

THE ABSENCE OF AN ENVIRONMENTAL DEPENDENCE IN THE MASS-METALLICITY RELATION AT $Z=2$

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ABSTRACT

We investigate the environmental dependence of the mass-metallicity relation at $z = 2$ with MOSFIRE/Keck as part of the ZFIRE survey. Here, we present the chemical abundance of a Virgo-like progenitor at $z = 2.095$ that has an established red sequence. We identified 43 cluster ($\langle z \rangle = 2.095 \pm 0.004$) and 74 field galaxies ($\langle z \rangle = 2.195 \pm 0.083$) for which we can measure metallicities. For the first time, we show that there is no discernible difference between the mass-metallicity relation of field and cluster galaxies to within 0.02dex. Both our field and cluster galaxy mass-metallicity relations are consistent with recent field galaxy studies at $z \sim 2$. We present hydrodynamical simulations for which we derive mass-metallicity relations for field and cluster galaxies. We find at most a 0.1dex offset towards more metal-rich simulated cluster galaxies. Our results from both simulations and observations are suggestive that environmental effects, if present, are small and are secondary to the ongoing inflow and outflow processes that are governed by galaxy halo mass.

Subject headings: cosmology: observations — galaxies: abundances — galaxies: fundamental parameters — galaxies: high-redshift — galaxies: evolution

1. INTRODUCTION

The evolution of galaxies is likely dependent on halo mass and regulated by baryonic feedback cycles (e.g., Dekel et al. 2009). In addition, environment plays a role in removing and truncating gas reservoirs while increasing the frequency of galaxy interactions/mergers, which could cause differences in morphology and color seen locally for field and cluster galaxies (e.g., Dressler 1980). However, selecting low redshift galaxies by their stellar ages and stellar masses shows that their observable properties are independent of environment (see Blanton & Moustakas 2009, for a review). This is also confirmed by studies showing that the mass-metallicity relation of local field and cluster star-forming galaxies are consistent (Mouhcine et al. 2007; Ellison et al. 2009; Scudder et al. 2012; Hughes et al. 2013). If there is a difference in the mass-metallicity relation as a function of environment at $z \sim 0$, then it is observationally constrained to be around 0.05dex (Ellison et al. 2009) while simulations constrain it to be less than ~ 0.05 dex (Davé et al. 2011).

Although it is clear that a mass-metallicity relation exists at $z \sim 2$ (Erb et al. 2006; Sanders et al. 2014; Steidel et al. 2014), it is unclear if it differs as a function of environment at high redshift where clusters are beginning to form. Exploring the environmental influence on galaxies at high redshift is difficult since only a handful of spectroscopically

confirmed clusters with $z \gtrsim 2$ exist (e.g., Kurk et al. 2004; Galametz et al. 2013; Gobat et al. 2013; Shimakawa et al. 2014; Valentino et al. 2014; Yuan et al. 2014). Only three studies have attempted to address the effects of environment on the mass-metallicity relation using small samples of galaxies, or inhomogeneous field and cluster selections, and have produced conflicting results. A star-forming protocluster containing 6 galaxies at $z = 1.99$ was found to be up to 0.25dex poorer in metals than their field counterparts (Valentino et al. 2014), while two star-forming protoclusters at $z = 2.2$ (24 galaxies) and at $z = 2.5$ (36 galaxies) were found to be more enriched than those of field galaxies for $M_* < 10^{11} M_\odot$ (Shimakawa et al. 2014). On the other-hand, Kulas et al. (2013) found for 20 star-forming protocluster galaxies that they do not exhibit a dependence of metallicity on mass (i.e., zero slope) with the low-mass protocluster galaxies showing an enhancement in metallicity compared to field galaxies. Although there appears to be some disagreement between studies, these ~ 0.15 dex differences are marginally detected at less than two sigma.

Here, we present Keck/MOSFIRE observations from the ZFIRE survey⁸ (T. Nanayakkara et al. in prep) in order to clarify the debate on the dependence between the mass-metallicity relation and environment found at $z \sim 2$. We identified 43 cluster ($\langle z \rangle = 2.095 \pm 0.004$) and 74 field galaxies ($\langle z \rangle = 2.195 \pm 0.083$) (Spitler et al. 2012; Yuan et al. 2014) for which we can measure metallicities. This study is unique given the large number of galaxies obtained for a single cluster, with field galaxies selected the same way and observed simultaneously with the same instrument. In § 2 we describe the data and our metallicity measurements. In § 3, we present the mass-metallicity relation for field and cluster galaxies at $z \sim 2$. Our data are consistent with previously published field galaxy relations, however contrary to other cluster galaxy works, we do not find a difference in the relation as a function of environment. We further show that this result is consistent with

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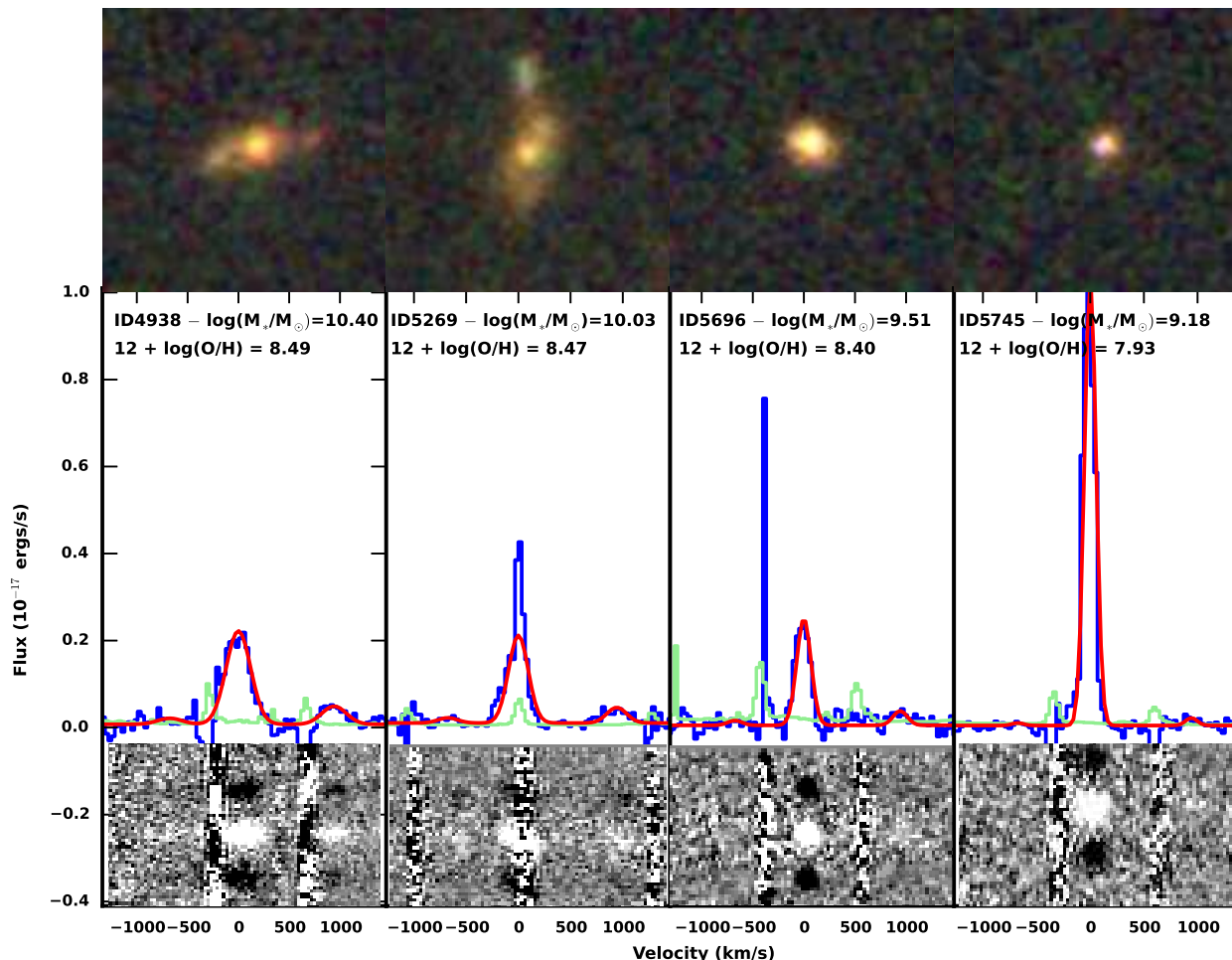


FIG. 1.— Representative sample of flux-calibrated 1D and 2D MOSFIRE spectra of four cluster members in order of decreasing stellar mass. The spectra are plotted with respect to the systemic velocity of each galaxy, as defined by their nebular emission-lines. Both the [N II] doublet and H α are shown in the 1D and 2D spectra. Strong sky-lines are seen as long vertical lines in the 2D spectra. The 1D data (blue), 1σ error spectra (green) and best-fit Gaussian models (red) are shown. The metallicity for each object is also listed. The top panels show $4'' \times 4''$ three color *HST* images, using the F814W, F125W and F160W filters, obtained from the publicly available CANDELS data (Grogin et al. 2011; Koekemoer et al. 2011; Skelton et al. 2014).

current simulation predictions. We end with concluding remarks in § 4.

Throughout, we adopt a $h = 0.70$, $\Omega_M = 0.3$, $\Omega_\Lambda = 0.7$ cosmology.

2. MOSFIRE SPECTROSCOPIC OBSERVATIONS AND SAMPLE

The $z = 2.095$ cluster was previously identified using the photometric redshifts (Spitler et al. 2012) from the medium-band FourStar Galaxy Evolution Survey (ZFOURGE, Straatman et al. in prep). As part of the spectroscopic followup to ZFOURGE, the ZFIRE survey used Keck/MOSFIRE to spectroscopically confirm the existence of a Virgo-like progenitor at $z = 2.095$ containing at least 57 members with a velocity dispersion of 550 km s^{-1} (Yuan et al. 2014). Furthermore, the ZFIRE survey yielded an additional 123 spectroscopic redshifts of field galaxies with $1.98 \leq z \leq 3.26$. The spectroscopic targets were selected using the photometric redshifts from the K-band selected catalog from ZFOURGE (Spitler et al. 2014, Straatman et al. in prep), which have an accuracy of $\Delta z / (1 + z_{\text{spec}}) = 2\%$ (Tomczak et al. 2014; Yuan et al. 2014).

The MOSFIRE near-infrared K- and H-band spectroscopic observations, data reduction and flux calibration procedures are described in Yuan et al. (2014) with additional details to

be presented T. Nanayakkara et al. (in prep). All spectra are calibrated to vacuum wavelengths. Our typical 3σ flux limit is $1.8 \times 10^{-18} \text{ ergs/s/cm}^2$.

Gaussian profiles were simultaneously fit to H α and [N II] emission-lines to determine their total flux. The line centers and velocity widths were tied together for a given pair of lines. Examples of our 2D and 1D MOSFIRE spectra and line-fits are shown in Figure 1 for galaxies that have stellar masses ranging between $\log(M/M_\odot) = 10.4 - 9.2$ (also see Yuan et al. (2014) for additional examples).

We compute a gas-phase oxygen abundance for each galaxy using the N2 relation of Pettini & Pagel (2004) where $12 + \log(\text{O}/\text{H}) = 8.90 + 0.57 \times \text{N2}$ ($\text{N2} \equiv \log([\text{N II}]/\text{H}\alpha)$). The Pettini & Pagel (2004) relation is established from a sample of low-redshift extragalactic H II regions for which both N2 and oxygen abundances are directly measured. Applying this relation to high redshift galaxies implies the caveat/assumption that the ionization parameters and electron densities are similar to those of low redshift galaxies, however, it is known that typical ionization parameters are much higher for $z \sim 2$ galaxies with $\log(U) \geq 7.3$ (e.g., Shirazi et al. 2014; Steidel et al. 2014; Kewley et al. 2015). It is important to note however, that Kewley et al. (2015) has shown that our $z \sim 2$ field and cluster galaxies have consistent ISM conditions, which al-

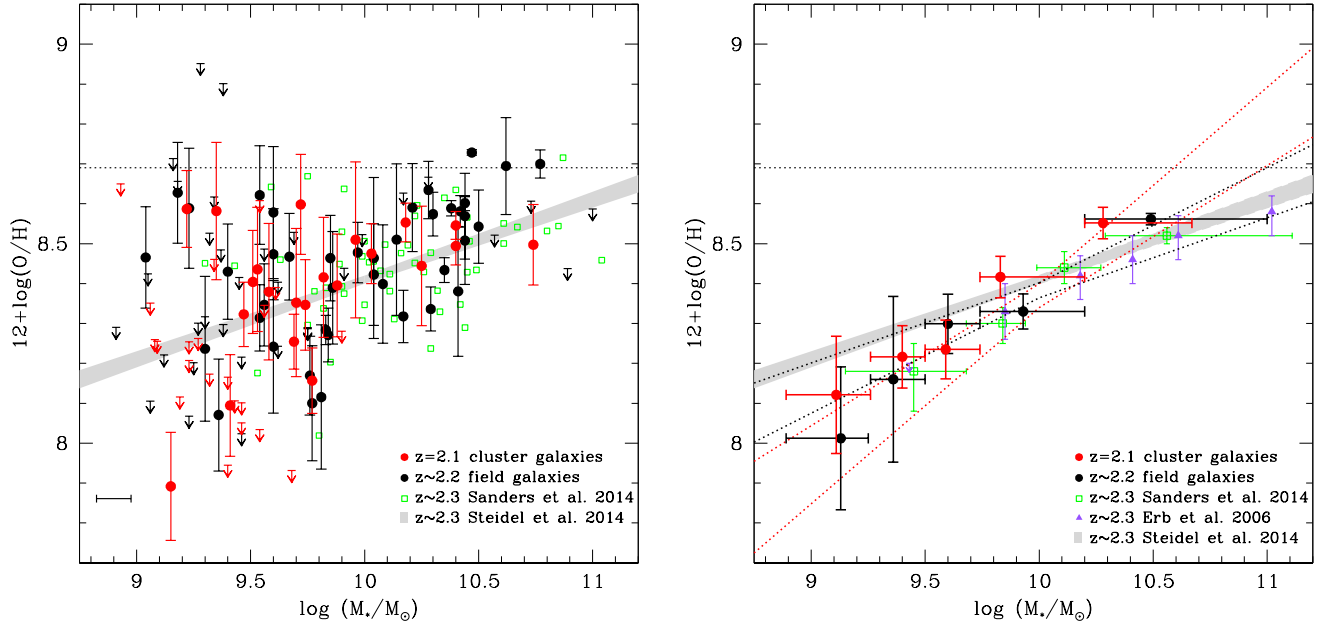


FIG. 2. — (left) The mass-metallicity relation for star-forming $z = 2.1$ cluster (red) and $z \sim 2.1$ field galaxies (black). Circles indicate metallicity measurements where both $H\alpha$ and $[NII]$ are detected with greater than 3σ significance and downward arrows are quoted as 1σ limits on $[NII]$. The average error in determining the mass of galaxies using ZFOURGE photometry and FAST of ± 0.076 is shown in the bottom left. The green circles show the individual MOSDEF detections (Sanders et al. 2014), while the grey shaded region shows the fit to KBSS-MOSFIRE (Steidel et al. 2014). The dotted horizontal line solar abundance (Asplund et al. 2009). — (right) The dotted lines are bootstrap fits, with 1σ limits, to the mass-metallicity data from the left panel for cluster (red) and field (black) galaxies (see text for details). The solid points are stacked spectra within a given mass bin and note that these are consistent with the fitted data. We further show additional binned data from the literature. Note both cluster and field galaxies are consistent within the 1σ errors.

lows for a meaningful direct comparison between the mass-metallicity relations of field and cluster galaxies.

From the parent sample of Yuan et al. (2014), we identify 49 cluster and 86 field galaxies with an $H\alpha$ flux detected at greater than 3σ significance. Using the ZFOURGE AGN catalog (M. Cowley et al. in prep), we remove AGNs from our sample (7 from the field, 3 from the cluster). An AGN is identified as, or a combination of, an infrared source (following methods of Donley et al. 2012), an X-ray source (following methods of Szokoly et al. 2004) or a radio source (following methods of G. Rees et al. 2015, in prep). In addition, we further require $\log([NII]/H\alpha) < -0.3$ (Sanders et al. 2014), which removes 8 additional AGN (5 field, 3 cluster).

Our final sample contains 43 cluster ($\langle z \rangle = 2.095 \pm 0.004$) and 74 field galaxies ($1.98 \leq z \leq 2.56$, $\langle z \rangle = 2.195 \pm 0.083$) for which we can measure metallicities. We require a 3σ detection significance level for $[NII]$, otherwise 1σ detection limits are shown. Our final sample contains 22 metallicity measurements and 21 limits for the cluster galaxies and 41 metallicity measurements and 33 limits for the field galaxies.

We use stellar masses computed from the ZFOURGE photometry using Bruzual & Charlot (2003) stellar population models with FAST (Kriek et al. 2009), assuming exponentially declining star formation histories, solar metallicity, a Chabrier (2003) initial mass function and constrained to the spectroscopic redshift (see Tomczak et al. 2014, for details).

2D Kolmogorov-Smirnov test shows that the cluster and field galaxies have statistically consistent ($P(KS) < 1\sigma$) observational properties such as extinction, (determined by FAST) and star-formation rates (determined by $H\alpha$ – to be discussed in Kacprzak et al., in prep).

3. RESULTS

3.1. ZFIRE Observations

In Figure 2 (left), we show the mass-metallicity relation for our field (black) and cluster (red) galaxies at $z \sim 2$, including 1σ limits. We have metallicity measurements for a significant range of galaxy masses from $8.9 \leq \log(M/M_\odot) \leq 11.0$. We further show the 53 individual detection from MOSDEF (Sanders et al. 2014) and the fitted relation from KBSS-MOSFIRE (Steidel et al. 2014). Note that the scatter in the data is similar to the scatter in the MOSDEF distribution and our data seem to follow the fitted data from KBSS-MOSFIRE. Furthermore, our cluster and field galaxies appear to have similar mass-metallicity distributions.

In Figure 2 (right), we show a bootstrap fit (1000 times) to the data from Figure 2 (left) using $12 + \log(O/H) = y_i + m_i(M - 10)$. We fit the relation including the 1σ limits using the expectation-maximization maximum-likelihood method of Wolynetz (1979). Including limits we find for the cluster $y_c = 8.370 \pm 0.030$ and $m_c = 0.424 \pm 0.068$ while for the field we find $y_f = 8.384 \pm 0.018$ and $m_f = 0.245 \pm 0.044$. These fits, along with their 1σ errors, are shown as dotted lines in Figure 2 (right). From the fitted data, we find that both cluster and field galaxies exhibit similar mass-metallicity relations and are consistent within 1σ . The maximum separation between the fitted field and cluster galaxy metallicity is at most 0.014 ± 0.035 dex. There could be a difference in the slope between field and cluster galaxies, which is mostly driven by the larger number of low mass cluster metallicity limits.

To explore the similarities between the field and cluster galaxy data, we further stack the spectra in five mass bins with roughly equal numbers of galaxies per bin. We stacked the spectra, weighting by the uncertainty spectrum, to determine the typical metallicity in a given mass bin shown in Fig-

ure 2. We found no discernible difference if we weighted each spectrum by its $H\alpha$ luminosity. Again, the stacked spectra show that cluster and field galaxies have equivalent mass-metallicity relations and are consistent within the 1σ errors. The stacked spectra are also consistent with the fits to the individual datapoints.

The fits and stacked data for both our field and cluster galaxies are consistent with the previous results of MOSDEF (Sanders et al. 2014), KBSS-MOSFIRE (Steidel et al. 2014) and Erb et al. (2006). However, the low mass end of the field galaxies marginally deviate away from the KBSS-MOSFIRE fit, but is consistent with their binned data (not shown). Any observed minor differences could be due to sample selection biases (KBSS-MOSFIRE is rest-frame ultraviolet selected while MOSDEF and ZFIRE are rest-frame optical selected) or how detection significance levels and fits were conducted. However, given that our cluster and field data are consistent with all previous works, further validates the lack of a difference between field and cluster galaxies.

3.2. Cosmological Simulations

To further examine if the environment of galaxies actually influences their metallicities, we perform a similar analysis using cosmological simulations. The simulations are performed with a Gadget-3 based hydrodynamical code that includes important baryon physics such as star formation, feedback from supernovae and AGN, and chemical enrichment from Type II and Ia supernovae, and asymptotic giant branch stars with Kroupa IMF (see Kobayashi, Springel & White 2007; Taylor & Kobayashi 2014, for the details). Metallicities derived for Kroupa IMF are virtually identical for those derived for a Chabrier IMF. The input nucleosynthesis yields are in excellent agreement with the observed elemental abundances in the Milky Way Galaxy from carbon to zinc (Kobayashi & Nakasato 2011).

Different from the Davé et al. (2011) simulations, we include AGN feedback, whereby AGN-driven winds eject metals from massive galaxies to the intergalactic medium, and some less-massive galaxies undergo external enrichment depending on the environment. However we find that for the mass-metallicity relation, the effect of AGN is small and the trend originates mainly from supernova/hypernova-driven galactic winds, which is much larger in less-massive galaxies (Kobayashi, Springel & White 2007).

The simulations are run for a $25h^{-1}$ Mpc box with two different initial conditions. The cluster simulation is chosen from ten realizations to have a strongest central concentration, which gives the most massive galaxy with the stellar mass $\sim 10^{12}M_{\odot}$ (Taylor & Kobayashi 2014) at $z=0$, while the field simulation is same as used in Kobayashi, Springel & White (2007) and does not contain any central concentrations. The stellar masses are estimated by fitting a core-Sérsic profile, and the oxygen abundances are measured in $15h^{-1}$ kpc weighted by the star formation rates of gas particles to be comparable to our emission-line observations. At $z=0$, the mass-metallicity relations of simulated galaxies are in good agreement with the observed mass-metallicity relations both for stellar and gas-phase metallicities (Taylor & Kobayashi 2015). These relations evolve as a function of time, with lower metallicities and a steeper slope at higher redshifts (Taylor & Kobayashi 2015, in prep.).

Figure 3 shows the mass-metallicity relations of the “cluster” and “field” simulations at $z=2$. We apply an

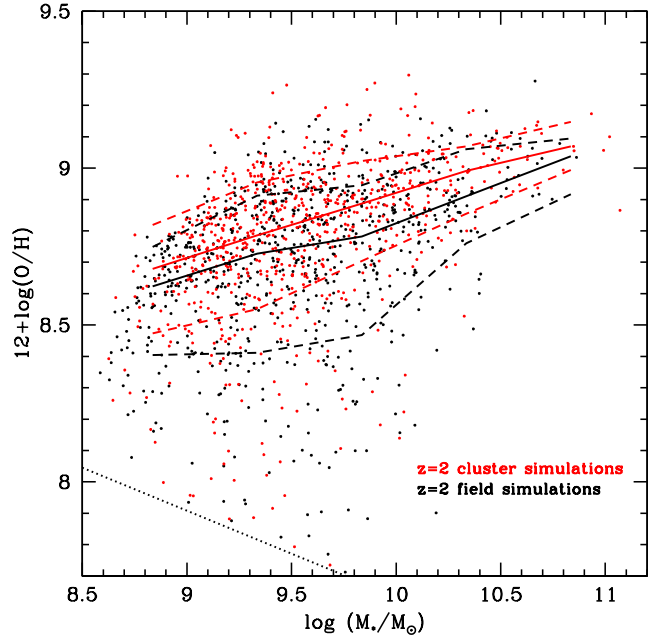


FIG. 3.— Mass-metallicity relation for simulated field (black) and cluster (red) galaxies. The solid and dashed lines show the moving median with 68% of confidence level. The dotted line is an observational limit of our ZFIRE survey (see text for details). We find that both field and cluster galaxies have consistent mass-metallicity relations with maximum separations of 0.1dex.

observationally-based detection limit on the simulated mass-metallicity distribution. The N2-based metallicity measurement is confined by the detection limit of $[NII]$. Based on a few simple assumptions, Yuan et al. (2013) used the SFR-mass relation, flux detection limit and redshift to determine observational detection limit on the mass-metallicity relation. For the ZFIRE survey, our typical 3σ flux limit is 1.8×10^{-18} ergs/s/cm² resulting in the limiting relation of: $12+\log(O/H) > -0.274 \times \log(M_*/M_{\odot}) + 10.371$. This observational detection limit is important for understanding the incompleteness and biases due to observational limitations. While all of our observational data reside above this limit, we apply it to our simulated data (dotted line).

In Figure 3, the solid and dashed lines show the moving median with 68% confidence levels also shown. Both the field and cluster galaxies exhibit similar mass-metallicity relationships within 1σ . The maximum separation between the fitted field and cluster galaxy metallicity is at most 0.1dex. This is consistent with previous results from $z=0$ simulations that constrain the difference to be less than ~ 0.05 dex (Davé et al. 2011).

Note that there is an ~ 0.5 dex offset in the zero-point between simulations and observations, which can be partly attributed to the uncertain normalization in metallicity measurements (e.g., Kewley & Ellison 2008; Davé et al. 2011).

4. CONCLUSIONS

High redshift protoclusters are ideal laboratories to study the possible influences of environment on galaxies. It is important to establish whether the environment can affect chemical evolution via restricting inflow and outflow, which may be responsible for galaxies migrating from the blue to the red sequence, or if a galaxy’s chemical evolution is established early and is solely dependent on its internal evolutionary pro-

cesses.

The environment may already be affecting the morphological properties of galaxies at $z = 2$. In our cluster, quiescent galaxies have similar colors and sizes relative to field quiescent galaxies, however, cluster star-forming galaxies are larger and redder on average when compared to field star-forming galaxies – suggesting environment can transform some galaxy properties at this early stage of formation (Allen et al. 2015).

It is a concern when searching for metallicity differences as a function of environment that the precise metallicities derived for high redshift galaxies are likely incorrect due to their different ISM conditions relative to $z = 0$ galaxies – where emission-line metallicity indicators are calibrated (e.g., Pettini & Pagel 2004). However, this does not affect the relative offsets between the field and cluster galaxies given Kewley et al. (2015) has shown that for our cluster, both field and cluster galaxies have similar ISM conditions.

Here, we present the chemical abundance of a Virgo-like progenitor at $z = 2.1$ (Yuan et al. 2014) that has an established red sequence (Spitler et al. 2012). Using our sample of field galaxies at a similar redshift, we show that the mass-metallicity relation of field and cluster galaxies are consistent with 1σ errors. We further show that both our field and cluster galaxies have consistent mass-metallicity relations when compared to other field galaxy surveys at $z \sim 2$ (Erb et al. 2006; Sanders et al. 2014; Steidel et al. 2014). Although we cannot rule out weak environmental trends in chemical enrichment, our analysis shows that the difference between field and cluster galaxies in the mass-metallicity relation is less than 0.02dex.

Our simulations have shown that cluster galaxies may be marginally more metal rich than field galaxies by at most 0.1dex (although consistent within the scatter). This could be due to the removal of gas from the outskirts of galaxies which can produce an observed increase in metallicity by ~ 0.1 dex (Hughes et al. 2013) or due to the shorter gas recycling times

in denser environments (Oppenheimer & Davé 2008). However, given that the offset is small, it is suggestive that these effects do not play a significant role in the chemical evolution of galaxies, especially given that there is no observed differences in mass-metallicity relation of field and cluster galaxies at $z = 0$ (Mouhcine et al. 2007; Scudder et al. 2012; Hughes et al. 2013).

Our results from the simulations and observations are suggestive that environmental effects, if present, are secondary to the ongoing internal processes within $z \sim 2$ galaxies that are likely governed by halo mass.

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