A complete distribution of redshifts for sub-millimetre galaxies in the SCUBA-2 Cosmology Legacy Survey UDS field

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ABSTRACT
Sub-millimetre galaxies (SMGs) are some of the most luminous star-forming galaxies in the Universe, however their properties remain hard to determine due to the difficulty of identifying their optical/near-infrared counterparts. One of the key steps to determining the nature of SMGs is measuring a redshift distribution representative of the whole population. We do this by applying statistical techniques to a sample of 761 850 \(\mu\)m sources from the SCUBA-2 Cosmology Legacy Survey observations of the UKIDSS Ultra-Deep Survey (UDS) Field. We detect excess galaxies around \(> 98.4\) per cent of the 850 \(\mu\)m positions in the deep UDS catalogue, giving us the first 850 \(\mu\)m selected sample to have virtually complete optical/near-infrared redshift information. Under the reasonable assumption that the redshifts of the excess galaxies are representative of the SMGs themselves, we derive a median SMG redshift of \(z = 2.05 \pm 0.03\), with 68 per cent of SMGs residing between 1.07 < \(z\) < 3.06. We find an average of 1.52 ± 0.09 excess \(K\)-band galaxies within 12 arc sec of an 850 \(\mu\)m position, with an average stellar mass of \(2.2 \pm 0.1 \times 10^{10} \, M_\odot\). While the vast majority of excess galaxies are star-forming, 8.0± 2.1 per cent have passive rest-frame colours, and are therefore unlikely to be detected at sub-millimetre wavelengths even in deep interferometry. We show that brighter SMGs lie at higher redshifts, and use our SMG redshift distribution – along with the assumption of a universal far-infrared SED – to estimate that SMGs contribute around 30 per cent of the cosmic star formation rate density between 0.5 < \(z\) < 5.0.

Key words: galaxies: high-redshift, star-formation, submillimetre: galaxies

1 INTRODUCTION
Sub-millimetre wavelengths are well-suited to studying high redshift galaxies, since redshift effects combine with the steep Rayleigh-Jeans tail of the dust spectral energy distribution resulting in negative \(K\)-corrections. This ensures that galaxies of a fixed far-infrared luminosity (a proxy for star-formation rate) are approximately equally bright from \(z = 1\) out to \(z = 6\) (e.g. Blain et al. 2002).

The low resolution of sub-millimetre observations with even the most widely-used cameras – the Sub-millimetre Common-User Bolometer Array (SCUBA Holland et al. 1999) on the 15m James Clerk Maxwell Telescope, and the Large APEX Bolometer Camera (LABOCA; Siringo et al. 2009) on the APEX 12m telescope – and high redshift nature of sub-millimetre galaxies (SMGs), make identifying their counterparts (i.e. the sources responsible for the submillimetre emission) challenging (e.g. Ivison et al. 2007), particularly in deep optical observations. While the tight far-infrared radio correlation (e.g. Helou et al. 1985; Yun et al. 2001; Jarvis et al. 2010; Smith et al. 2014), and low sky density of radio sources (e.g. Condon et al. 2012), allow the unambiguous identification of many SMG counterparts using high-resolution radio observations (e.g. Ivison et al. 2002, 2005, 2007), this is still a challenging undertaking, despite the current availability of sensitive radio data over degree-scale fields. This means that the most fundamental requirement for inferring the properties of SMGs – their redshift distribution – is hard to measure (e.g. Smail et al. 2002). Chapman et al. (2005) obtained spectroscopic redshifts to 73 SMGs based on following up 98 out of 104 radio-identified SMGs in a parent sample of 150 > 3\(\sigma\) SCUBA 850 \(\mu\)m sources, while Wardlow et al. (2011) were able to robustly identify only 72 out of 126 SMGs (an identification rate of 57 per cent) detected in LABOCA observations of the ECDFS field, using a combination of radio, 24 \(\mu\)m and Spitzer IRAC data. Recent advances have improved matters, even the latest methods (e.g. the “tri-colour” technique put forward by Chen et al. 2016) can identify reliable
counterparts to only 69 ± 16 per cent of SMGs. This means that, although SMGs are undoubtedly some of the most rapidly star-forming systems in the Universe (e.g. Hayward et al. 2011, 2013a), optical/near-infrared studies of their counterparts and therefore redshifts have so far been incomplete.

At the same time, several studies had attempted to complete the redshift distribution of SMGs using longer wavelengths, for example Koprowski et al. (2014), Koprowski et al. (2016) and Michałowski et al. (2017), which used an average SMG template from Michałowski et al. (2010) to find the redshift giving the best fit to the far-infrared/millimetre photometry. Of course, the redshifts produced using long wavelengths are in general less accurate than those produced from optical/near-infrared data (although the latter are also highly uncertain at the highest redshifts). There are several reasons for this: for example that far-infrared data are susceptible to the influence of the choice of dust SED, and are subject to errors arising from blended far-infrared photometry (e.g. Scudder et al. 2016, although – as in the aforementioned studies – this may be mitigated using deblending techniques such as those from Merlin et al. 2015 or Hurley et al. 2017). On the other hand, this method of redshift estimation does benefit from not requiring an optical/near-infrared counterpart, is able to obtain individual redshifts for every source, and is also potentially less susceptible to the influence of chance alignments between optical sources, e.g. lensing.

Given the low-resolution of sub-millimetre data based on single-dish observations, interferometers have an important role to play for studying SMGs. Some of the first results using sensitive data from the Atacama Large Millimetre Array (ALMA) to identify the counterparts to SMGs by Hodge et al. (2013) showed using a combination of radio and mid-IR data that ~ 80 per cent of SMGs are identified correctly, but with completeness of just 45 per cent. Interferometry has also shown that many SMGs have multiple counterparts; while Barger et al. (2012) found that 37.5 per cent of bright SMGs are multiples (albeit with a 1σ confidence interval between 17-74 per cent), Hodge et al. (2013) found that at least 35 per cent of SMGs are multiples, while Chen et al. (2013) used the SMA to determine a lower multiple fraction of 12.5±6.8 per cent, and this value is likely to be affected by the sample selection (e.g. the flux limit). Multiplicity is also a key parameter if we are to clarify the role of SMGs within current models of galaxy formation and evolution, however it presents considerable challenges for traditional cross-identification efforts (e.g. using likelihood ratio methods Wolfstengroft et al. 1986; Sutherland & Sanders 1992; Smith et al. 2011; Fleuren et al. 2012). The properties of SMGs are therefore still under investigation, using both observations (e.g. with large amounts of time allocated to observe the source counts and multiplicity with the Atacama Large Millimetre Array, ALMA; Hodge et al. 2013; Karim et al. 2013; Carniani et al. 2015; Simpson et al. 2015; Fujimoto et al. 2016; Oteo et al. 2016; Dunlop et al. 2017), and simulations (e.g. can theory produce sufficiently star forming galaxies, or are chance alignments required? Davé et al. 2010; Hayward et al. 2013b; Cowley et al. 2015; Muñoz Arancibia et al. 2015).

New technology used by the Sub-millimetre Common User Bolometer Array 2 (hereafter SCUBA-2; Holland et al. 2013) has given us unprecedented mapping speed at these wavelengths, meaning that we can now efficiently survey large areas. As a result, the SCUBA-2 Cosmology Legacy Survey (CLS; Geach et al. 2017), has surveyed ~5 deg² to better than mJy depth, increasing the total known sample of 850 μm sources by an order of magnitude. The extensive efforts to cross-identify these sources at these wavelengths highlights that they are critical if we are to understand the properties of SMGs, and their high-redshift, dusty nature means that the K band data in the UKIDSS Ultra-Deep Survey (Hartley et al. 2013) are ideal for this purpose. With sensitive ancillary data covering the rest-frame UV, optical and near-infrared (UVOIR) bands, we can also estimate the redshifts and stellar masses of possible counterparts, as well as classify them on the basis of their rest-frame colours. Williams et al. (2009) identified regions in the rest-frame (U − V) vs (V − J) – hereafter “UVJ” – space thought to contain predominantly passive and star-forming galaxy populations, and this method is widely used (e.g. Whitaker et al. 2012; Hatch et al. 2014; Leja et al. 2015; Mendel et al. 2015; Rees et al. 2016; Fumagalli et al. 2016).

In this paper we statistically study the optical/near-infrared properties of galaxies around the positions of a large sample of sub-millimetre sources taken from the CLS, Wardlow et al. (2011) and Simpson et al. (2014) made attempts to statistically identify those SMGs that could not be cross-identified using other means in the ECDF-S field, however the ancillary data in those works were not deep enough to detect counterparts to the full SMG sample (while the former work detected counterparts to 85 per cent of their SMG sample, the latter found only 0.61 ± 0.07 counterparts per ALMA blank SMG). Given the availability of the largest samples of sub-millimetre positions from the CLS, and the deepest K-band data from the UDS, we now extend this idea to infer the properties of the whole 850 μm-selected sample, complementary to the aforementioned long-wavelength estimates of the complete SMG redshift distribution most recently by Michałowski et al. (2017).

In section 2 we introduce the data sets used in our analysis, and explain how our sample was selected, while section 3 contains our results, which we discuss in section 4, before concluding with section 5. We adopt a standard cosmology with ΩM = 0.3, ΩΛ = 0.7, H0 = 71 km s⁻¹ Mpc⁻¹, while all magnitudes and colours are quoted on the AB system (Oke & Gunn 1983).

2 DATA AND SAMPLE SELECTION

We base our analysis on the 850 μm data from the CLS observations of the UKIDSS UDS field. The CLS 850 μm data reduction is described in Geach et al. (2017), and the UDS field is centred on α = 02°17′46″, δ = −05°05′15″ (J2000), covering an area of 0.8 deg² with a median RMS ~0.88 mJy beam⁻¹. We use the catalogue of SMGs in the CLS-UDS maps from Geach et al. (2017), which contains 1,088 SMGs detected at > 3.5σ.

The UDS data release 8 (Hartley et al. 2013) has a 5σ depth of K = 24.6 within 2-arcsec apertures over a field of 0.8 deg². Over the central 0.6 degree² of this field, the DR8 catalogue includes matched photometry in the UVBRI′z′JHK, 3.6 μm and 4.5 μm bands (measured using the method in Simpson et al. 2012), ideal for estimating galaxy colours. We use the high quality (Δz/ (1 + z) ~ 0.031) photometric redshifts from Hartley et al. (2013), alongside stellar mass estimates and rest-frame colours estimated using the FAST code (Kriek et al. 2009), which will be fully described in Smith et al. (in preparation). We derive these assuming an initial mass function from Chabrier (2003), based on the stellar SEDs from Bruzual & Charlot (2003), with exponentially declining star formation histories, a range of metallicities (0.2 < Z/Z⊙ < 2.5), a range of 0.0 < ΛV < 5.0 (assuming a dust law from Calzetti et al. 2000), and correcting for extinction in our own galaxy. Rest-frame colours for galaxies are estimated by convolving the best-fit BC03 spectra found by FAST with the Bessel
$U$- and $V$-band curves (Bessell 1990) and with the Maun Kea $J$ band filter curve (Tokunaga et al. 2002) in the rest-frame. These values allow us to locate galaxies within the $UVJ$ diagram, in which passive galaxies are those which have $(U - V)_{\text{rest}} > 1.3$, $(V - J)_{\text{rest}} < 1.6$ and $(U - V)_{\text{rest}} > 0.88 \times (V - J)_{\text{rest}} + 0.49$.

We limit the influence of bright stars and UDS image artefacts (e.g. detector cross-talk) by removing all sources which are flagged by a factor of $\mu$ shift distribution for 850 $\mu$m sources have been shown to be overdense (m sources based on the UDS optical/near-infrared photometric redshifts. However, the price that we pay for this is that we do not identify the counterparts to any individual 850 $\mu$m source, and we also suffer from the issue that, because the environments of 850 $\mu$m sources have been shown to be overdense by a factor of 80 $\pm$ 30 times the background level (Simpson et al. 2015), the excess galaxies that we see in the near-infrared may not be responsible for the sub-millimetre emission themselves (see section 3.4, below).

### 3.1 Astrometry and initial checks

Before searching around the 850 $\mu$m source positions for $K$-band galaxies, we must first ensure that the CLS and UDS positions are consistent with each other. We do this by following the method used for sources in the Herschel-ATLAS survey by Smith et al. (2011), which involves creating a 2-dimensional histogram of the difference between the 850 $\mu$m and UDS positions for every source in each catalogue, which is shown in figure 1. Each bin of the histogram is 1 arc sec in size, and reveals a residual offset in the 850 $\mu$m astrometry relative to the UDS. To make the best estimate of the magnitude and direction of the offset, we model this distribution using a simple three-component model, consisting of two Gaussians with common centre, plus a constant background, and find the best fitting values for the centroid. The best-fit offsets derived using this model are $\Delta \alpha = 1.41 \pm 0.15$ arc sec and $\Delta \delta = -0.95 \pm 0.14$ arc sec, giving an effective offset of 1.7 arc sec (i.e. smaller than the pixel size in the 850 $\mu$m maps) which we apply to the CLS catalogue before continuing.

![Figure 1. Image showing a two-dimensional histogram of the differences between the 850 $\mu$m positions of the 761 sources in our catalogue and the F12 formalism:](http://www.nottingham.ac.uk/astronomy/UDS/)

$\chi^2 > 20$ in either the Hartley et al. (2013) or FAST SED fitting, to limit the influence of bad fits on photometric redshifts, galaxy colours and stellar masses.

### 3 RESULTS

In contrast to other investigations on this subject, we do not attempt to identify individual counterparts to CLS sub-millimetre sources. Instead, we take a statistical approach by measuring the properties of galaxies detected within and immediately around the SCUBA-2 beam, after subtracting off the expected background population, as a function of search radius. This method has the benefit of not requiring any assumptions about the number of $K$-band sources around each individual 850 $\mu$m position, and in the coming sections we will show that this enables us to generate a complete redshift distribution for 850 $\mu$m sources based on the UDS optical/near-infrared photometric redshifts.

The method of Fleuren et al. (2012, hereafter F12), in which this parameter is referred to as $Q_0$. It is difficult to estimate this value directly, due to the high probability of observing unrelated background sources around the 850 $\mu$m positions (i.e. the observed number of apparent counterparts within a particular search radius is in fact the sum of the actual number of counterparts and the number of chance associations), and because of the possibility of finding multiple $K$-band galaxies per 850 $\mu$m source. F12 showed that it is preferable to estimate $(1 - Q_0)$, by instead counting the number of ‘blanks’ (i.e. the number of sources without any possible counterpart) and statistically accounting for the unrelated background population. In the F12 formalism:

$$\frac{1 - Q_0}{\bar{R}} = \frac{S}{\bar{R}}$$

where $S$ is the fraction of 850 $\mu$m sources without a possible counterpart, and we estimate $\bar{R}$ (the fraction of random positions without a possible counterpart) by generating one hundred model catalogues with 761 random positions within the survey area, and returning the number of times zero matches are obtained (accounting for the masked area of our survey). We estimate these values as a function of radius, and the results are shown in figure 2, in which the light blue dashed line and red crosses connected by a red solid line show the fraction of blanks around random positions and 850 $\mu$m positions, respectively. The red crosses (showing the
results around the 850 μm positions) differ considerably from the results 
oround random positions.

The black filled circles show our best estimate of \((1 - Q_0)\) for CLS 850 μm sources, estimated using equation 1, and detailed in table 1. To determine whether seeing an excess \(K\)-band galaxy around all of the 850 μm sources is real (or just due to the large source density in the UDS catalogue), we first estimate the average number of excess non-blanks (i.e. detections) that we observe above what would be expected at random positions, \(N_{\text{excess}}\). We do this using equation 2:

\[
N_{\text{excess}} = (S - R)N_{850} - \sum_{N_{850}} P(\text{false}),
\]

where \(N_{850}\) is the number of 850 μm sources in our sample, and \(P(\text{false})\) is the probability that each 850 μm source is a false positive (as calculated by Geach et al. 2017, and these values indicate a total of 45.6 ± 1.8 spurious sources in our sample). We then calculate the null probability of this excess by taking the probability that a position is a blank out to some separation, \(R\), and multiplying it by itself \(N_{\text{excess}}\) times, giving a null probability of

\[
P_{\text{null}} = R^{N_{\text{excess}}}.
\]

The results are shown by the grey dot-dashed line in figure 2, and tabulated for separations ≤ 10 arc sec in table 1, which suggests that we can be confident that we detect a significant galaxy excess around \(> 98.4 \pm 0.9\) per cent of the 850 μm sample. This value is a little surprising, since the ‘false-positive’ probabilities imply that \(Q_0\) should be no more than 94 per cent, and the uncertainty on \(Q_0\) is insufficient to fully account for the discrepancy. If the false-positive probabilities are unduly conservative, this is relevant to other studies as well, for example Michałowski et al. (2017), who found that the faintest sub-millimetre sources have a lower ID fraction, and attributed this partly due to the increased fraction of spurious sources at fainter flux limits, and partly due to fainter sub-millimetre sources also being fainter in the radio maps (or other ancillary data) and thus harder to cross-identify. Forthcoming observations with ALMA will hold the key to determining how many of the sources in this catalogue are truly real.

### 3.3 The \(K < 24.6\) galaxy population around 850 μm sources

Having ascertained that the UDS data are deep enough that almost every CLS 850 μm source has at least one detectable (if not identifiable) and associated \(K < 24.6\) galaxy, we now wish to estimate how many galaxies we find for each. We do this by calculating the number of possible counterparts within a range of search radii between 0 and 20 arc sec, and subtract off the number of unassociated background sources that we would expect based on scaling the source density in the UDS \(K\) band catalogue to the relevant search area. The results of doing this are shown in figure 3, in which the red points with Poisson error bars show the radial distribution of the number of excess galaxies around the 761 850 μm sources. For comparison, we also overlay the corresponding plot based on 1,000 Monte Carlo simulations of the hypothetical scenario with one counterpart galaxy for each 850 μm position, assuming normally-distributed positional uncertainties depending solely on the signal-to-noise ratio of each source in the CLS catalogue (following the method in Ivison et al. 2007), added in quadrature with the 2 arc sec uncertainty resulting from pixel-quantised positions in the public CLS catalogue. We overlay the median-likelihood values (black) on the 16th and 84th percentiles of the cumulative frequency distribution (in grey) as a function of separation. We observe that the number of excess galaxies increases steadily out to around 12 arc sec, giving an average of \(1.52 \pm 0.09\) excess \(K < 24.6\) galaxies around each 850 μm source. These values highlight that in many cases we are detecting an excess of nearby \(K\)-band galaxies rather than the sources responsible for the 850 μm emission; this number is therefore not directly analogous to the SMG ‘multiplicity’ discussed above, but assuming that it is not dominated by a handful of sources with many components (and our estimate of \(Q_0\) derived in section 3.2 suggests that this is a reasonable assumption), finding \(1.52 \pm 0.09\) excess galaxies per 850 μm position is in good agreement with more direct studies of SMG multiplicity, both ob-

### Table 1. Tabulated values of \(Q_0\), as a function of maximum separation from the 850 μm source positions, with the right-hand column showing the probability of obtaining our results by chance, after accounting for the fraction of sources in the > 3.5σ 850 μm catalogue which are spurious.

<table>
<thead>
<tr>
<th>Max separation (arc sec)</th>
<th>(Q_0)</th>
<th>(P_{\text{null}})</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.103</td>
<td>0.000</td>
</tr>
<tr>
<td>2</td>
<td>0.346</td>
<td>0.000</td>
</tr>
<tr>
<td>3</td>
<td>0.602</td>
<td>0.000</td>
</tr>
<tr>
<td>4</td>
<td>0.802</td>
<td>0.000</td>
</tr>
<tr>
<td>5</td>
<td>0.882</td>
<td>0.000</td>
</tr>
<tr>
<td>6</td>
<td>0.947</td>
<td>0.000</td>
</tr>
<tr>
<td>7</td>
<td>0.967</td>
<td>0.000</td>
</tr>
<tr>
<td>8</td>
<td>0.984</td>
<td>0.000</td>
</tr>
<tr>
<td>9</td>
<td>0.975</td>
<td>0.205</td>
</tr>
<tr>
<td>10</td>
<td>1.000</td>
<td>0.780</td>
</tr>
</tbody>
</table>

Figure 2. Illustration of the procedure of Fleuren et al. (2012) to estimate \((1 - Q_0)\), the fraction of 850 μm sources which are not detected in the UDS catalogue. The red crosses show the fraction of blanks (i.e. those 850 μm positions with no possible counterpart within the search radius), while the light blue dashed line shows the corresponding values based on random positions, both relative to the right-hand vertical axis. The black filled circles represent the values obtained dividing the number of blanks by the randomly generated values, which is our estimate of \((1 - Q_0)\), relative to the left-hand axis. The grey dot-dashed line linking the triangles, indicates the probability of obtaining the number of blanks around the 850 μm source positions by chance, and this is < 1 per cent at all separations ≤ 10 arc sec. The values for \(Q_0\) and the probability of the null hypothesis are shown in table 1.
Figure 3. The radial distribution of excess galaxies around the CLS 850\,\mu m positions (red points with error bars), compared with expectations based on a single counterpart per SMG assuming normally distributed positional offsets depending on the signal-to-noise ratio, following Ivison et al. (2007), shown as the solid black line with grey region indicating the 16th and 84th percentiles of the expected excess based on our Monte Carlo simulations. While the left-hand vertical axis shows the total number of excess galaxies around the sample of 761 850\,\mu m sources in our search area, the right-hand axis has been scaled to show the average number of excess \( K \)-band galaxies around each source. The horizontal dashed line shows the number of 850\,\mu m sources in our catalogue.

3.4 The properties of galaxies near 850\,\mu m sources

We characterise these galaxies by extending the method of section 3.3 to produce background-subtracted distributions of their photometric redshifts, \( K \)-band magnitudes and stellar masses, and these are shown in figure 4. To determine the extent to which the properties of these sources are representative of the SMG host galaxy population, we perform an identical analysis using realistic mock catalogues based on lightcones from the Bolshoi simulation (Klypin et al. 2011), containing galaxies with stellar mass \( > 10^8 \, M_\odot \), over 0.5 \( < z \) \( < 8.0 \), which were produced by Hayward et al. (2013b) to study SMGs. While the stellar masses of excess galaxies within 12 arc sec of 850\,\mu m sources in the Bolshoi simulation (selected to the same flux criterion as in the real CLS catalogues) are significantly different from the stellar masses of the SMGs themselves, a \( K - S \) test shows that we are unable to rule out the hypothesis that the redshift distributions are drawn from the same parent distribution (we perform this simulation 1,000 times and find a median \( P \approx 0.3 \)). We therefore conclude that the photometric redshift derived in this manner is representative of the full SMG population.

In the top panel of figure 4 we show the photometric redshift distribution of the 1154.6 \( \pm 67.5 \) excess galaxies around all 761 \( > 3.5 \sigma \) CLS 850\,\mu m sources in our survey area as the black histogram, derived from the best-fit redshifts from the Hartley et al. (2013) catalogue, and overlaid (in red) with the corresponding distribution derived from the individual redshift probability distribution functions. The median redshift of the 850\,\mu m sources is \( \langle z \rangle = 2.05 \pm 0.03 \), which makes for an interesting comparison with many previous studies despite their incomplete redshift information (e.g. Wardlow et al. 2011; Casey et al. 2013; Simpson et al. 2014; Chen et al. 2016), and despite the important role played by selection (which we will discuss in section 4.2). We find that 18.2 per cent of the SMGs in our sample lie at \( z > 3 \), in good agreement with Wardlow et al. (2011). We also overlay the results of performing an identical analysis on the same number of random positions as the grey error bars, which recover a redshift distribution consistent with zero excess galaxies, reassuring us that our results are not caused by some undiagnosed bias. We have overlaid our results on the redshift distribution for the \( \geq 4\sigma \) sample of SMGs selected from the CLS observations of the COSMOS and UDS fields from Michałowski et al. (2017), who (as discussed in section 1) completed the redshift distribution for the \(~\)third of sources without cross-identified counterparts in their sample using long wavelength data. The Michałowski et al. (2017) redshift distribution (which has been arbitrarily re-scaled for clarity) has a higher median \( \langle z \rangle = 2.40^{+0.10}_{-0.04} \), and this is most readily apparent in the increased high-redshift tail in the shaded grey distribution in the top panel of figure 4. This apparent disagreement between the two \( > 4\sigma \) source redshift distributions (shaded grey from Michałowski et al. 2017, corresponding to the green distribution from this work) is of particular interest given the complementary strengths and weaknesses of the two methods.

Though the Bolshoi simulation shows us that the mass distribution of the galaxies in the simulation around the 850\,\mu m source positions differs from the mass distribution of the model SMG counterparts, it is nevertheless instructive to calculate the \( K \)-band magnitude and stellar mass distributions of these sources. In the middle panel of figure 4 we show the distribution of \( K \)-band magnitude for the excess galaxies, overlaid with the results of the analogous experiment using the same number of random positions (grey error bars). Interestingly, rather than increasing towards the limit of the UDS catalogue, the magnitude distribution peaks around \( K = 23.4 \) magnitudes (\( \sim 1.2 \) magnitudes above the \( K = 24.6 \) magnitude limit) before turning down. This reinforces our result from section 3.2 that the UDS data are sensitive enough to detect an excess of galaxies around virtually all of the 761 850\,\mu m sources in the Geach et al. (2017) catalogue for which we have coverage. If the excess \( K \)-band galaxies that we detect are not the sources responsible for the 850\,\mu m emission, the magnitude distribution of SMG counterparts must be bimodal, as expected based on the extreme dust columns around bright SMGs found by Simpson et al. (2015), \( A_V \approx 540^{+200}_{-100} \), mag. That we are detecting galaxies around 850\,\mu m sources not necessarily responsible for the 850\,\mu m emission offers a possible means to reconcile our results with the fact that 5 out of the 30 \( > 8 \) mJy CLS sub-millimetre sources in Simpson et al. (2016) do not have a \( K \)-band counterpart to at least one of the multiple blended components resolved by ALMA in this field.

To test for the possible influence of incompleteness in our \( K \)-band catalogue on our magnitude distribution, we correct the \( K \)-band magnitude distribution using the completeness curve for the parent UDS DR8 catalogue from Mortlock et al. (2015), and the results of applying this correction are overlaid as the black filled circles, which are consistent with the original results. In the bottom panel of figure 4, we show the corresponding mass distribution. We find that the galaxies around SMGs have an average stellar mass of \( 2.2 \pm 0.1 \times 10^{10} \, M_\odot \), around a factor of two lower than the value found by Wardlow et al. (2011, after accounting for the different initial mass function used in that work), though as noted above, that work...
assumed a standard H-band mass-to-light ratio for the stellar mass estimation, and was unable to account for the whole 850 µm source population, while we are likely biased towards lower stellar masses by including SMG neighbours in our calculation.

Since we derived rest-frame colours for every source in the UDS catalogue, we are able to apply the same technique to determine the locations of the excess galaxies around SMGs in the U/V J colour space. The results of doing so are shown in figure 5, in which the left-hand panel shows the distribution of galaxies in the UDS catalogue, with a dashed line to highlight the division between the regions occupied by star-forming and passive galaxies at z > 1, taken from Hartley et al. (2013). The colour of each bin is chosen to indicate the logarithm of the number of sources in that bin, ranging from 5 to 100 galaxies. In the right panel, we show the corresponding colour-colour space for galaxies within 12 arc sec of a CLS 850 µm source, with the same colour scaling, highlighting that while the vast majority are classified as star-forming on the basis of their rest frame colours, a small subset (an excess of 92.8 ± 23.7, or 8.0 ± 2.1 per cent of the total galaxy excess) are consistent with being passive galaxies, in agreement with previous work on smaller samples of the SMGs themselves (Smail et al. 2004).2

These results make a particularly interesting comparison with the results of Smith et al. (in preparation), who find that the average 850 µm flux density of z > 1, K-selected and U/V J star-forming galaxies increases with increasingly red (V − J)rest colour, meaning that we expect many SMG neighbours to be sub-millimetre faint, and therefore very difficult to identify even using e.g. sensitive high resolution sub-millimetre observations with ALMA, and the same is of course true of the passive galaxies. This highlights the need for deep optical/near-infrared data alongside sensitive interferometry if we are to truly understand the relationship between the properties of SMG host galaxies and their environments.

4 DISCUSSION

4.1 Can we believe photometric redshifts for sources this faint?

In deriving these results, we have of course assumed some degree of reliability in the UDS photometric redshifts, which Hartley et al. (2013) showed to be very precise. However, this can only be verified using spectroscopy, which is extremely challenging to obtain for large samples of faint sources such as those studied here, and the lower left panel of figure 4 indicates that ~ 39 per cent of the galaxies associated with 850 µm positions are fainter than K = 23.0, the limit of the UDS+ spectroscopic sample selection (Almaini et al. in prep).

Meanwhile, some works in the literature (e.g. Simpson et al. 2014) have been reluctant to quote photometric redshifts for sources with formal detections (defined as having an SNR > 3σ) in fewer than four optical/near-infrared bands, taking the conservative view that photometric redshifts derived for such sources are unreliable. However, other works have shown the value of measurements for deriving galaxy parameters even when they are not formally significant (e.g. Smith et al. 2013, 2014), and this is one of the reasons why photometric redshift codes such as FAST (Kriek et al. 2009)

2 To convince ourselves that our background subtraction is working as expected, we inverted the data and re-plotted with the same colour scheme, revealing no significant galaxy excess.
and LEPHARE (Ilbert et al. 2006) ideally require measured flux densities rather than magnitudes in their input catalogues (since fluxes are symmetric even for faint sources, and allow noisy negative flux estimates to be naturally included in the fitting).

Since we have not directly identified any counterparts to the 850 μm sources, it is difficult to directly investigate the number of photometric detections for any individual source. However, we can repeat our analysis, this time including only those sources which have at least four > 3σ detections in the UDS catalogue, and see what difference this makes to our results. We are still able to detect at least one galaxy associated with every SMG (i.e. our estimate of Q0 is still consistent with unity), and we still detect a significant excess of 1,091.8 ± 66.8 galaxies, as compared with 1154.6 ± 67.5 when the full sample is considered. This change indicates that around 5 per cent of the galaxies around SMGs have fewer than four 3σ detections, but the significance of the change is < 1σ, based on propagating the Poisson error bars. The average photometric redshift of the excess galaxies around SMGs in the remaining sample is 1.99 ± 0.03, which is consistent with the original value of 2.05 ± 0.03, while the UV/J passive fraction in the excess galaxies is unchanged. We therefore suggest that while this aspect may play a minor role, it does not give us any cause to mistrust our results more than we would any other study using photo-z; our approach benefits once more from not relying on any one single photometric redshift.

4.2 Do the brightest SMGs differ from the rest?

Several previous investigations (e.g. Ivison et al. 2002; Pope et al. 2005; Biggs et al. 2011; Chen et al. 2016) have found evidence for differences between the brightest and faintest SMGs in terms of their redshifts and the number of sources contributing to the single-dish 850 μm flux density (though Wardlow et al. 2011, found no evidence for this). In figure 6 we show how the median redshift varies as a function of the 850 μm flux density as red error bars, ranging from the full sample, to increasingly brighter subsets (note that the left-most error bar is derived based on the whole population, with increasingly smaller subsets as we move towards brighter SNRs). Also overlaid are results from selected other observational works in the literature (Chapman et al. 2005; Wardlow et al. 2011; Casey et al. 2013; Vieira et al. 2013; Simpson et al. 2014; Michałowski et al. 2017; Chen et al. 2016), along with their quoted error bars. We have also overlaid an estimate based on the latest measurements of the far-infrared luminosity function using SCUBA-2 and ALMA data from Kопrowski et al. (2017), shown as the dot-dashed light blue line) and theoretical results for bright (>5 mJy) SMGs based on the GALFORM semi-analytic model presented in Cowley et al. (2015), and based on the simulations from Hayward et al. (2013a).

We find strong evidence for a higher median redshift for increasingly bright 850 μm sources in our sample, with error bars estimated from the redshift histograms using the median statistics method of Gott et al. (2001). The average redshift ranges from 2.05 ± 0.03 for the full SNR > 3.5σ sample (equivalent to a 3 mJy-selected sample due to the highly uniform 850 μm map) of 761 galaxies, up to 3.13 ± 0.18 for the 45 sources brighter than 8σ. This result becomes even clearer if we consider the values quoted by other surveys, although the scatter in those works is considerably larger due to the smaller sample sizes, with the exception of Michałowski et al. (2017) who calculated the average redshift in bins of 850 μm flux density, including the ultra-faint sample from Kопrowski et al. (2016); these values are also overlaid in figure 6. The brightest samples, including the S1.1mm > 4.2 mJy SMGs from Kопrowski et al. (2014) over the COSMOS field (corresponding to 850 μm flux > 9.8 mJy assuming a standard dust SED) with ⟨z⟩ = 3.44 ± 0.16, and S1.4mm > 20 mJy SMGs (corresponding to 850 μm fluxes > 100 mJy) observed by the South Pole Telescope, which have an average redshift of 3.5 according to both Vieira et al. (2013) and Weiβ et al. (2013), further underline this trend.

In figure 7 we show a similar analysis, this time calculating the average number of galaxies around 850 μm positions as a function of SNR/flux. Taking the error bars into account, the data reveal...
we bring all of this information together, in an attempt (i.e. we ensure that we encode the behaviour apparent (Madau & Dickinson 2014) to (Dunlop et al. 2017) also shows little or no evidence for an increasing number of excess K < 24.6 galaxies towards brighter flux densities. This is reassuring, since if brighter 850 µm sources had a significantly larger number of excess galaxies, this might have skewed our photometric redshift distribution given that brighter sources lie at higher redshifts (figure 6).

It is of course possible that strongly gravitationally lensed sources within the 850 µm selected population could artificially increase the number of excess galaxies observed around the 850 µm positions, and previous works have shown that bright sub-millimetre flux selection can efficiently identify such systems (e.g. Negrello et al. 2010). However, according to the latest results, lensed systems only contribute appreciably to the 850 µm number counts above fluxes of 20 mJy (Geach et al. 2017), and there are no sources this bright in our sample. Since figure 7 also shows little evidence for an increase in the average number of excess galaxies for the brightest sources in our sample, we therefore suggest that strongly lensed galaxies do not have a major influence on our results.

4.3 The contribution of SMGs to cosmic star formation

In figure 8 we bring all of this information together, in an attempt to measure the contribution of SMGs to the cosmic star formation rate density (SFRD) estimates from Behroozi et al. (2013, shown as the dashed line) and Madau & Dickinson (2014, dotted line). We do this by randomly assigning redshifts to the 850 µm sources by sampling from the cumulative frequency distribution of photometric redshifts, using the different distributions shown in the main panel of figure 4 (i.e. we ensure that we encode the behaviour apparent in figure 6). We can then convert the deboosted 850 µm flux density supplied in the CLS 850 µm catalogue (Geach et al. 2017) to an SFR assuming an isothermal dust SED model (e.g. Hildebrand 1983; Smith et al. 2013) with \( T = 30 \text{ K} \) and \( \beta = 1.5 \), and a standard relationship between far-infrared luminosity and SFR from Kennicutt (1998) adapted for our choice of initial mass function such that \( \text{SFR} (\text{M}_\odot \text{ yr}^{-1}) \approx 1.06 \times 10^{-10} \left( L_{\text{IR}} / L_\odot \right) \). We estimate the star formation rate density in bins of redshift by calculating \( \sum \psi_i \), where \( \psi_i \) represents the SFR of the \( i \)-th source in the sample, and \( V_{\text{max}} = \) the maximum co-moving volume within which that source could be detected – is calculated by determining the redshift at which the 850 µm source would become too faint to be included in our 3.5 µm catalogue, accounting for the effective area of our survey, which is 0.527 deg^2. The grey points show these raw results, and we are able to correct these values to account for the completeness and fraction of false positives using the values supplied for each source in the CLS 850 µm catalogue. The corrected values are shown as the black asterisks, with error bars assigned from repeating the redshift assignment process 1,000 times, and counting the 16th and 84th percentiles of the resulting star formation rate density in each bin.

Though we have assumed a single isothermal dust SED template to make the conversion from 850 µm flux density to SFR, under this assumption we find that our SMG sample with complete redshift information contributes 30.5 ± 1.2 per cent of the Behroozi et al. (2013) cosmic star formation rate density estimate between 0.5 < z < 5.0 (where the uncertainty on the value we quote has been derived solely on the basis of Monte Carlo sampling from the photometric redshift distribution, and does not contain any contribution from the large uncertainty associated with the choice of far-infrared SED). This value is in excellent agreement with the 30 per cent estimated by Barger et al. (2012) based on SMGs’ radio luminosities, though it is 50 per cent higher than...
found by Michałowski et al. (2010), despite our use of a comparatively quiescent far-infrared SED relative to some other common choices (e.g. those based on prototypical local galaxies such as M82 or Arp220 from Polletta et al. 2007, or based on SMGs from Pope et al. 2008 and Michałowski et al. 2010). However using any of these templates would result in the apparent contribution of star formation in SMGs exceeding the total in our lowest redshift bin at 0.5 < z < 1. We are of course able to mitigate this behaviour by assuming a relationship between far-infrared luminosity and dust temperature (as found by many other studies; e.g Chapman et al. 2003; Hwang et al. 2010; Smith et al. 2013; Symeonidis et al. 2013; Swinbank et al. 2014), though given that we have not identified individual counterparts to the sub-millimetre sources, it is difficult to directly address the Herschel properties of the counterparts in the current work, however this will be possible in future studies with complete x-IDs and fully deblended Herschel photometry.

Also overlaid in figure 8 are the SFRD calculated based on the obscured star formation attributed to galaxies with SFR > 300M⊙ yr⁻¹ from Michałowski et al. (2017, grey diamonds), and the corresponding larger estimate of the total dust-obscured star formation based on the latest ALMA results (reconstructing the relationship between obscured star formation rate and stellar mass) using deep observations of the Hubble Ultra Deep Field by Dunlop et al. (2017, grey triangles). The comparison between the latter study and our results is of particular interest, since together the two studies imply that roughly 60 per cent of the total dust-enshrouded star formation over 1 < z < 4.5 is captured in SMGs detected by SCUBA-2. We have also included the results derived based on a 500 µm selected sample of sources obtained from 20 deg² of Herschel data from Rowan-Robinson et al. (2016, as light-grey squares), although as the authors note, they detect a far larger cosmic star formation rate density than other works. This discrepancy underlines the power of SCUBA-2 for high redshift studies.

Finally, we note that despite the uncertainty over the far-IR SED, we have reached our plausible results with the largest SMG sample with complete redshift information, and having naturally accounted for the fraction of 850 µm sources which are broken up into multiple components in high resolution sub-millimetre interferometry, even if those components are widely separated in redshift.

5 CONCLUSIONS
We have used 761 850 µm sources from the SCUBA-2 CLS observations of the UKIDSS UDS field (Geach et al. 2017), alongside the 8th UDS data release (Hartley et al. 2013) to statistically measure the complete redshift distribution of 850 µm sources. Whilst our method is unable to identify the counterparts to individual SMGs, we are able to account for multiple neighbouring galaxies, and for the distribution of background sources using the rich ancillary data that are available over this field.

We find that the UDS data are sufficiently deep to detect excess galaxies around virtually all of the 761 850 µm sources in our survey area, though we do not identify them, and they are not necessarily the same galaxies responsible for the 850 µm emission (some of which are too faint to be detected even in the UDS K-band data; Simpson et al. 2016). Simulations based on model light cones suggest that the redshift distribution of excess galaxies within 12 arc sec of an 850 µm source is indistinguishable from that of the SMGs themselves, and we use this fact to measure their complete optical/near-infrared photometric redshift distribution, finding that the SMGs in our > 3.5σ sample have an average redshift of 2.05 ± 0.03. We find an average of 1.52 ± 0.09 excess galaxies within 12 arc sec of an 850 µm position, and use the rest-frame colours of these galaxies to show that while the majority are likely to be dusty star forming galaxies, a substantial fraction are likely to be sub-millimetre faint, passive galaxies, and therefore difficult to detect even in deep high-resolution sub-millimetre imaging e.g. with ALMA. We show that the brightest SMGs lie at higher redshifts than the rest of the SMG population, and under the assumption of a universal isothermal far infrared dust spectral energy distribution we find that SMGs contribute around 30 per cent of the cosmic star formation rate density between 0.5 < z < 5.0.

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