

1 **Title:** Methodological approaches and related challenges associated with the determination  
2 of critical power and  $W'$

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7 **Abstract**

8 The relationship between exercise intensity and time to task-failure ( $P$ - $T$  relationship) is  
9 hyperbolic, and characterised by its asymptote (critical power, CP) and curvature constant  
10 ( $W'$ ). The determination of these parameters is of interest for researchers and practitioners,  
11 but the testing protocol for CP and  $W'$  determination has not yet been standardised.  
12 Conventionally, a series of constant work-rate tests (CWR) to task-failure have been used to  
13 construct the  $P$ - $T$  relationship. However, the duration, number, and recovery between  
14 predictive CWR, and the mathematical model (hyperbolic or derived linear models) are known  
15 to affect CP and  $W'$ . Moreover, repeating CWR may be deemed as a cumbersome and  
16 impractical protocol. Recently, CP and  $W'$  have been determined in field and laboratory  
17 settings using time-trials, but the validity of these methods has raised concerns. Alternatively,  
18 a 3-min all-out test (3MT) has been suggested, as it provides a simpler method for the  
19 determination of CP and  $W'$ , whereby power output at the end of the test represents CP, and  
20 the amount of work performed above this end-test power equates to  $W'$ . However, the 3MT  
21 still requires an initial incremental test, and may overestimate CP. The aim of this review is,  
22 therefore, to appraise current methods to estimate CP and  $W'$ , providing guidelines and  
23 suggestions for future research where appropriate.

24

25 Key words: Exercise tolerance; Exercise domains; Fitness testing; Performance; Fatigue

## 26        **1. Introduction**

27        The relationship between exercise intensity and time to task-failure ( $T_{lim}$ ) (i.e. the  $P$ - $T$   
28        relationship) has received extensive research attention. The first attempts to model the  $P$ - $T$   
29        relationship date back to the beginning of the 20<sup>th</sup> century when Kennelly (69) and Hill (50)  
30        studied the speed of humans and animals over various distances. However, Scherrer and  
31        Monod (95) formally described the  $P$ - $T$  relationship as hyperbolic in a single-joint muscle  
32        action. The  $P$ - $T$  relationship appears to be highly conserved, and has subsequently been  
33        observed in various forms of whole body exercise, in individuals with different levels of fitness,  
34        and across animal species (90).

35        The hyperbolic  $P$ - $T$  relationship is characterised by two parameters. The asymptote of the  
36        hyperbola is defined as critical power (CP), and the curvature constant is notionally  
37        abbreviated as  $W'$ . Briefly, it has been suggested that CP demarcates the highest exercise  
38        intensity at which metabolic and systemic responses attain a steady state (61,90,91). Where  
39        power is directly measurable (e.g. cycling), CP is typically expressed as a mechanical power  
40        output (PO). However, factors which affect the relationship between oxygen consumption  
41        ( $\dot{V}O_2$ ) and PO, such as cadence, are known to also affect CP (8), and indeed some authors  
42        have proposed to use the term 'critical intensity' and to express CP as a  $\dot{V}O_2$  equivalent (118).  
43        However, as expressing CP as a PO may be more applicable (86) and freely chosen cadence  
44        is relatively consistent within individuals (47), this review will consider CP as a mechanical  
45        PO. With regards to  $W'$ , it represents the amount of work that can be performed above CP,  
46        and was originally considered to represent anaerobic energy production (51,81). However, it  
47        is now accepted that the precise aetiology of  $W'$  is more complex, and affected by factors such  
48        as accumulation/depletion of intramuscular substrates and fatigue-related metabolites (90).  
49        Further details on the aetiology of CP and  $W'$  are discussed elsewhere (59,90,108).

50        The determination of CP and  $W'$  is of interest to researchers and practitioners alike. For  
51        instance, prescribing exercise intensities relative to CP may elicit a more homogenous  
52        response than other approaches to normalise the intensity of exercise, such as a percentage

53 of maximum oxygen consumption ( $\dot{V}O_{2max}$ ) (4,71,74). Secondly, exercise within the 'severe'  
54 domain, above CP, results in a progressive depletion of  $W'$ , so that when  $W'$  is depleted,  
55 exercise is either terminated or the intensity reduced to  $<CP$ . The determination of CP and  $W'$   
56 therefore allows prediction of the time to reach  $T_{lim}$  during exercise above CP. These  
57 predictions are typically within 15% of the actual  $T_{lim}$ , and actual and predicted  $T_{lim}$  are strongly  
58 correlated ( $r \geq 0.87$ ) (29,41,62,68,84,87,114). Thirdly, CP is strongly associated with  
59 endurance performance, and it has been shown to account for 69-86% of the variance in  
60 sporting events lasting ~2.2 to ~59 min (17,20,70,99). Similarly, running events lasting longer  
61 than 1 h, such as the marathon, are also strongly correlated with the running equivalents of  
62 CP (termed critical speed (CS)), and completed at an intensity close to, but fractionally below,  
63 CP (41,59).. Moreover, the combination of CS and the running equivalent of  $W'$  ( $D'$ ) predicts  
64 5000-m running performance within 1% (85). Finally, with the advantages of the  
65 aforementioned applications, it is not surprising that the  $P$ - $T$  relationship has been used to  
66 evaluate and monitor performance, and proposed as a tool for anti-doping (37,93,116).

67 The determination of CP and  $W'$ , however, is not standardised. In most laboratories, CP and  
68  $W'$  have been determined using a series of square-wave constant work-rate tests to task-  
69 failure (CWR), in which  $T_{lim}$  is recorded. These CWR are usually interspersed with 24 h of  
70 recovery, making this method cumbersome and impractical. Several attempts have been  
71 made to simplify the protocol, including reducing the number of CWR required, or shortening  
72 the 24-h recovery duration between CWR. In addition, advancements in the development of  
73 power meters and ergometers have facilitated the determination of CP and  $W'$  using time-  
74 trials (TT), both in the field and the laboratory. Alternatively, CP and  $W'$  may be determined  
75 using a 3-min all-out test (3MT), whereby the mean PO during the final 30 s of the test  
76 represents CP, and the amount of work performed above that mean end-test PO represents  
77  $W'$ . However, the above approaches have limitations, and there are methodological  
78 challenges that need to be considered. The estimation of CP and  $W'$  is influenced by the  
79 testing protocol and, as a result, research findings between studies are difficult to compare.

80 This review aims to draw attention to these issues and, where appropriate, to state relevant  
81 recommendations for the determination of CP and  $W'$ .

82 **2. Conventional approach to determine CP and  $W'$ : mathematical models,**  
83 **and duration, number, and recovery between tests.**

84 The conventional approach to determine CP and  $W'$  in a laboratory setting requires the  
85 performance of 3–5 CWR, where PO and  $T_{lim}$  are recorded. From these data, total work  
86 performed (i.e.  $Work = PO \times T_{lim}$ ) and the inverse of  $T_{lim}$  (i.e.  $T_{lim}^{-1}$ ) can be calculated  
87 (Table 1); with subsequent linear and non-linear models applied to estimate CP and  $W'$   
88 (43,49,51,60,81).

89 \*\*\*Figure 1 near here\*\*\*

90 \*\*\*Table 1 near here\*\*\*

91 PO and  $T_{lim}$  derived from each CWR can be fitted using a hyperbolic function (Figure 1A). The  
92 asymptote of the hyperbola represents CP, and the curvature constant denotes  $W'$ . For any  
93 given PO above CP, the duration of exercise to task-failure (i.e.  $T_{lim}$ ) is determined as:

94 
$$T_{lim} = \frac{W'}{PO - CP} \quad [1]$$

95 The non-linear equation [1] can be rearranged to a linear function by plotting PO against the  
96 inverse time ( $T_{lim}^{-1}$ ). Here, the slope of the line represents  $W'$ , and the y-intercept represents  
97 CP (Panel 1B):

98 
$$PO = CP + W' \times T_{lim}^{-1} \quad [2]$$

99 An alternative linear function of the  $P$ - $T$  relationship may be obtained by plotting the work  
100 accomplished in each CWR against  $T_{lim}$  (Figure 1C). The y-intercept of this line represents  $W'$ ,  
101 and the slope represents CP:

102 
$$Work = W' + CP \times T_{lim} \quad [3]$$

103 Fitting the  $P$ - $T$  relationship with a 2-parameter function (non-linear or derived linear functions)  
104 has some limitations. For instance, as  $T_{lim}$  approaches zero,  $PO$  becomes infinite. To  
105 overcome this limitation, a third parameter,  $k$ , has been introduced (80):

$$106 \quad T_{lim} = \left( \frac{W'}{PO-CP} \right) + k \quad [4]$$

107 where  $k$  is interpreted as the maximum instantaneous  $PO$  ( $PO_{max}$ ). Hence, with the inclusion  
108 of  $k$ , as  $T_{lim}$  approaches zero,  $PO$  approaches  $PO_{max}$ .  $CP$  and  $W'$  can be determined from a 3-  
109 parameter model, in which  $k$  is substituted as:

$$110 \quad T_{lim} = \left( \frac{W'}{PO-CP} \right) + \left( \frac{W'}{CP-PO_{max}} \right) \quad [5]$$

111 Another limitation of 2-parameter models is the assumption that, for any intensity below  $CP$ ,  
112 there is no contribution of  $W'$  at the onset of exercise. However, with a demonstrated link  
113 between  $CP$  and  $\dot{V}O_2$  on-kinetics (46,83), some authors have suggested that  $W'$  contribution  
114 at the onset of exercise may be somewhat underestimated (60,82). Wilkie (117) proposed  
115 accounting for  $\dot{V}O_2$  on-kinetics through the use of a rather fast time constant of 10 s for all  
116 individuals. While the inclusion of the time constant of  $\dot{V}O_2$  on-kinetics appears to be  
117 physiologically sound, it seems a cumbersome addition and is currently not used. Further  
118 research may investigate whether the inclusion of an individually-derived time constant  
119 improves the precision of  $CP$  and  $W'$  estimations.

120 An area of concern is the test-retest reliability of the estimates of  $CP$  and  $W'$  derived from  
121 CWR. Using the linear  $T_{lim}^{-1}$  model (Equation [2]), the coefficient of variation (CV) and  
122 correlation coefficient ( $r$ ) of  $CP$  have been reported at 3% and 0.96, respectively; whereas the  
123 corresponding values for  $W'$  were 10.3% and 0.79, respectively (44). It is worth noting that a  
124 10-15% variability in  $T_{lim}$  has been observed in CWR (5,72,82). A large variation in  $W'$  may  
125 occur as a result of the nature of the mathematical model, since small changes in  $T_{lim}$  during  
126 exhaustive CWR have a negligible effect on  $CP$ , but a much larger effect on  $W'$  (93,105,107).  
127 Nonetheless, the test-retest reliability seems to be poorer for  $W'$  than  $CP$  using other

128 methodological approaches (e.g. TT or all-out tests, see discussion below). Furthermore,  
129 studies comparing different approaches to determine CP and  $W'$  typically report a closer  
130 agreement between methods for estimating CP than for  $W'$  (e.g. (65,85,96,103,109,119)),  
131 although a high reliability for both parameter estimates (ICC of 0.94 and 0.95 for CP and  $W'$ ,  
132 respectively) was reported after a familiarization trial when using TT under controlled  
133 laboratory conditions (103). Overall, however,  $W'$  appears to exhibit a greater variability than  
134 CP, though the reason(s) for this phenomenon are not yet completely understood.

### 135 2.1. Effect of the mathematical modelling on CP and $W'$ estimations

136 The equations described above typically fit the data with a high degree of accuracy ( $R^2 \geq 0.82$ )  
137 (14,23,43). However, they result in different estimations of CP and  $W'$ , even though some of  
138 these equations [1-3] are mathematically equivalent (14,19,20,22,23,43,56,94). Depending on  
139 the model, estimations of CP typically are, from highest to lowest, in the following order: linear  
140  $T_{lim}^{-1}$  model (equation [2]), linear total work model (equation [3]), 2-parameter hyperbolic model  
141 (equation [1]), and 3-parameter model (equation [5]); with estimations of  $W'$  following the  
142 reverse order (Figure 2). It is important to note that in some studies no differences between  
143 mathematical models were reported (e.g. (19,31,105)). Nonetheless, irrespective of whether  
144 estimations of CP derived from different mathematical models reach statistical significance,  
145 large  $T_{lim}$  differences have been observed during exercise at respective CP intensities, ranging  
146 ~20-60 min (21,23,51,77,85,87).

147 The question of which mathematical model should be used to determine CP and  $W'$  remains  
148 unresolved. The 3-parameter model consistently produces lower estimates of CP and greater  
149 estimates of  $W'$  than 2-parameter models (14,20,22,28,43). Furthermore, the 3-parameter  
150 protocol, suggested by Morton (80), requires a relatively large number of trials, including some  
151 with low (<1 min) and high (>15 min)  $T_{lim}$ , which in turn can affect the estimation of CP and  $W'$   
152 (see section 2.2). Moreover, the 3-parameter model may produce non-physiological estimates  
153 of  $PO_{max}$ , and the parameter exhibits large inter-subject variability (28,43,80). These issues  
154 may explain why most recent studies have indeed used 2-parameter models (e.g.

155 (61,63,79,91)). An alternative approach has been proposed by Hill (51), and recently adopted  
156 by some researchers (18,19,101), whereby the model producing the lowest standard error of  
157 estimate (SEE) is used. We therefore recommend that the  $P$ - $T$  relationship should be  
158 characterised with the 2-parameter model that results in the lowest SEE.

## 159 2.2. Effect of duration of predictive trials on CP and $W'$

160 The characteristics of the tests used to define the  $P$ - $T$  relationship have a profound effect on  
161 CP and  $W'$  estimates. For instance, the duration of CWR is known to affect CP and  $W'$   
162 (16,26,57,75,102,106,115). If data from five tests to task-failure is rearranged, and only the  
163 three tests with the shortest durations are considered, CP has been shown to be 14-20%  
164 greater than that derived from the three longest durations, irrespective of the overall range of  
165 duration of all five exhaustive CWR (16,57). Moreover,  $W'$  appears to be notably more  
166 sensitive to the duration of the trials, with the three shortest exhaustive trials producing  $W'$   
167 estimates ~70% greater than those derived from the three longest trials (16). The effect of trial  
168 duration on CP and  $W'$  is shown in Figure 3.

169 Scherrer and Monod (95) stipulated that the work- $T_{lim}$  relationship (equation [3]) loses linearity  
170 for exercise durations <2 min, with di Prampero (92) specifying that the range of test durations  
171 should be such that  $\dot{V}O_{2max}$  is elicited, and that  $W'$  is fully depleted during each trial. However,  
172 the first requirement is not always verified (48,53,75,81), and a complete depletion of  $W'$  may  
173 be difficult to assess. At very high intensities (i.e. short  $T_{lim}$ ),  $W'$  may contribute more than the  
174 model predicts due to the relatively slow increase in  $\dot{V}O_2$  (16,81,107). Moreover, at such high  
175 intensities, it is possible that exercise terminates before  $\dot{V}O_{2max}$  has been reached  
176 (27,52,92,105). Therefore, trials with a  $T_{lim}$  <2 min should be considered too short and not  
177 included in the determination of CP and  $W'$  (16,60,91,92). On the other hand, exercise  
178 performed above CP and continued for >2 min should lead to maximal values of  $\dot{V}O_2$  and  
179 blood lactate concentration (19,25,88). However, some studies have reported that  $\dot{V}O_2$  did not  
180 reach its maximum at task-failure during the longest predictive trials, which corresponded to  
181 intensities slightly (~10%) above CP (11,94). The reason(s) for this phenomenon remain

182 unknown, but it is likely to be multifactorial, including physiological and/or psychophysiological  
183 factors (1,11,94). Therefore, it is recommended that exhaustive trials which result in  $T_{lim} > 15$   
184 min should be avoided as  $\dot{V}O_{2max}$  may not be reached. Furthermore, whenever possible, and  
185 at least for research purposes, we recommend that the attainment of  $\dot{V}O_{2max}$  should be verified  
186 for all predictive trials.

187 The range in the duration of the trials should also be considered when investigating alternative  
188 testing protocols (i.e. duration of criterion versus experimental trials) (104). In order to  
189 minimise such effects, it is now common that CP and  $W'$  are determined from trials with  $T_{lim}$   
190 ranging between 2 and 15 min, with a minimum of at least 5 min between the longest and  
191 shortest trial (e.g. (67,105,112)). Nonetheless, it has been shown recently that the duration of  
192 the predictive trials may still affect the estimation of CP and  $W'$ , even when these trials are  
193 performed within the recommended  $T_{lim}$  range of 2-15 min. Triska et al. (102) determined CS  
194 and  $D'$  from two protocols: three TT of 12, 7, and 3 min and three TT of 10, 5, and 2 min. The  
195 former protocol resulted in ~3% lower CS and ~14% higher  $D'$  compared to the latter protocol.  
196 It is unclear if these findings can be extrapolated to other forms of exercise such as cycling,  
197 but these data suggest that a consistent protocol should be used to assess or monitor  
198 performance using the CP model.

199 In summary, 2-15 min is the recommended duration of trials, and exhaustive trials resulting in  
200 a  $T_{lim} < 2$  min or  $> 15$  min should be excluded from calculations. The specific duration of  
201 predictive trials should also be considered, even if the overall range of durations falls within  
202 the target of 2-15 min. Alternatively, research investigating the effects of a treatment may  
203 employ the same duration (i.e. TT). Furthermore, the attainment of  $\dot{V}O_{2max}$  should be verified  
204 wherever possible before including respective trials in the calculation of CP and  $W'$ .

### 205 2.3. Effect of the number of trials on CP and $W'$

206 Critical power and  $W'$  can be determined from just two trials. Indeed, CP determined from two  
207 exhaustive trials with relatively different  $T_{lim}$  ( $> 15$  min) was only ~1.1% greater than that

208 determined using four trials (55). More recently, Simpson and Kordi (97) determined CP and  
209  $W'$  in experienced cyclists using a protocol consisting of two laboratory-based TT of 3 and 12  
210 min, interspersed with 40 min of passive rest. The authors noted that, after two familiarisation  
211 sessions, the addition of a third trial of intermediate duration (5 min) did not affect CP or  $W'$ . A  
212 potential limitation of this approach is that using only two exhaustive trials always results in a  
213 perfect fitting of the model, and therefore SEE cannot be determined. Instead, to ensure a  
214 high quality of the model, particularly for research purposes, the  $P$ - $T$  relationship is most  
215 commonly determined from three or more CWR to task-failure (51). Indeed, a recent approach  
216 proposes performing trials until the model falls within a certain SEE; for example, less than  
217 2% (36,40,102) or 5% (18,19) for CP, and less than 10% for  $W'$  (18,19,36,40,102). In  
218 summary, using only two exhaustive trials may seem an attractive option to determine CP and  
219  $W'$  in the interest of a short protocol. However, where possible and at least for research  
220 purposes, we recommend using three or more trials, so that the  $P$ - $T$  relationship provides  
221 estimates within predetermined SEE's for CP and  $W'$ .

#### 222 2.4. Duration of the recovery between exhaustive trials

223 The duration of the recovery between exhaustive trials is usually at least 24 h, which makes  
224 the determination of the  $P$ - $T$  relationship cumbersome. To address this issue, some authors  
225 have investigated whether a shorter recovery between trials affects CP and/or  $W'$   
226 (15,45,63,85,97,105). Karsten et al. (64) compared the conventional 24 h method with two  
227 experimental recovery durations of 3 h and 30 min. The authors observed that, in comparison  
228 with the standard 24-h-recovery protocol, the two shorter recovery protocols were sufficient to  
229 not affect CP (prediction error of 2.5% and 3.7% for the 3 h and 30 min recovery protocols,  
230 respectively, compared to 24 h). However, the prediction error inherent in the experimental  
231 protocols was higher for  $W'$  (25.6% and 32.9% for the 3-h and the 30-min protocols,  
232 respectively). The authors proposed a couple of reasons to explain these findings. Firstly, the  
233 shorter recovery protocols might have led to only a partial reconstitution of  $W'$ ; although  $W'$   
234 may be restored within ~25 min following exhaustive exercise (33,39,98). Secondly, high-

235 intensity exercise can affect the  $\dot{V}O_2$  on-kinetics and increase (i.e. 'prime') performance in  
236 subsequent exercise performed up to 45 min after the initial bout (3,24). However, Karsten et  
237 al. (63) more recently showed that  $\dot{V}O_2$  on-kinetics were not significantly different between  
238 repeated CWR and TT following a 60-min recovery period, suggesting that, at least for the 3-  
239 h recovery intervention, the argument does not hold. In summary, a single-day determination  
240 of CP can be achieved by reducing the inter-trial recovery time to 30 minutes. However, at  
241 present, a more conservative recovery of 60-min is preferred to determine both CP and  $W'$ , in  
242 order to minimise any potential priming effect and to allow for a full reconstitution of  $W'$ .

### 243 **3. Determination of CP and $W'$ using time trials under laboratory and field** 244 **conditions**

#### 245 3.1. Laboratory and field determination of critical power and $W'$

246 With the popularisation of power meters PO data is readily available, which allows analysis of  
247 the  $P$ - $T$  relationship in the field. For instance, PO data from elite cyclists over a competitive  
248 season have been reported for exercise durations ranging from 1 s to 4 h and, unsurprisingly,  
249 mean PO decreases nonlinearly as the duration increases (89). Indeed, a translation of  
250 laboratory-based determination of CP and  $W'$  into the field was attempted by Karsten et al.  
251 (65). The study compared CP and  $W'$  results, using three laboratory CWR (resulting in task-  
252 failure times of ~12, 4, and 2.5 min) with those determined from three track-based TT where  
253 participants had to produce the highest possible PO for 12, 7 and 3 min. All tests were  
254 performed on separate days and the authors reported a close agreement between laboratory  
255 and field CP values (prediction error of 7 W). However, field values of  $W'$  were ~5 kJ higher  
256 than those obtained in the laboratory, irrespective of the mathematical model used. In a follow  
257 up study (67), a shortened testing protocol (i.e. a 30 min intra-trial recovery period; see Section  
258 2.4) was used to investigate whether CP and  $W'$  could be reliably determined from road PO  
259 data. The study comprised three experimental protocols and a criterion protocol to determine  
260 CP and  $W'$ . The criterion protocol consisted of three laboratory-based CWR interspersed with  
261 30-min recovery; and the experimental protocols were: i) a TT field-based protocol consisting

262 of three maximal exhaustive efforts over 12, 7 and 3 min, interspersed with 30-min recovery;  
263 ii) a field-based protocol consisting of three TT over the same durations, but interspersed with  
264 24-h recovery; and iii) non-intentional TT maximal efforts (i.e. highest PO over the three  
265 durations obtained at any point during a single training session). The results demonstrated a  
266 high agreement for all experimental CP values with a mean prediction error of ~11, 17 and 14  
267 W for protocols i, ii, and iii, respectively. However, results for  $W'$  showed an unacceptably high  
268 prediction error of ~3, 4, and 3 kJ, respectively. All experimental protocols were repeated three  
269 times with a mean within-protocol CV for CP of 2.4%, 6.5%, and 3.5%, respectively. Of note  
270 is that protocol ii is at the upper end of what is considered as acceptable reliability for  
271 physiological variables in sports science research (2,54). With regards to  $W'$ , only protocol iii,  
272 the non-intentional efforts, provided a relatively low CV for  $W'$  (~17%) when compared to  
273 protocol i (~46%) and protocol ii (~45%). Triska et al. (105) compared a single-day field test  
274 to estimate CP and  $W'$  (three TT of 12, 6, and 2 min) with a laboratory-based protocol using a  
275 cadence dependent (i.e. linear) mode to mimic 'real-world' exercise. The authors reported  
276 similar mean values between conditions for CP (laboratory: ~280 W vs. field: ~281 W), and a  
277 95% LoA of -55 – 50 W. In contrast,  $W'$  was significantly higher under laboratory conditions  
278 (~21.6 vs. ~16.3 kJ) with a correspondingly poor agreement (95% LoA: -3.5 – 16.4 kJ)  
279 between protocols. Altogether, these data suggest that CP can be determined with reasonable  
280 precision in the field, or by simulating field conditions (i.e. using TT). However,  $W'$  appears to  
281 be under- (single-day approach, (105)) or over-estimated (multi-day approach, (65)) using  
282 these tests; though reasons have not yet been elucidated.

### 283 3.2. Time-trial versus constant work-rate tests

284 There are a number of methodological differences between laboratory- and field-based tests  
285 that need to be considered within the context of CP and  $W'$  determination. First, laboratory-  
286 based protocols typically use open-end tests (i.e. CWR), whereas field tests typically employ  
287 maximal effort over a fixed time or distance (i.e. TT). Time-trials exhibit less test-retest  
288 variation than CWR (72), and therefore resulting in significantly lower SEE for CP and  $W'$

289 estimates (63). Secondly, TT are self-paced, and pacing has been shown to affect the  $P-T$   
290 relationship (18,62). Black et al. (18) compared estimations of CP and  $W'$  derived from 4-6  
291 CWR prediction trials performed on different days with work-matched TT in the laboratory.  
292 Despite being equalled for work, mean PO was higher, and therefore  $T_{lim}$  shorter during TT,  
293 possibly due to the fast-start commonly adopted in TT (18). As a result, CP was ~7% higher  
294 using TT, whereas  $W'$  was not affected by the type of exhaustive trials; though there was a  
295 negative correlation ( $r = -0.74$ ) between the relative change in CP and  $W'$  in CWR and TT (18).  
296 In contrast, Karsten et al. (63) compared non time-matched CWR with TT in the laboratory,  
297 with a recovery time of 60 min between efforts to avoid a possible  $\dot{V}O_2$  priming effect evident  
298 with shorter recovery periods (see Section 2.4). The results demonstrated a low prediction  
299 error for CP (2.7%; 8 W), but a high prediction error for  $W'$  (18.8%; 2.5 kJ); though it is likely  
300 that the latter was influenced by the relatively short recovery period between efforts. It is also  
301 worth noting that Black et al. (18) utilised self-paced TT, where the ergometer was set in linear  
302 mode with a fixed resistance (i.e. cadence-dependent mode) allowing PO to be regulated by  
303 cadence only, whereas Karsten et al. (63) utilised self-paced TT, where the ergometer allowed  
304 PO to be self-regulated using changes in gear ratio (virtual) and cadence, in an attempt to  
305 better replicate real-world cycling. Thirdly, TT are not constrained by cadence, whereas CWR  
306 are commonly performed at a predetermined cadence (105), and pedalling rate is known to  
307 affect CP and  $W'$  (8,34,73,110). Fourthly, the duration of CWR is variable, whereas it can be  
308 standardised for TT. As a result, there might be differences in the duration of exhaustive trials  
309 (18), which, as discussed above, can affect CP and  $W'$ . Further evidence for the effects of  
310 time differences also comes from other exercise modes. In running, Galbraith et al. (45)  
311 reported that estimations of CS derived from three TT interspersed with either 30 or 60 min of  
312 passive rest between trials were not significantly different from three CWR performed in the  
313 laboratory using a multi-day protocol (typical error  $0.14 \text{ m}\cdot\text{s}^{-1}$  and  $0.16 \text{ m}\cdot\text{s}^{-1}$  for 30 or 60-min  
314 rest, respectively). In contrast, field-based estimations of  $D'$  were significantly lower (typical  
315 error 88 m and 84 m for 30 or 60-min rest protocols, respectively) than those derived from a  
316 laboratory-based test. The field-based approach also exhibited comparable test-retest

317 variability to that obtained from the conventional laboratory-based approach (0.4% and 13%  
318 for CS and  $D'$ , respectively). Triska et al. (104) attempted to address the issues surrounding  
319 the values of  $D'$  by time-matching the laboratory and the field trial durations. The authors  
320 reported no differences and positive correlations for CS and  $D'$  between the two conditions,  
321 and LoA of  $\pm 0.24 \text{ m}\cdot\text{s}^{-1}$  and  $\pm 75.5 \text{ m}$ . These studies seem to indicate that reasons other than  
322 that of trial duration are responsible for the conundrum surrounding  $D'$ . Fifthly, there appear to  
323 be a number of factors during field-based TT protocols that might affect CP and  $W'$  such as  
324 standing vs. rolling starts, overcoming inertia and acceleration, increased air resistance, or  
325 differences in terrain (78,88,105). The precise role of each of these factors warrants further  
326 investigation. On the other hand, field based-based tests can offer a more ecologically valid  
327 approach to estimate CP and  $W'$ . This is particularly true if CP and  $W'$  are to be used in the  
328 field, where the above issues of acceleration, pacing or air resistance, remain present. A final  
329 point to consider is the test-retest reliability of estimations of CP and  $W'$  using TT. Recently,  
330 Triska et al. (103) performed three identical TT to determine CP and  $W'$  using a single-day  
331 protocol with the first TT used as familiarisation. The authors noted that the CV of CP and  $W'$   
332 between the familiarisation and the first subsequent TT were 4.1% and 25.3%, respectively.  
333 However, the analysis of the two consecutive TT performed after familiarisation produced  
334 closer estimates in both CP and  $W'$  (2.6% and 8.2%, respectively). Therefore, the authors  
335 concluded, familiarisation is advisable to determine CP and  $W'$  from TT using a single-day  
336 protocol.

337 In summary, although laboratory-based TT can be used to determine CP and  $W'$ , some  
338 discrepancies in the estimation of CP and, in particular,  $W'$  are evident. Nonetheless, and even  
339 though there are methodological differences between CWR and TT protocols, TT may be  
340 preferable over CWR, particularly if the data are to be used under field conditions. If CP and  
341  $W'$  are determined from TT, performing a familiarisation trial is advisable to increase the  
342 reliability of the estimates.

#### 4. The 3-min all-out test

The conventional approach to determine CP and  $W'$  requires the performance of repeated maximal efforts, which may compromise the practical application of the model. It has been hypothesised that the parameters of the  $P$ - $T$  relationship may be obtained from a single all-out test. The rationale is that, at the start of all-out efforts,  $W'$  is heavily utilised; however, as the exercise continues and PO decreases, so does  $W'$ . If the duration of exercise is sufficiently long,  $W'$  becomes fully depleted and, therefore, the PO at or towards the end of an all-out effort should represent CP. Dekerle et al. (35) first explored this idea using an all-out effort lasting 90 s; but the authors noted that at the end of the test, PO was greater than CP, and that  $W'$  was not fully depleted. Burnley et al. (25) extended the duration to 180 s, and observed that the decrease in PO had stabilised in the final 30 s of the test (defined as 'end-test power output' [EP]) (Figure 4). In a follow-up study, a close agreement was reported between the conventionally determined CP and the EP obtained during a 3MT ( $r = 0.99$ ;  $SSE = 6.4$  W) (109). Moreover, the work performed above EP (WEP) was similar to  $W'$  ( $r = 0.84$ ;  $SEE = 2.6$  kJ). For the purpose of this review we will use CP and  $W'$  when referring to results derived from the conventional protocol using CWR or TT, and EP and WEP when referring to the 3MT.

The original 3MT still requires two testing days, as a prior exhaustive incremental maximal test is a prerequisite for the subsequent ergometer setting, using values of gas exchange threshold (GET), preferred cadence, and  $\dot{V}O_{2max}$  (25,109). The 3MT starts with a period of unloaded cycling after which participants are instructed to accelerate their cadence up to 110–120 rpm at which point the cycle-ergometer switches into the linear mode. The linear factor is set so that at the participant's preferred cadence, the PO corresponds to halfway between GET and  $\dot{V}O_{2max}$  (50% $\Delta$ ; Equation [6]), which is suggested to approximate CP (25):

$$Linear\ factor = \frac{PO\ at\ 50\%\Delta}{Cadence^2} \quad [6]$$

As fatigue develops during all-out exercise, cadence drops resulting in a decline in PO and the typical curvilinear 3MT power profile. To prevent pacing, participants are blinded to

369 elapsed time, and strong verbal encouragement is required throughout the test. To provide  
370 reliable results, a familiarisation 3MT trial is also commonly performed, increasing the overall  
371 time required to determine EP and WEP. Performing a GXT, a familiarisation trial and the  
372 actual 3MT necessitates more than one laboratory visit, which in turns lengthens a protocol  
373 that benefits from an otherwise short testing methodology.

374 There are no formal criteria to verify the validity of the 3MT. However, some authors reported  
375 that PO plateaus towards the end of the 3MT, as determined using consecutive 30-s bins  
376 (25,42). It has been also reported that PO peaks within the first 10 s (109), and subsequently  
377 decreases rapidly so that >90% of WEP is depleted within the first 90 s of the test (110). In  
378 addition, as an all-out effort is required, a decrease in PO greater than 5% of EP (see  
379 discussion below on reliability) for 5 s may denote pacing and cause some reconstitution of  
380 WEP, and therefore an overestimation of this parameter. An accurate selection of the linear  
381 factor is crucial, since relatively small alterations in preferred cadence by  $\pm 10$  rpm can  
382 significantly affect EP and/or WEP and end test cadence (110). To reflect the maximal (i.e. all-  
383 out) nature of the test,  $\dot{V}O_2$  has been suggested to attain its maximum during a 3MT  
384 (25,42,109); and blood lactate concentration reaches  $>8$  mmol·L<sup>-1</sup> (25,110,113). In summary,  
385 the following criteria may be proposed to ensure a true 3MT all-out effort: i) a plateau in PO in  
386 the last 30 s of the test; ii) the attainment of peak PO within the first 10 s of the test; iii) rapid  
387 initial decrease of PO, so that >90% of WEP is depleted within the first 90 s of the test; iv) no  
388 decrease in PO  $>5\%$  EP for  $>5$  s during the test; v) an end-test cadence within 10 rpm of  
389 preferred cadence; vi) the attainment of  $\dot{V}O_{2max}$ ; and vii) a blood lactate concentration  $>8$   
390 mmol·L<sup>-1</sup>. With regards to the reliability of EP and WEP, both parameters show a similar  
391 degree of reliability to those derived from the conventional testing approach. Specifically, the  
392 reliability of EP has consistently been shown to be better (CV of 3-7%) than that of the WEP  
393 (8-21%) (25,38,58,73).

#### 4.1. Single-day alternatives of the original 3MT

As the original 3MT requires two laboratory visits, several authors have attempted to shorten or to simplify the original 3MT. For instance, Johnson et al. (58) proposed that the resistance of the 3MT may be determined relative to body mass, somewhat similar to the Wingate anaerobic test. Bergstrom et al. (10) reported that a modified 3MT, performed on a mechanically-braked ergometer, with resistances set at 4.5% body mass, could be used to determine EP and WEP. However, if the resistance was set at 3.5% body mass the modified 3MT produced different estimates of EP and WEP than those derived from the original 3MT and from the conventional approach (10); although the error was not reported, and agreement between methods was identified using a test of difference. In a similar study, Clark et al. (31) performed a 3MT on a mechanically braked ergometer using loads of 3, 4, or 5% of body mass for recreationally active, anaerobic and aerobic athletes, and endurance athletes, respectively. There were no significant differences in either EP or WEP determined from the 3MT, irrespective of whether values were determined using linear factors based upon body mass or using the conventional linear factor of 50% $\Delta$ . The authors, however, reported a large individual variation between the methods in estimates of EP and, particularly, WEP (4.2% and 39.4%, respectively). Dicks et al. (38) calculated the linear factor based on age, gender, body mass and self-reported physical activity levels. The authors reported no differences in either EP or WEP between the original 3MT and the alternative 3MT. Moreover, there were no differences between the parameters of the  $P$ - $T$  relationship derived from the alternative 3MT, and those derived from three CWR using linear models (Eqs. [2,3]). However, the CV between methods was again much higher for WEP ( $\geq 21.8\%$ ) than for EP ( $\leq 4.8\%$ ) (38). In addition, Dicks et al. (38) used CWR lasting ~3, 4, and 5 min to model the  $P$ - $T$  relationship; possibly overestimating CP and underestimating  $W'$  (see Section 2.2). Constantini et al. (33) evaluated the effects of performing the incremental test and 3MT in a single testing session. The authors reported that a 3MT performed 20 min after the incremental test resulted in EP and WEP values similar to those obtained when the 3MR and incremental test were performed over different days (SEE 5 W and 1.81 kJ for EP and WEP, respectively). Clark et al. (30) evaluated the merits of

422 performing a 3MT on the CompuTrainer, a training ergometer often used by cyclists. The  
423 results showed a good agreement between conventional (linear work and  $T_{lim}^{-1}$  models) and  
424 3MT approaches for determining CP and EP (2.8% and 3.1%, respectively). However, a poor  
425 agreement between WEP and  $W'$  derived from the linear Work- $T_{lim}$  (CV of 24.4%) and PO-  
426  $T_{lim}^{-1}$  (CV of 26.3%) models was also reported.

427 In summary, various alternatives have been proposed to simplify the conventional 3MT.  
428 Overall, alternative approaches of the 3MT discussed above seem to produce similar EP  
429 values compared to the original 3MT. However, since WEP seems to exhibit large variation,  
430 alternative protocols to the 3MT warrant caution, and as such, the conventional approach is  
431 preferred.

432 Most of research focusing on the 3MT has been performed in healthy and athletic populations;  
433 most likely because of the challenging nature of sustaining an all-out effort for three minutes.  
434 It is nonetheless worth noting that the 3MT has been performed by adolescents (14-15 years),  
435 who might have a reduced anaerobic fitness compared to adults (7). No significant differences  
436 were observed between the conventional and 3MT approaches to estimate CP/EP and  
437  $W'$ /WEP values in adolescents; though a large variation (~20%) within-individuals prevented  
438 the 3MT and conventional approaches from being used interchangeably (6). Future research  
439 should consider whether the 3MT is a feasible option for non-athletic populations, particularly  
440 those with limited fitness.

#### 441 4.2. Critical appraisal of the 3-min all-out test

442 Other approaches have been adopted to determine CP and  $W'$  using a 3MT, which provide  
443 further insight into the validity of EP and WEP for estimation of CP and  $W'$ . For instance,  
444 several studies have investigated the 3MT using isokinetic cycling exercise. Dekerle et al. (34)  
445 reported that the isokinetic 3MT produced measures of CP and  $W'$  that were not significantly  
446 different from those derived using the traditional approach; although the large intra-subject  
447 variability, in particular for WEP, led the authors to caution against the use of the isokinetic

448 3MT. Karsten et al. (66) reported a greater EP (~7%) and smaller WEP (~25%) derived from  
449 an isokinetic 3MT than those obtained from the conventional approach, with poor levels of  
450 agreement between these two approaches. In contrast to the above, Wright et al. (119)  
451 conducted the only study to date comparing the conventional CWR with the 3MT method in  
452 both, linear and isokinetic mode, and reported that the 3MT provided a better agreement in  
453 isokinetic mode (LoA=4 ± 30 W; SEE=5%) than in linear mode (LoA=30 ± 47 W; SEE=8%).  
454 Moreover, the authors noted significant differences and low LoA between  $W'$  and WEP derived  
455 from both isokinetic mode 3MT (LoA -7 ± 9 kJ; SEE 27%), and linear-mode 3MT (LoA 9±9 kJ;  
456 SEE=26%) (119).

457 The 'gold-standard' approach to determine CP and  $W'$  is still a series of CWR in the laboratory  
458 (51,60), and therefore is the method chosen to validate the 3MT (12,96,109,110). However,  
459 while several studies have reported a close agreement between traditional and 3MT derived  
460 measures of CP and EP (12,96,109,110), others have reported that EP overestimates CP,  
461 irrespective of the mathematical model used to determine CP (9,14,84). Indeed, whilst  
462 exercise at CP can be sustained for >20 min, exercise at EP was only maintained for 12–15  
463 min (12,13,76). However, EP has demonstrated a strong positive correlation with a various  
464 thresholds, such as the lactate threshold ( $r = 0.79$ ), the maximal lactate steady state (MLSS;  
465  $r = 0.93$ ), and the onset of blood lactate accumulation ( $r = 0.85$ ) (100); and Black et al. (17)  
466 observed that performance in a 16.1 km cycling TT was strongly correlated with EP ( $r = 0.83$ ).  
467 However, the PO associated with the MLSS was 24 W (11%) (42) to 54 W (21%) (100) lower  
468 than EP. Moreover, the difference between EP and MLSS showed heteroscedasticity, as the  
469 difference between these two parameters increased in highly trained individuals (100). Indeed,  
470 the use of the 3MT has been criticised for elite cyclists as EP overestimated CP by ~50 W,  
471 and WEP underestimated  $W'$  by ~8.8 kJ (9), and the difference between actual performance  
472 and the estimated performance derived from the 3MT increases with Nonetheless, 3MT is  
473 able detect changes in CP following four weeks of high-intensity training, as both CP and EP  
474 increased by a similar ( $r = 0.77$ ) magnitude, and the agreement between CP and EP was

475 good, pre- and post-training (typical error 4.6 W and 4.3 W, respectively) (111). Furthermore,  
476 Clark et al. (32) demonstrated that a 3MT is able to detect fatigue-induced changes in EP and  
477 WEP during prolonged cycling. These authors found that 2 hours of heavy exercise causes a  
478 decrease of 8% and 20% for CP and  $W'$ , respectively, suggesting EP and WEP may be able  
479 to assess fatigue. In summary, although 3MT may offer a time-efficient approach to estimate  
480 CP and  $W'$  and an ability to monitor training adaptations and fatigue, these studies suggest  
481 that a degree of caution is warranted when assuming that EP and WEP represent CP and  $W'$ ,  
482 respectively, particularly in elite athletes.

## 483 **5. Conclusions**

484 The non-linear  $P$ - $T$  relationship is well described by a hyperbolic function, which results in two  
485 parameters: the asymptote (CP), and the curvature constant ( $W'$ ). Conventionally, several  
486 CWR to task-failure are required to determine CP and  $W'$ , using various modelling techniques.  
487 However, the mathematical model used, and the characteristics of the exhaustive trials such  
488 as duration, rest between trials, and mode (TT vs. CWR) have been shown to affect CP and  
489  $W'$  estimations. It is recommended that CP and  $W'$  should be determined using the the two-  
490 parameter model that results in the lowest SEE. Regarding the exhaustive trials, a minimum  
491 of three CWR or TT is recommended with a duration spanning 2 min to 15 min. Trials which  
492 fall outside of this time range should not be used to estimate CP and  $W'$ , and the attainment  
493 of  $\dot{V}O_{2max}$  should be verified where possible. Moreover, if the individual SEE exceeds 2-5% for  
494 CP and/or 10% for  $W'$ , further trials should be included in the calculation. Whilst recovery  
495 between exercise bouts of  $\geq 60$  mins appears to be sufficient to avoid  $\dot{V}O_2$  priming effects, the  
496 inability to determine  $W'$  suggests that at present 24 h recovery periods between trials are  
497 best. The use of TT has recently been used to determine the  $P$ - $T$  relationship from the field.  
498 Although there are a number of factors that might confound laboratory- vs. field-based tests,  
499 such as seating positions, acceleration and inertia, air resistance, or differences in terrain; field  
500 tests seem to provide similar CP values than those established in the laboratory whilst also  
501 offering an ecologically valid and practical approach to determine CP and  $W'$ . Field-based

502 tests can be integrated into daily training, which in turn reduces the need for laboratory access  
503 and equipment. Similarly, CP testing in the laboratory can now be performed using TT.  
504 However, whilst this testing method provides highly reliable results for both parameters, it still  
505 requires further research to investigate validity of  $W'$  values. The 3MT allows the determination  
506 of EP and WEP, which are considered to represent CP and  $W'$ , respectively. Although a good  
507 agreement between estimates of CP and  $W'$  derived from the conventional approach and 3MT  
508 has been used to validate the latter; recent research suggests that EP may overestimate CP,  
509 especially in elite athletes. The original 3MT requires repeated laboratory visits: an initial GXT  
510 to determine gas exchange threshold and  $\dot{V}O_{2max}$ , and a subsequent visit to perform the actual  
511 3MT. A number of alternatives have been proposed to further reduce the protocol to a single-  
512 day test. Though some of these alternatives have shown good agreement between methods,  
513 further research should also investigate the physiological responses at EP, determined from  
514 these alternatives 3MT protocols. The recommendations given in the current review should  
515 be applied to cycling, but, where possible, might be extended to other modes of exercise, such  
516 as running, swimming, rowing, or kayaking.

517

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818 **7. Tables and Figures**

819 **Table 1.** Example of data collected from five constant-work rate bouts to task-failure in a trained  
820 cyclist. Power and Duration are recorded during the test, and work and Time<sup>-1</sup> subsequently  
821 calculated. 'Max' represents peak power output.

822

Trial	Power (W)	Duration (s)	Work (kJ)	Time <sup>-1</sup> (s <sup>-1</sup> )
1	415	135	56.03	0.0074
2	360	240	86.40	0.0042
3	340	408	138.72	0.0025
4	320	600	192.00	0.0017
5	310	930	288.30	0.0011
Max	1100			

823

824 **Figure Legends**

825

826 **Figure 1.** Different modelling approaches to determine critical power and the curvature constant  
827  $W'$  from data presented in Table 1. Panel A represents the 2-parameter hyperbolic power-duration  
828 relationship. Panel B represents the 3-parameter hyperbolic power-duration relationship. Panel C  
829 represents the 2-parameter linear work- $T_{lim}$  relationship. Panel D represents the 2-parameter linear  
830 power output-  $T_{lim}^{-1}$  relationship.  $T_{lim}$  represent duration until task-failure.

831

832 **Figure 2.** The effect of the different mathematical modelling approaches to determine critical power  
833 and  $W'$  on the relationship between power output and time to task-failure. Data from Table 1.

834

835 **Figure 3.** The effect of the duration of the trial on critical power (CP) and  $W'$ . Data from Table 1.

836

837 **Figure 4.** Outline of the 3-min all-out test. Panel A represents data from 30 seconds before the  
838 start of the test (start at time = 0 s). Panel B represents 30-seconds averages through the test.  
839 Filled circles (●) denote power output, and open circles (○) represent oxygen consumption ( $\dot{V}O_2$ ).  
840 Note that power output initially increases, reaching a peak in the first few seconds of the test, and  
841 then progressively decreases until, eventually levels off in the final 30 s of the test (i.e. end-test  
842 power output).

843