Galactic synchrotron emissivity measurements between $250^\circ < l < 355^\circ$
from the GLEAM survey with the MWA

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ABSTRACT

Synchrotron emission pervades the Galactic plane at low radio frequencies, originating from cosmic ray electrons interacting with the Galactic magnetic field. Using a low-frequency radio telescope, the Murchison Widefield Array (MWA), we measure the free–free absorption of this Galactic synchrotron emission by intervening H II regions along the line of sight. These absorption measurements allow us to calculate the Galactic cosmic ray electron emissivity behind and in front of 47 detected H II regions in the region $250^\circ < l < 355^\circ, |b| < 2^\circ$. We find that all average emissivities between the H II regions and the Galactic edge along the line of sight ($\epsilon_B$) are in the range of $0.39 \sim 1.45$ K pc$^{-1}$ with a mean of 0.77 K pc$^{-1}$ and a variance of 0.14 K pc$^{-1}$ at 88 MHz. Our best model, the two-circle model, divides the Galactic disc into three regions using two circles centring on the Galactic Centre. It shows a high emissivity region near the Galactic Centre, a low emissivity region near the Galactic edge, and a medium emissivity region between these two regions, contrary to the trend found by previous studies.

Key words: cosmic rays – H II regions – Galaxy: structure – radio continuum: general.

1 INTRODUCTION

The plane of the Milky Way is dominated by diffuse radio emission with a brightness temperature of thousands of Kelvin at low radio frequencies (Zheng et al. 2016). This emission originates from relativistic electrons interacting with the Galactic magnetic field. The total synchrotron power ($P$) radiated by one electron follows $P \propto E^2 B^2$, where $E$ is the electron energy, and $B$ is the Galactic magnetic field strength (Westfold 1959; Epstein & Feldman 1967).

Many previous low radio frequency observations have focused on two-dimensional (2D) Galactic maps, i.e. tracing the distribution of brightness temperature with Galactic longitude and latitude. de Oliveira-Costa et al. (2008) summarized 31 total power surveys in...
the frequency range $4 \leq \nu \leq 820$ MHz. All of these observations were performed between 1944 and 1982 with angular resolutions larger than several degrees. One widely used all-sky map is that of Haslam et al. (1982) at 408 MHz with an angular resolution of 51 arcmin. All of these 2D maps show a bright Galactic plane with spatial emissivity$^1$ information integrated along the line of sight. Here, we focus on the effect of the ionized hydrogen regions (H II regions) on the synchrotron background that gives rise to absorption features against the bright diffuse synchrotron background.

Absorption of synchrotron radiation by H II regions provides an opportunity to study the emission distribution along the line of sight. This idea is not new, having been put forward in the 1950s (Scheuer & Ryle 1953). The diffuse synchrotron emission can be absorbed by the free electrons in H II regions via free–free absorption. The optical depth of an H II region is proportional to the inverse square of the frequency (Condon 1992). At frequencies below about 200 MHz, H II regions become nearly opaque and show absorption features (Mezger & Henderson 1967; Kurtz 2005). Thus, an H II region separates the emission behind it and in front of it along the line of sight, when completed with information about the H II region distance, enabling the measurement of the radial emissivity distribution with respect to the Sun.

To date, a modest number of H II region absorption measurements have been made, limited by the poor angular resolution of telescopes observing at low radio frequencies. Most synchrotron emissivity calculations were made from samples each with less than 18 objects of sufficient angular resolution (Jones & Finlay 1974; Caswell 1976; Krymkin 1978; Abramenko & Krymkin 1990; Fleishman & Tokarev 1995; Roger et al. 1999). Prior to Nord et al. (2006, hereafter N06) only 46 emissivity measures had been collected in the literature. In the largest study to date, N06 observed the Galactic Centre in the range of $-15^\circ < \ell < 26^\circ$, $|b| < 5^\circ$ at 74 MHz using the Very Large Array (VLA). They detected 42 absorbing H II regions (mainly in the range of $6^\circ < \ell < 26^\circ$) with known distances from which they modelled the emissivity distribution and found the data to be consistent with a constant emissivity of 0.36 $\pm$ 0.17 K pc$^{-1}$ at 74 MHz beyond 3 kpc and zero emissivity within 3 kpc of the Galactic Centre.

The above observations require three-dimensional (3D) modelling to reveal the distribution of the Galactic magnetic field and cosmic ray electrons. There have been an ever improving set of models for one or both (Beuermann, Kanbach & Berkhuijsen 1985; Han et al. 2006; Sun et al. 2008; Sun & Reich 2010, 2012; Orlando & Strong 2013). The accuracy of any emissivity calculation is fundamentally tied to the quality of the underlying models. In total, emissivities have only been determined for $\sim$90 H II regions across the entire Galactic plane and all of these values are critical to the accuracy of models for the distributions of the magnetic field and cosmic ray electrons. In this work, which is the pilot for a larger study, we use the superb capabilities of the MWA to determine the emissivities towards 47 H II regions, making this the largest single study of this kind to date. In Section 2, we introduce our observations and methods of emissivity measurements. In Section 3, we show our measured emissivities. In Section 4, we model the emissivity distribution. In Section 5, we summarize our results and discuss future work.

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$^1$ Emissivity is the brightness temperature per unit length with the unit of K pc$^{-1}$, which is equivalent to $7.66 \times 10^{-41}$ W m$^{-3}$ Hz$^{-1}$ sr$^{-1}$ at 88 MHz in our observations.

2 MWA 88 MHz Data and Analysis

2.1 Data

We use data from the GLEAM survey: the Galactic and Extragalactic All-sky MWA survey (Wayth et al. 2015). The observations used in this study were performed for 10 h on 2014 March 17. The data reduction follows the method described in the MWA commissioning survey (Hurley-Walker et al. 2014) with more specific details discussed in Hindson et al. (2016). The main steps of data reduction include flagging, calibrating, and imaging individual snapshots. The calibrated Stokes XX and YY snapshots were imaged with a robust weighting of 0.0. To correct the astrometric changes in source position generated by the ionosphere (Lui et al. 2015), we cross-matched the position of compact sources with MRC sources (Large et al. 1981; Large, Cram & Burgess 1991) to determine an average astrometric correction and shifted each snapshot accordingly.

The GLEAM data span 72–231 MHz divided into five bands. The shortest baseline ($D_{\text{min}}$) is 7.7 m corresponding to an angular scale of 25$^\circ$ at 88 MHz (Tingay et al. 2013). The surface brightness sensitivity ranges from 50 to 100 mJy beam$^{-1}$ for the range of angular sizes from 5$^\circ$ to 15$^\circ$ (Hindson et al. 2016). In this paper, we use the data at the lowest frequency of 88 MHz with a bandwidth of 30.72 MHz to maximize H II region absorption detections. These data have a 1σ sensitivity of 99 mJy beam$^{-1}$ with an angular resolution of 5.6 arcmin $\times$ 5.6 arcmin (1 Jy beam$^{-1} = 5652.1$ K). The noise level is the lowest at Galactic longitude $\sim$300$^\circ$ and increases towards lower and higher Galactic longitudes shown in Fig. 1.

Previous single-dish surveys can recover the total power of the sky, but their angular resolutions are in the order of degrees, which is not sufficient to resolve distant or small Galactic H II regions. By contrast, the excellent angular resolution of the GLEAM survey enables the detection of H II regions with minimum sizes from 2 to 33 pc for distances from 1 to 20 kpc (Hindson et al. 2016). However, as an interferometer, the MWA is insensitive to power from large-scale structures. The MWA consists of 128 aperture arrays distributed in a dense core $<1.5$ km in diameter with a maximum baseline of about 2.5 km. Thus, MWA has excellent ($u, v$) coverage and surface brightness sensitivity to structures on angular scale from 5.6 arcmin to 31$'$ at 88 MHz, which is sufficient for our emissivity measurements with H II regions of typical angular scale sizes of several arcminutes. The observations of N06 are only sensitive to structures with angular sizes from $\sim$10 to 40 arcmin, resulting in negative temperature measurements for their observed absorption regions. Our observations also differ from N06 in spatial coverage. Our current measurements cover the southern sky in the range 250$^\circ$ $< \ell < 355^\circ$, $|b| < 2^\circ$, whereas N06 mainly covers the northern sky in the range $-15^\circ < \ell < 26^\circ$, $|b| < 5^\circ$, furthermore the work of N06 was conducted at 74 MHz, whereas the work in this paper is based on 88 MHz.

2.2 Emissivity calculations

As discussed above, H II regions become optically thick at low frequencies, absorbing the diffuse synchrotron radiation emitted behind them. An H II region whose distance is known is a valuable probe of the synchrotron emission behind and in front of it. Here, we introduce the formalism for using H II regions to determine the average emissivity along the line of sight. The quantities of foreground and background emissivity are shown in Fig. 2.

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1 Emissivity is the brightness temperature per unit length with the unit of K pc$^{-1}$, which is equivalent to $7.66 \times 10^{-41}$ W m$^{-3}$ Hz$^{-1}$ sr$^{-1}$ at 88 MHz in our observations.
Figure 1. A portion of the Galactic plane at 88 MHz with a bandwidth of 30.72 MHz observed by the MWA (Hindson et al. 2016). The angular resolution is 5.6 arcmin × 5.6 arcmin. The white polygons and yellow circles show the H II regions with detected and undetected absorption features, respectively. Several absorption regions near the top-left corner in the top panel are detected but not measured due to the overlapped H II regions with different distances. The striations in the middle of the second panel is caused by the bright Centaurus A. The black boxed region is enlarged in Fig. 3 to show an example absorption feature. Throughout we use the ‘cubehelix’ colour map (Green 2011). The colour scale is adapted to ensure the Galactic features are highlighted.

Figure 2. A schematic diagram showing a portion of the Galactic disc (grey), the Galactic Centre (GC), an H II region, the Sun, the temperatures \( T_t, T_o, T_f, T_e \), the path lengths \( D_f, D_b \), and the emissivities \( \epsilon_f, \epsilon_b \).

Similar to a single-dish telescope (Kassim 1987), we observe the H II region with a brightness temperature of

\[
T_o = T_e(1 - e^{-\tau}) + T_b e^{-\tau} + T_f, \tag{1}
\]

where \( T_e \) is the electron temperature of the H II region, \( T_b \) is the brightness temperature of the synchrotron emission from the H II region to the Galactic edge along the line of sight, \( T_f \) is the brightness temperature of the synchrotron emission from the H II region to the Sun, and \( \tau \) is the optical depth of the H II region.

Usually, H II regions become optically thick (\( \tau \gg 1 \)) at frequencies below approximately 200 MHz (Mezger & Henderson 1967). So the observed brightness temperature of the H II region becomes

\[
T_o = T_e + T_f. \tag{2}
\]

The brightness temperature of the sky neighbouring the H II region \( T_t \) is

\[
T_t = T_f + T_b. \tag{3}
\]

Defining the average emissivity as the brightness temperature per unit length, the average emissivities behind \( (\epsilon_b) \) and in front \( (\epsilon_f) \) of H II regions are

\[
\epsilon_f = T_f / D_f = (T_o - T_b) / D_f, \quad \epsilon_b = T_b / D_b = (T_t - T_o + T_e) / D_b, \tag{4}
\]

where \( D_f \) is the distance between the H II region and the Sun and \( D_b \) is the distance between the H II region and the edge of the Galactic plane. \( T_e \) and \( D_f \) are from the literature (see the references in Table 1). \( T_e \) is mainly measured from radio recombination lines at about 9 GHz (Balser et al. 2015 and reference therein). For H II regions without measured \( T_e \), we estimate from the relation between the electron temperature and the Galactocentric radius \( T_e = (4928 \pm 277) + (385 \pm 29) R_{gal} \) from Balser et al. 2015 (a similar relation is derived in Alves et al. 2012). When estimating the electron temperature using the relation in Balser et al. (2015) and Alves et al. (2012), respectively, the differences are 1–8 per cent on \( \epsilon_b \), depending on the distance of H II regions. The small differences do not change our modelling results. \( D_f \) is mainly measured using kinematics and parallax methods, which are summarized in Anderson et al. (2014). We calculate \( D_b \) assuming a Galactocentric radius of 20 kpc (Ferrière 2001 and references therein). Note that our \( \epsilon_b \) depends on this assumed Galactocentric radius. \( T_o \) and \( T_t \) are from our observations.
Table 1. Emissivity measurements for H II regions with absorption features.

<table>
<thead>
<tr>
<th>WISE name</th>
<th>$I_p$</th>
<th>$I_{p}$</th>
<th>$T_p$</th>
<th>$D_p$</th>
<th>$T_{p}$</th>
<th>$D_{p}$</th>
<th>$e_p$</th>
<th>$Q$</th>
<th>Ref.</th>
</tr>
</thead>
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<tr>
<td></td>
<td>Jy beam$^{-1}$</td>
<td>Jy beam$^{-1}$</td>
<td>$\times 10^4$ K</td>
<td>kpc$^{-1}$</td>
<td>$\times 10^4$ K</td>
<td>K pc$^{-1}$</td>
<td>K pc$^{-1}$</td>
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<tr>
<td>G332.70+00.783</td>
<td>1.49 ± 0.29</td>
<td>3.30 ± 0.29</td>
<td>0.84 ± 0.16</td>
<td>1.87 ± 0.16</td>
<td>3.7 ± 0.4</td>
<td>7.33 ± 0.33</td>
<td>0.3 ± 0.4</td>
<td>0.04 ± 0.22</td>
<td>0.39 ± 0.08</td>
</tr>
<tr>
<td>G332.64+00.514</td>
<td>2.35 ± 0.29</td>
<td>3.30 ± 0.29</td>
<td>1.33 ± 0.16</td>
<td>1.87 ± 0.16</td>
<td>3.0 ± 0.4</td>
<td>7.33 ± 0.33</td>
<td>0.3 ± 0.4</td>
<td>0.04 ± 0.22</td>
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<td>0.04 ± 0.22</td>
<td>0.39 ± 0.08</td>
</tr>
</tbody>
</table>

Notes. (1) the name of H II regions from the WISE H II region catalogue. (2) and (3) the MWA surface brightness measurements of the absorbing H II region and the neighbouring region, respectively. Cols (4) and (5): the brightness temperatures of the absorbing H II region and the neighbouring region, respectively. Cols (6): the distance from H II regions to the Sun found in the literature. Cols (7): the electron temperature of H II regions from the literature. Cols (8): the average emissivity from H II regions to the Sun. Cols (9): the average emissivity from H II regions to the Galactic edge. Cols (10): the indicative quality of emissivity measurements: a higher value means higher quality (see Section 3.1). Cols (11): the references for the distances and electron temperatures. The first and second number indicate the reference for the distance in Col. (6) and the electron temperature in Col. (7), respectively. The reference list: 1. Anderson et al. (2014); 2. Balser et al. (2015); 3. Caswell & Haynes (1987); 4. García et al. (2014); 5. Hou & Han (2014); 6. Nord et al. (2006); 7. Paladini, Davies & De Zotti (2004); 8. Quirosa et al. (2006); 9. Reid et al. (2014).

*The electron temperature of this H II region is derived from the statistical relation $T_e = (4928 \pm 277) \times (385 \pm 29) R_{H}$ from Balser et al. (2015).

Unlike a single-dish telescope, an interferometer is incapable of measuring the total power of the Galactic plane emission. The data miss an unknown background offset across a large sky area, resulting in ~70 per cent error in the absolute level of the measurements. As a result, our measurements of $e_p$ have an additive offset or a scaling error and are not absolutely correct (equation 4). However, they are relatively correct because the missing power on scales less than a few degrees is absent equally from $T_p$ and $T_{p}$, so the difference
Figure 3. An example of H II region (G331.365+00.521) absorption feature at 88 MHz from the MWA (left) and an emission feature at 12 µm from WISE (right). The white solid and dashed lines show our defined absorption and neighbouring regions, respectively. See Section 2.3 for the rules for selecting the absorbed and neighbouring regions. The red circle shows this H II region defined in the WISE H II region catalogue. The blue circle in the left corner shows the FWHM of the synthesized beam. The root mean square of this H II region in this MWA image is about 0.26 Jy beam⁻¹. This entire field is marked by a square in Fig. 1.

\[ T_e - T_o = \epsilon \lambda \] (equation 4) is correct. However, because \( \epsilon \) relies only on \( T_o \), which is not absolutely calibrated, we will not use \( \epsilon \) in our modelling.

It should be noted that the above formulae differ from those used by N06 because the MWA recovers the large-scale background emission to a scale of \( \sim \lambda / D_{\text{min}} \approx 25' \) surrounding the H II regions, whereas N06’s observations do not.

2.3 H II region selection criteria

In this paper, we work with a sample of H II regions with known distances and obvious absorption features to measure the average emissivities along a path. Using the 12 and 22 µm data with high angular resolutions of 6.5 and 12 arcsec, respectively, from the Wide-field Infrared Survey Explorer (WISE), Anderson et al. (2014) constructed a catalogue of \( \sim 8000 \) Galactic H II regions. This WISE H II region catalogue constrains each H II region within a radius. To select our sample, we search for absorption regions within these radii. We omitted overlapping H II regions with different distances in our sample due to the complexity in obtaining reliable average emissivities. Note that Hindson et al. (2016) have presented a catalogue of 306 H II regions using the data with all the frequencies between 72 and 231 MHz from the MWA GLEAM survey. We do not use this catalogue because most of their measurements do not show obvious absorption features, and they did not publish the part of the sky closer to the Galactic Centre.

We define absorption regions such that they are each:

(i) inside the radius defined in the WISE H II region catalogue;
(ii) lower than the nearby \( T_\text{e} \) by at least 3\sigma in surface brightness;
(iii) larger than the beam size to avoid beam dilution;
(iv) coincident with 12 µm emission features in the WISE observations (Wright et al. 2010) given the 12 µm emission is mainly from polycyclic aromatic hydrocarbon (PAH) molecules, which traces ionization fronts. The 22 µm emission traces small dust grains composing the inner core of an H II region (see Deharveng et al. 2010; Anderson et al. 2014 and reference therein). Thus, we expect the 12 µm emission region to be coincident with the absorption feature caused by free electrons from ionization, whereas the 22 µm emission region is much smaller than the absorption feature.

For each absorption feature, we choose a nearby, non-absorbed area to estimate \( T_e \) such that the area:

(i) is located in the similar Galactic latitude as the absorption region given the brightness temperature decreases rapidly with latitude;
(ii) does not overlap with any H II region in the WISE H II region catalogue;
(iii) does not overlap with any supernova remnants listed by Green et al. (2015) to avoid contamination from bright non-thermal emission in our observations;
(iv) does not have an obvious coherent structure, in order to avoid the effects caused by unknown sources, such as the undetected H II regions and supernova remnants.

We show an example of an absorption region and a neighbouring region in Fig. 3. We confirm that the low surface brightness region in the centre of the MWA image (Fig. 3, left) is from H II region absorption by comparing with the WISE image (Fig. 3, right). The WISE image is constructed by stacking 15 facets and then cropped to the same size as the MWA image. The line-like features are edges of image facets. These features do not have an effect on determining the location of the H II region.

3 NEW EMISSIVITY MEASUREMENTS

3.1 The emissivity distribution

We use equation (4) and the MWA measurements of \( T_e \) and \( T_o \) to estimate the average emissivities both behind and in front of 47 H II regions (see Table 1). We find that all average emissivities between the H II regions and the Galactic edge along the line of sight (\( \epsilon_\text{b} \)) are in the range of \( 0.39 \sim 1.45 \) K pc⁻¹ with an average of \( 0.77 \) K pc⁻¹ and a variance of \( 0.14 \) K pc⁻¹. The average...
emissivities between the H II regions and the Sun ($\epsilon_j$) have a large range of 0.01 to $8.93$ K pc$^{-1}$ with a mean of 2.6 K pc$^{-1}$ and a variance of 2.0 K pc$^{-1}$, although these are subject to an uncertainty in total power affecting $\epsilon_j$.

We estimate the local root mean square (rms) noise for the measured surface brightness ($I$) using the standard deviation of pixel values in a representative neighbouring region. To incorporate the uncertainty in the distance measurement used in each H II region, we proceed as follows: (i) where an error is explicitly stated in the literature this is used verbatim; (ii) where no error has been quoted, then H II regions with parallax distance measurements are assigned a 10 per cent error; (iii) H II regions with a kinematic distance measurement are assigned a 50 per cent error; and (iv) for all other cases, including H II regions without a specified distance measurement method, we assign an error of 100 per cent. The errors of the electron temperature ($T_e$) of H II regions are from the literature. Each above error is propagated to the average emissivities ($\epsilon_j$ and $\epsilon_b$). All the quoted errors are 1σ.

The magnitude of any extragalactic synchrotron emission is negligible compared with Galactic synchrotron since its brightness temperature is in the range from 195 to 585 K at 88 MHz which is only ~2 per cent of the Galactic component (Guzmán et al. 2011 and references therein). Its effect (~0.03 K pc$^{-1}$) on our measurements is smaller than our minimum error (0.05 K pc$^{-1}$) and much smaller than our average error (0.14 K pc$^{-1}$).

We give an indicative quality number to each measurement as a means of judging reliability (Table 1, Column 10). The quality number is the number of matched conditions below, maximum value of 6 means all conditions met:

(i) The H II region is isolated and does not overlap with other H II regions.
(ii) The H II region belongs to a ‘known’ H II region group, as defined in the WISE H II region catalogue (Anderson et al. 2014). ‘Known’ H II regions are associated with radio recombination lines or H$_\alpha$ emission; they are confirmed H II regions, unlike ‘group’ and ‘candidate’ H II regions.
(iii) The area of the absorption region is at least two times larger than the beam size.
(iv) The location of the absorption feature corresponds well with that of the WISE 12 µm emission feature (Wright et al. 2010). We use this criterion because the lowest temperature region in some absorption features has a positional or dimensional offset compared with the brightest emission feature in WISE.
(v) The distance of the particular H II region is measured rather than assuming it has the same distance as any other associated H II regions.
(vi) The electron temperature of the H II region is measured rather than calculated from the statistical relation in Balser et al. (2015).

Fig. 4 shows the emissivity ($\epsilon_j$) distribution along different lines of sight. Our measured emissivities increase rapidly with respect to Galactic longitude (Fig. 5, left). This is coincident with the total line-of-sight emissivity distribution, which can be seen in Fig. 6. The emissivity over the line of sight excluding point sources and supernova remnants decreases obviously with respect to Galactic longitude from 355° to 250°. Our measured emissivities are relatively high measured from H II regions with high Galactic latitude and relatively low derived from H II regions with low Galactic latitude (Fig. 5, right). This plot possibly reflects the decreasing of emissivity with the distance to the Galactic plane (Peterson & Webber 2002), although our detections are limited in the range of the Galactic latitude from $-1°$ to $2°$.

Similar variations are also found in other surveys, e.g. the 408 MHz Haslam map (fig. 4 in Haslam et al. 1982). The intensity profiles along Galactic longitude and latitude are well fitted by three magnetic field models in Sun et al. (2008) and Sun & Reich (2010).

3.2 Comparison with the literature

According to the brightness temperature spectrum $T(v) \propto v^{-2.3}$ (Guzmán et al. 2011) and the typical emissivity of 0.01 K pc$^{-1}$ (Beuermann et al. 1985) at 408 MHz (Haslam et al. 1982), the typical emissivity at 88 MHz is expected to be 0.34 K pc$^{-1}$. The mean of our measured emissivity ($\epsilon_j$) of 0.77 K pc$^{-1}$ with a variance of 0.14 K pc$^{-1}$ agrees within 3σ with this estimation.

To check for any systematic differences between the samples, we compare the measurements for three H II regions that appear both in our sample and N06, in Table 2. Using the same distances and electron temperatures as listed in N06, and scaling our measurements from 88 to 74 MHz using a brightness temperature spectral index of 2.3 ($T_e \propto v^{-2.3}$, Guzmán et al. 2011), our measurements agree within 1σ for the H II region G348.6–0.6. Our measurements are higher than those in N06 for H II regions G351.5–0.5 and G348.7–1.0, with a 3σ discrepancy. The disparity may be caused by the improved angular resolution of the MWA, which reduces the beam dilutions, leading to better measurements of surface brightness differences between the absorbed and neighbouring regions (see Marr, Snell & Kurtz 2015 for beam dilution). For example, the angular diameter of H II region G348.7–1.0 is 4.47 arcmin, whereas the resolution element in N06 for this observation field is 8.33 arcmin × 5.00 arcmin, leading to a beam dilution factor of just over 2. The emissivity of 0.36 ± 0.05 K pc$^{-1}$ at 74 MHz in N06 would be 0.75 ± 0.10 K pc$^{-1}$ after correction for beam dilution, which agrees well with our measured emissivity 0.68 ± 0.13 K pc$^{-1}$ (scaled to 74 MHz).

3.3 Non-detections and detection bias

About 80 H II regions with radii larger than the beam size and smaller than the maximum angular scale sensitivity are not detected as absorption regions in the region we analyse (Fig. 1). A possible reason is that not enough synchrotron emission exists behind these H II regions; an absorption feature is only apparent when the integrated brightness temperature blocked by an H II region is larger than its electron temperature (see equations 2 and 3). As shown in Fig. 1, all of our 47 detections are in the range of 315° < $l$ < 355°, whereas only 25 non-detections are in this range. The other 55 non-detections are in the low brightness temperature region with the range of 250° < $l$ < 315°, which might be detectable in emission at higher frequencies and these will be followed up in future. Two other possibilities of non-detections are a high electron temperature and/or a low optical depth for these H II regions.

Note that we assume H II regions associated with absorption features have an optical depth much larger than one. In future, the work will use the MWA GLEAM survey coverage 72–231 MHz to measure the optical depth and confirm this hypothesis.

Finally, our emissivity measurements do not sample the whole Galactic disc uniformly mainly due to the non-uniform distribution of H II regions. Most of the observed H II regions are nearby, with distances of several kiloparsecs. The H II regions with large distances usually have large distance uncertainties, resulting in large emissivity uncertainties.
Figure 4. Distribution of emissivities ($\epsilon_b$) on lines of sight and the two-circle model. Each colour represents a path over which the emissivities are averaged. The colours of the lines indicate the value of emissivities along different paths. The Galactic non-thermal emission is assumed to lie in a disc with a Galactocentric radius of 20 kpc shown by the grey circle segment. The two circles near the Galactic Centre divide the Galactic plane into three regions with emissivities of $\epsilon_1$, $\epsilon_2$, and $\epsilon_3$, respectively. The Galactocentric radius of the Sun is 8.5 kpc. The Sun and Galactic Centre (GC) are marked as a black dot and plus, respectively.
Figure 5. Distributions of emissivities ($\epsilon_b$) with respect to Galactic longitude (left) and latitude (right). Some measurements have large errors due to the uncertainty of the distances of H II regions.

Figure 6. Distributions of emissivity from the Sun to the Galactic edge over the line of sight with respect to the Galactic longitude in the range $250^\circ < l < 355^\circ$, $|b| < 3^\circ$: this includes the contributions from point sources and supernova remnants. The bin size in Galactic longitude is 3.75 arcmin. There is a trend of increasing emissivity with longitude. The high emissivity near the Galactic longitude $264^\circ$ is contributed by the Vela supernova remnant. Note that we do not recover the total power of the Galaxy due to the interferometric nature of the measurements.

4 MODELLING THE EMISSIVITY DISTRIBUTION

The measured emissivities need modelling to show the emissivity distribution with respect to the Galactic radius. We build four simple models to probe this complex problem.

The synchrotron emissivity is the power per unit volume per unit frequency per unit solid angle produced by cosmic ray electrons interacting with the magnetic field. Since we can only measure the average emissivity along paths, we adopt four simple models: uniform; Gaussian; exponential; and two-circle to fit the emissivity distribution of the Galaxy. We fit our measured $\epsilon_b$ using these models. We test the uniform model given that N06 found a constant emissivity outside of a circular region centred at the Galactic Centre with a radius of 3 kpc. The exponential model is motivated by the exponential cosmic ray electron distribution used in Sun et al. (2008). The Gaussian model is an alternative form to express a decreasing emissivity profile from the Galactic Centre. The two-circle model is constructed with more free parameters and to specifically account for the high emissivities found for regions with paths close to the Galactic Centre.

Before showing details of each model, we define $R_0$ to be the Galactocentric radius of the Sun, $R$ to be the Galactocentric radius of any point on the Galactic plane, $d$ to be the distance from an H II region to the Sun, $f$ to be the Galactic longitude, $\alpha$ and $\beta$ to be free parameters related to the Gaussian and exponential models.

The uniform model assumes a constant emissivity distribution across the Galactic disc.

Table 2. Comparison of three emissivities measured in N06 and this work.

<table>
<thead>
<tr>
<th>H II region (this work)</th>
<th>G351.516−00.540</th>
<th>G348.710−01.044</th>
<th>G348.691−00.826</th>
</tr>
</thead>
<tbody>
<tr>
<td>H II region (N06)</td>
<td>G351.5−0.5</td>
<td>G348.7−1.0</td>
<td>G348.6−0.6</td>
</tr>
<tr>
<td>Distance (kpc, used in N06)</td>
<td>3.3</td>
<td>2.0</td>
<td>2.7</td>
</tr>
<tr>
<td>$T_e (\times 10^3$ K, used in N06)</td>
<td>5.7 ± 1.0</td>
<td>6.2 ± 1.0</td>
<td>4.8 ± 1.0</td>
</tr>
<tr>
<td>Angular diameter (arcmin, used in N06)</td>
<td>3.46</td>
<td>4.47</td>
<td>13.27</td>
</tr>
<tr>
<td>$\epsilon_b$ (K pc$^{-1}$, at 74 MHz, N06)</td>
<td>0.36 ± 0.06</td>
<td>0.36 ± 0.05</td>
<td>0.51 ± 0.05</td>
</tr>
<tr>
<td>$\epsilon_b$ (K pc$^{-1}$, at 74 MHz, N06, corrected for beam dilution)</td>
<td>1.24 ± 0.21</td>
<td>0.75 ± 0.10</td>
<td>0.51 ± 0.05</td>
</tr>
<tr>
<td>$\epsilon_b$ (K pc$^{-1}$, scaled at 74 MHz, this work)$^*$</td>
<td>0.85 ± 0.16</td>
<td>0.68 ± 0.13</td>
<td>0.48 ± 0.16</td>
</tr>
</tbody>
</table>

$^*$To compare our measurements with those in N06, we re-calculate our emissivities for these three H II regions using the distances and electron temperatures from N06 and scale our measurements from 88 to 74 MHz using a brightness temperature spectral index of 2.3.
Table 3. Parameters from fitting the measured emissivities with four models: uniform, Gaussian, exponential, and two-circle model.

<table>
<thead>
<tr>
<th>Model</th>
<th>Free parameters</th>
<th>$\chi^2_{\text{red}}$</th>
<th>Degrees of freedom</th>
</tr>
</thead>
<tbody>
<tr>
<td>Uniform</td>
<td>$\epsilon = 0.64 \pm 0.10$</td>
<td>5.90</td>
<td>46</td>
</tr>
<tr>
<td>Gaussian</td>
<td>$\alpha_1 = 1.8^{+1.8}<em>{-1.0}, \beta_1 = 5.6^{+\infty}</em>{-1.0}$</td>
<td>5.26</td>
<td>45</td>
</tr>
<tr>
<td>Exponential</td>
<td>$\alpha_2 = 2.8^{+3.8}<em>{-2.0}, \beta_2 = 0.20^{+0.20}</em>{-0.20}$</td>
<td>4.95</td>
<td>45</td>
</tr>
<tr>
<td>Two-circle</td>
<td>$R_1 = 1.7^{+0.2}<em>{-0.3}, R_2 = 5.2^{+4.8}</em>{-3.2}$</td>
<td>2.95</td>
<td>42</td>
</tr>
<tr>
<td></td>
<td>$\epsilon_1 = 8.2^{+5.3}<em>{-3.5}, \epsilon_2 = 0.84^{+0.76}</em>{-0.55}, \epsilon_3 = 0.51^{+0.19}_{-0.27}$</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Notes. The unit of $\epsilon, \epsilon_1, \epsilon_2, \epsilon_3, \alpha_1$, and $\alpha_2$ is K pc$^{-1}$. The units of $R_1, R_2$, and $\beta_1$ is kpc. The unit of $\beta_2$ is kpc$^{-1}$. All the quoted errors are at 2σ level. The Gaussian model tends to the uniform model when $\beta_1$ tends to infinity.

Figure 7. Triangle plot showing the correlations between the two-circle model parameters: the grey-scale traces the distributions of chi-square with darker regions indicating lower values. The 2σ boundaries of chi-square are shown by white contours. The black solid lines show the relative likelihood distributions with dashed lines showing the best values and 2σ limits of the parameters.

In the Gaussian model, the emissivity is assumed to have a distribution $\epsilon(R) = \alpha_1 \exp(-R^2/2\beta_1^2)$. We assume the emissivity peaks at the Galactic Centre. $R$ is a function of the distance $d$, so the emissivity $\epsilon$ is also a function of $d$. The average emissivity from the H$\pi$ region to the Galactic edge is the integration of $\epsilon(d)$ for $d$ and then divided by the corresponding path length.

The exponential model has an emissivity distribution in the form of a natural exponential function $\epsilon(R) = \alpha_2 \exp(-\beta_2 R)$.

The method of calculating the average emissivities along the line of sight from this model is the same as that in the Gaussian model.

We also develop a simple two-circle model motivated by the data. In this model, we divide the Galactic plane into three regions using two circles centring on the Galactic Centre. $R_1$ and $R_2$ ($R_1 < R_2$) is the radius of circle 1 and circle 2, respectively. $\epsilon_1$ is the emissivity in circle 1. $\epsilon_2$ is the emissivity in the region between circle 1 and
circle 2. $\epsilon_3$ is the emissivity in the region outside circle 2 and within the Galactic edge (see Fig. 4).

With the assumptions in each model, we determine the free parameters by fitting the observed emissivities ($\epsilon_b$) and those from the model using the (reduced) chi-squared test (e.g. Andrae, Schulze-Hartung & Melchior 2010) to compare the goodness of fit of the models. We did not fit the average emissivities from H II regions to the Sun, since they are not absolutely reliable as mentioned in Section 2. We sample the whole parameter spaces and find the minimum of chi-squares for each model. We use the boundary of fixed $\Delta \chi^2 (2\sigma)$ to estimate the quoted errors. We project the full $M$-dimensional ($M = 2, 5$) confidence region on the one-dimensional confidence interval for each parameter.

The results of modelling are shown in Table 3. The uniform model shows an average emissivity of $0.64 \pm 0.10$ K pc$^{-1}$ with a poor reduced chi-square ($\chi_{\text{red}}^2 = 5.90$). The Gaussian and Exponential models have similarly poor fits ($\chi_{\text{red}}^2 \sim 5.26$ and 4.95). The Two-circle model has the best performance compared with the other three models ($\chi_{\text{red}}^2 = 2.95$). It shows a high emissivity ($8.2^{+4.5}_{-2.8}$ K pc$^{-1}$) region near the Galactic Centre within a radius of $1.7^{+0.5}_{-0.3}$ kpc, a low emissivity ($0.51^{+0.29}_{-0.22}$ K pc$^{-1}$) region outside of a radius of $5.2^{+3.2}_{-3.2}$ kpc, a medium emissivity ($0.84^{+0.76}_{-0.55}$ K pc$^{-1}$) region between the two. In Fig. 7, we show the correlations between the parameters for the two-circle model. We see that in the $2\sigma$ contour of chi-square, a lower $R_1$ corresponds to a higher $\epsilon_1$, but when $R_1$ is lower than about 1.3 kpc, $\epsilon_1$ does not increase further. Similarly, a higher $R_2$ cannot give a lower $\epsilon_2$ when $R_2$ exceeds about 6 kpc. In the sub-plot $R_2: \epsilon_3$, $R_2$ is fixed to be higher than 1 kpc since it cannot be less than $R_1$. The $2\sigma$ errors for each parameter in the two-circle model are large due to the correlations between the parameters, and fundamentally due to the limited number of measurements, and because most of the H II regions are nearby; those that are more distant have large error bars on their distance measurements, reducing their importance during the fitting process. If we fix the parameters $R_1$ and $R_2$ to be the best values from our modelling, the errors of other parameters are reduced: $\epsilon_1 = 8.2^{+4.5}_{-2.8}$ K pc$^{-1}$, $\epsilon_2 = 0.84^{+0.33}_{-0.35}$ K pc$^{-1}$, and $\epsilon_3 = 0.51^{+0.14}_{-0.16}$ K pc$^{-1}$. Our best-fitting $R_1$ of the innermost circle includes the brightest Galactic Centre region. Potentially showing a physical correlation, the region between the best-fitting $R_1$ and $R_2$ includes several spiral arms, e.g. the 3-kpc ring, the Sagittarius arm, and the Norma arm. The large region outside of the outer most circle only contains the Scutum-Centaurus arm and the McClure-Griffiths arm (McClure-Griffiths et al. 2004).

Fig. 8 compares the models in more detail where it can be seen that none provide a good fit to the four measurements with short path lengths (14–16 kpc). However, all models similarly

Figure 8. Distributions of emissivities ($\epsilon_b$) from our measurements and models with the path length from H II regions to the Galactic edge along the line of sight.
account for the measurements with longer path lengths (18–26 kpc). The main differences among models appear at the path length above 26 kpc, where there are several high average emissivities. These high emissivities pass the region near the Galactic Centre. Only the two-circle model, which has additional free parameters, can recover these high emissivities (8.2^{+5.3}_{-2.5} K pc^{-1}) near the Galactic Centre.

Furthermore, the two-circle model can explain the low emissivity along the total lines of sight towards Galactic longitude between 270° and 320° (Fig. 6). The brightness temperature in these directions is significantly lower compared with that in other directions in Fig. 1.

N06 determined the best-fitting model with uniform emissivity between 3 and 20 kpc and zero within 3 kpc of the Galactic Centre. However, this model does not fit our data better than any of our models. Our best-fitting two-circle model shows the highest emissivity near the Galactic Centre, contrary to N06 but quite likely due to sampling bias: our work samples regions in the fourth quadrant, whereas N06’s sample region is mainly in the first quadrant; three of their measurements overlap with ours. Their measured emissivities are lower when the paths are closer to the Galactic Centre, whereas ours are opposite, driving our model fits to increase the emissivity near the Galactic Centre. Note that both of these two observations probe 2–3 kpc nearby the Galactic Centre but no detection is closer to the Galactic Centre. The modelling in Sun et al. (2008) suggested a high magnetic field strength and the free electron model in NE2001 (Cordes & Lazio 2002) suggested a high free electron density near 2–3 kpc of the Galactic Centre. These results support our conclusions.

Note that our four simplified models are only initial tests for the complex emissivity distribution. Our models have limited power to fully describe our measurements, not to mention other surveys at different frequencies. To understand the Galactic physical structures, we need to analyse our measurements and other survey data coherently using comprehensive models developed by Sun et al. (2008), Sun & Reich (2010), Orlando & Strong (2013), etc.

5 SUMMARY AND FUTURE WORK

We measured emissivities from 47 H II regions along the two paths and in front of H II regions. These measurements show the radial dependence of emissivity distribution. The modelling of these measurements shows a high emissivity region near the Galactic Centre and low emissivities near the Galactic edge.

In future, data covering two-thirds of the Galactic plane will be accessible through the GLEAM survey and we expect to derive new measurements from about 200 H II regions. We will take advantage of the data in all five frequency bands of the GLEAM survey to derive the emissivity spectrum. A 3D emissivity map, combining these discrete measurements and the total line-of-sight emissivity distributions, will show more details of the Galactic structures with the help of existed comprehensive 3D models. We may set a length-scale on cosmic ray electron propagation by comparing the possible cosmic ray source distribution and emissivity distribution. Possibly, we can derive the cosmic ray electron distribution with an assumed Galactic magnetic field distribution, and vice versa.

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