-6.19 \pm 6.87$ | Detected in $Z$ |
| 033953.40 | +49 0659.5 | - | 20.228 | 18.785 | 17.865 | 17.098 | 16.986 | $8.58 \pm 7.88$ | $-22.64 \pm 7.88$ | Detected in $Z$ |
| 025948.86 | +475031.8 | - | - | 18.810 | 17.938 | 17.138 | 17.249 | $4.88 \pm 6.53$ | $-14.06 \pm 6.53$ | No $Z, Y$ images |
| 030114.17 | +49 0305.5 | - | - | 18.798 | 17.916 | 16.824 | 17.112 | $7.84 \pm 6.33$ | $-10.54 \pm 6.33$ | No $Y$ image, detected in $Z$ ? |
| 030907.55 | +493736.8 | - | - | 19.067 | 18.241 | 17.339 | 17.336 | $-0.08 \pm 9.06$ | $-1.19 \pm 9.06$ | No $Y$ image |
| 031032.62 | +49 2519.4 | - | - | 19.043 | 18.290 | 17.289 | 17.416 | $0.63 \pm 8.53$ | $-5.17 \pm 8.53$ | Detected in $Y$ |
| 031126.76 | +49 1352.2 | - | - | 19.016 | 18.315 | 17.295 | 17.414 | $8.31 \pm 8.81$ | $-1.26 \pm 8.81$ | Detected in $Z+Y$ |
| 031205.31 | +49 0216.0 | - | - | 18.975 | 17.868 | 17.244 | 17.283 | $8.17 \pm 8.49$ | $-12.99 \pm 8.49$ | No $Y$ image |
| 031225.76 | +4943 42.5 | - | - | 19.058 | 18.137 | 16.984 | 17.066 | $14.33 \pm 7.12$ | $-16.47 \pm 7.12$ | No $Y$ image |
| 031456.42 | +50 0828.3 | - | - | 19.048 | 17.988 | 17.192 | 17.061 | $1.16 \pm 8.21$ | $-21.09 \pm 8.21$ | Detected in $Z+Y$ ? ? |
| 031622.23 | +523200.9 | - | - | 18.591 | 17.299 | 16.577 | 16.743 | $23.79 \pm 7.20$ | $-10.38 \pm 7.20$ | Spike of a bright star |
| 031625.02 | +523209.1 | - | - | 18.585 | 17.861 | 17.018 | 17.308 | $32.54 \pm 5.36$ | $-26.23 \pm 5.36$ | Detected in |
| 031737.31 | +470514.6 | - | - | 18.988 | 18.136 | 17.167 | 17.125 | $16.59 \pm 8.48$ | $-7.33 \pm 8.48$ | No $Y$ image |
| 031749.13 | +465835.3 | - | - | 19.058 | 18.136 | 17.290 | 17.220 | $5.62 \pm 9.28$ | $-3.97 \pm 9.28$ | Detected in $Y$ |
| 031823.96 | +462649.6 | - | - | 18.573 | 17.553 | 16.699 | 16.774 | $6.39 \pm 5.51$ | $-42.34 \pm 5.51$ | Detected in $Y$ |
| 031911.02 | +512447.0 | - | - | 19.093 | 18.463 | 17.314 | 17.329 | $2.22 \pm 9.51$ | $-9.80 \pm 9.51$ | No $Y$ image |
| 031919.19 | +461018.8 | - | - | 19.001 | 17.768 | 16.921 | 16.975 | $28.50 \pm 9.56$ | $-13.52 \pm 9.56$ | Detected in $Z+Y$ |
| 032041.79 | +50 4538.6 | - | - | 18.796 | 18.187 | 17.030 | 17.484 | $-0.96 \pm 9.46$ | $-10.49 \pm 9.46$ |  |
| 032114.74 | +46 3627.1 | - | - | 19.007 | 18.143 | 17.180 | 17.220 | $3.95 \pm 9.83$ | $-18.58 \pm 9.83$ | Detected in $Z+Y$ ? ? |
| 032153.44 | +464702.6 | - | - | 19.092 | 18.201 | 17.357 | 17.193 | $6.41 \pm 10.48$ | $-12.39 \pm 10.48$ |  |
| 032302.14 | +521358.8 | - | - | 18.945 | 17.873 | 17.000 | 17.120 | $11.70 \pm 10.54$ | $-6.76 \pm 10.54$ | Detected in $Y$ |
| 032403.07 | +50 0301.0 | - | - | 19.098 | 17.911 | 17.071 | 17.090 | $16.35 \pm 7.93$ | $-20.52 \pm 7.93$ | Detected in $Y$ |
| 032432.00 | +470429.5 | - | - | 18.656 | 17.941 | 17.035 | 16.878 | $5.29 \pm 8.02$ | $-11.42 \pm 8.02$ | Detected in $Z+Y$ |
| 032446.24 | +463625.4 | - | - | 19.040 | 18.289 | 17.244 | 17.165 | $10.75 \pm 10.39$ | $-21.22 \pm 10.39$ |  |
| 032614.34 | +515536.4 | - | - | 18.718 | 17.778 | 16.824 | 16.717 | $2.88 \pm 8.33$ | $-7.91 \pm 8.33$ |  |
| 032714.93 | +521558.3 | - | - | 18.750 | 17.710 | 16.717 | 16.713 | $6.39 \pm 6.88$ | $-9.24 \pm 6.88$ | Detected in $Z+Y$ |
| 032732.27 | +471145.4 | - | - | 19.079 | 18.325 | 17.133 | 17.227 | $-1.16 \pm 10.13$ | $-16.30 \pm 10.13$ |  |
| 032743.73 | +465502.9 | - | - | 19.042 | 18.433 | 17.275 | 17.368 | $5.02 \pm 10.04$ | $-8.77 \pm 10.04$ |  |
| 032816.47 | +4829 41.9 | - | - | 18.986 | 18.067 | 17.075 | 16.986 | $9.54 \pm 6.66$ | $-10.33 \pm 6.66$ | Detected in $Z+Y$ |
| 033017.49 | +48 0456.8 | - | - | 19.040 | 18.184 | 17.283 | 17.416 | $13.82 \pm 7.76$ | $-30.29 \pm 7.76$ |  |
| 033046.17 | +45 5736.0 | - | - | 18.938 | 17.983 | 17.221 | 17.139 | $9.57 \pm 8.37$ | $-9.08 \pm 8.37$ | Detected in $Z+Y$ |
| 033055.78 | +455556.6 | - | - | 18.465 | 17.740 | 16.968 | 16.958 | $25.29 \pm 8.24$ | $-19.76 \pm 8.24$ | Detected in $Z+Y$ |
| 033101.32 | +460914.4 | - | - | 19.092 | 17.954 | 17.266 | 17.256 | $2.25 \pm 9.52$ | $-0.70 \pm 9.52$ | Detected in $Z+Y$ |
| 033108.17 | +501016.6 | - | - | 18.924 | 18.075 | 17.172 | 17.177 | $-2.82 \pm 9.25$ | $-5.09 \pm 9.25$ |  |
| 033453.62 | +473424.5 | - | - | 19.077 | 18.227 | 17.341 | 17.419 | $20.62 \pm 9.37$ | $-4.52 \pm 9.37$ | Detected in $Z+Y$ |
| 033611.61 | +464835.0 | - | - | 18.925 | 17.920 | 16.965 | 16.953 | $14.27 \pm 7.87$ | $-21.11 \pm 7.87$ | Detected in $Z+Y$ |
| 033626.40 | +483822.4 | - | - | 19.081 | 18.295 | 17.183 | 17.317 | $-2.90 \pm 9.79$ | $0.75 \pm 9.79$ | Detected in $Y$ |
| 034315.74 | +4734 45.0 | - | - | 18.859 | 17.886 | 17.177 | 17.267 | $22.76 \pm 8.90$ | $-10.89 \pm 8.90$ | Detected in $Z+Y$ |

## APPENDIX E: TABLE OF SUBSTELLAR MULTIPLE SYSTEM CANDIDATES IN $\alpha$ Per

Table E1. Coordinates (J2000), near-infrared (ZYJHK1K2) photometry and proper motions (in mas yr ${ }^{-1}$ ) for substellar multiple system candidates identified photometrically in $\alpha$ Per.

| RA | Dec. | $Z$ | $Y$ | $J$ | $H$ | $K 1$ | $K 2$ | $\mu_{\alpha} \cos \delta$ | $\mu_{\delta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 030736.61 | +481938.7 | 17.013 | 16.253 | 15.493 | 14.909 | 14.496 | 14.490 | $18.12 \pm 2.74$ | $-24.09 \pm 2.74$ |
| 031840.74 | +505601.1 | 16.252 | 15.537 | 14.801 | 14.229 | 13.793 | 13.764 | $20.63 \pm 3.05$ | $-22.96 \pm 3.05$ |
| 032029.92 | +475642.8 | 16.833 | 16.064 | 15.301 | 14.714 | 14.283 | 14.265 | $24.79 \pm 2.27$ | $-23.82 \pm 2.27$ |
| 032308.69 | +480450.5 | 16.699 | 16.046 | 15.294 | 14.734 | 14.318 | 14.353 | $17.92 \pm 2.28$ | $-27.75 \pm 2.28$ |
| 032525.86 | +475442.4 | 17.892 | 16.752 | 15.841 | 15.170 | 14.645 | 14.628 | $20.05 \pm 2.32$ | $-25.97 \pm 2.32$ |
| 032731.32 | +483923.1 | 16.692 | 15.920 | 15.161 | 14.620 | 14.165 | 14.140 | $27.28 \pm 2.26$ | $-27.68 \pm 2.26$ |
| 032800.87 | +514152.8 | 17.226 | 16.584 | 15.848 | 14.940 | 14.592 | 14.623 | $14.22 \pm 2.94$ | $-20.31 \pm 2.94$ |
| 033024.28 | +515410.8 | 18.011 | 16.808 | 15.836 | 15.211 | 14.622 | 14.618 | $28.01 \pm 2.96$ | $-32.46 \pm 2.96$ |
| 033114.07 | +464754.8 | 16.850 | 16.157 | 15.444 | 14.849 | 14.441 | 14.465 | $26.05 \pm 2.94$ | $-24.76 \pm 2.94$ |
| 033337.35 | +504339.5 | 14.641 | 14.275 | 13.598 | 12.386 | 12.259 | 12.598 | $15.57 \pm 2.86$ | $-19.85 \pm 2.86$ |
| 033459.87 | +483753.7 | 16.586 | 15.877 | 15.141 | 14.572 | 14.129 | 14.154 | $25.53 \pm 2.98$ | $-25.35 \pm 2.98$ |
| 033547.37 | +491742.9 | 16.817 | 15.913 | 15.158 | 14.590 | 14.151 | 14.167 | $24.20 \pm 3.05$ | $-22.97 \pm 3.05$ |
| 033939.68 | +495527.3 | 19.573 | 18.169 | 16.991 | 16.334 | 15.715 | 15.661 | $26.05 \pm 3.43$ | $-21.38 \pm 3.43$ |
| 034059.57 | +471141.2 | 16.554 | 15.897 | 15.149 | 14.565 | 14.132 | 14.149 | $23.90 \pm 2.94$ | $-24.26 \pm 2.94$ |

## SUPPORTING INFORMATION

Additional Supporting Information may be found in the online version of this article:

Table A1. Known member candidates previously published in $\alpha$ Per and recovered in GCS DR9.
Table B1. Coordinates (J2000), near-infrared (ZYJHK1K2) photometry and proper motions (in mas $\mathrm{yr}^{-1}$ ) for all high-probability ( $p \geq 40$ per cent) members in $\alpha$ Per identified in the UKIDSS GCS DR9 using the probabilistic approach.

Table C1. Coordinates (J2000), near-infrared (ZYJHK1K2) photometry and proper motions (in mas $\mathrm{yr}^{-1}$ ) for all member candidates in $\alpha$ Per identified in the UKIDSS GCS DR9 with the standard method (method 2), including known members from earlier studies.

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[^0]:    *Based on observations made with the United Kingdom Infrared Telescope, operated by the Joint Astronomy Centre on behalf of the U.K. Particle Physics and Astronomy Research Council.
    $\dagger$ E-mail: nlodieu@iac.es

[^1]:    ${ }^{1}$ France Allard's Phoenix web simulator can be found at http://phoenix.enslyon.fr/simulator/index.faces

[^2]:    ${ }^{2}$ http://stev.oapd.inaf.it/cgi-bin/cmd_2.3

