

## Optimal Fractional-Order PI Control Design for a Variable Speed PMSG-Based Wind Turbine



Sarir Noureddine<sup>1\*</sup>, Sebaa Morsli<sup>1</sup>, Allaoui Tayeb<sup>1</sup>, Denai Mouloud<sup>2</sup>

<sup>1</sup> Department of Electrical Engineering, University of Tiaret, City of Tiaret 14023, Algeria

<sup>2</sup> Department of Engineering and Technology, University of Hertfordshire, City of Hatfield 19440, United of Kingdom

Corresponding Author Email: [noureddine.sarir@univ-tiaret.dz](mailto:noureddine.sarir@univ-tiaret.dz)

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### ABSTRACT

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wind turbine, MPPT, fractional order PI controller, PSO, GA

This paper focusses on the design of optimal control strategies for a variable-speed wind energy system based on Permanent Magnet Synchronous Generator (PMSG). The fractional order PI controller, denoted  $PI^\lambda$ , is an extension of the classical PI controller, which provides greater flexibility, better performance and robustness, however the tuning of the controller parameters is challenging. In this work, Particle Swarm Optimization (PSO) and Genetic Algorithm (GA) provide approximate solutions to various problems and form a good optimization. In our system, they are used to have the PI regulator parameters and tune the parameters of the proposed controllers. The proposed controllers have been applied as maximum power point (MPPT) controllers for the wind turbine and to regulate the PMGS currents under variable weather conditions and. The results show that, among all these controllers, the fractional order PI controller optimized by the PSO leads to better performance in terms of the transient response characteristics such overshoot, rise time and settling time.

## 1. INTRODUCTION

In recent years, the world is experiencing a shift towards the adoption of alternative, cheaper and cleaner energy sources [1]. This is driven by the rapid decline of global reserves of conventional energy resources and the potential threats fossil fuels are causing to the environment such as pollution and global warming [2]. With the global population growth and industrialization on the rise, the demand for electrical energy has witnessed unprecedented level across the globe, which is expected to increase further in the decades ahead.

Nowadays, wind energy is one of the most important renewable energy sources (RESs), which can be used not only as standalone systems to supply electricity to isolated areas but can also be integrated to the utility grid [3]. Wind energy is a pollution-free and inexhaustible source. Therefore, a wind energy generation system could be one of the potential sources of alternative energy for the future [4]. Wind generation systems can be installed close to areas where electricity demand is high for supplying local loads or deployed as wind farms either inland or offshore to supply large power capacity to support the electricity grid.

Wind Energy Conversion Systems (WECSs) generally comprise of a wind turbine, generator, power converter and their controllers [5]. In our project, we are interested in the permanent synchronous generator which is forms an important role as a main component of wind turbine, they are commonly used to convert the mechanical power output of steam turbines, gas turbines, reciprocating engines, and hydro turbines into electrical power for the grid [6], while Permanent magnet synchronous motors are the most widely used steady-state 3-phase AC motors, which convert electrical energy into mechanical energy. WECS are continuously subjected to

various disturbances such as atmospheric conditions which cause variations in the wind speed. WECS are generally designed to extract maximum power from the wind under different conditions by controlling the current and voltage of the wind generator [7-9]. Several control schemes have been proposed in the literature to improve the performance of the generator and enhance the efficiency of WECS. Proportional-Integral (PI) controllers are simple to implement and can achieve a good transient and steady state response with small overshoot and short settling-time and have been widely used in industrial processes [10, 11]. However, these classical controllers may not be very effective for systems exhibiting nonlinearities and parameter variations.

Many real-world physical systems are modeled by fractional-order differential equations, that is, equations involving non integer-order integrals such as dynamic systems characterized by memory and hereditary effects [12]. In recent years, fractional calculus has been applied to the modeling and control of various types of physical systems, and this is well documented in many control theories and applications literature. The concept of fractional-order control has been used to design PI like controllers with enhanced robustness and improved performance than the classical PI controllers.

The so-called Fractional-Order PI controller (FOPI), besides the proportional ( $K_p$ ) and integral ( $K_i$ ) gains, has an additional parameter termed the fractional integration order denoted by  $\lambda$ . Therefore, the FOPI has three tuning parameters which make it more flexible [13]. There are several powerful optimization methods which can be employed to determine the optimal set of parameters for the FOPI. In this paper, the PSO (Particle Swarm Optimization) and GA (Genetic Algorithm) methods are used to optimize the parameters of the classical PI and FOPI controllers [14-16]. The new task in our work is



$$G_s(s) = \frac{1}{ls + R} = \frac{i_{d,q}(s)}{V_{d,q}(s) + E_{d,q}(s)} \quad (5)$$

where,  $E_{d,q} = \pm \omega_e \phi_f$  are decoupling terms and considered as perturbations. The control loops of the current  $i_d$  and  $i_q$  are shown in Figure 3 by the block diagram.

### 3. FRACTIONAL PI CONTROLLER

In fractional-order calculus, the fundamental differ-integration operator  $aD_t^\alpha$  (where  $a$  and  $t$  are the limits of the operation) is defined as [23]:

$$aD_t^\alpha = \begin{cases} \frac{d^\alpha}{dt} & \alpha > 0 \\ 1 & \alpha = 0 \\ \int_a^t dt^\alpha & \alpha < 0 \end{cases} \quad (6)$$

where,  $\alpha$  is the order of the operation, generally  $\alpha \in \mathbb{R}$  but  $\alpha$  could also be a complex number. Fractional calculus has a larger range than integer order derivative. If a fractional order is used instead of the integer order in the derivative or integral, then a fractional calculus must be used to solve this fractional derivative and integral [24]. The generalized fractional differentiation and integration has mainly three definitions, the Grunwald-Letnikov (G-L) definition and the Riemann-Liouville (R-L) definition and the Caputo definition [25].

Grunwald-Letnikov's definition is perhaps the best known one due to its suitability for the design of discrete control algorithms. The  $m$  order fractional derivative of a continuous function  $f(t)$  is given by [26]:

$$aD_t^\alpha f(t) = \lim_{h \rightarrow 0} \frac{1}{h^\alpha} \sum_{j=0}^{\lfloor \frac{t-a}{h} \rfloor} (-1)^j \binom{\alpha}{j} f(t - jh) \quad (7)$$

In Eq. (7),  $\lfloor \frac{t-a}{h} \rfloor$  truncates  $\frac{t-a}{h}$  to an integer. To determine a fractional-order transfer function, consider a linear time-invariant fractional model of a system with input  $u$  and output  $y$  takes the following form [27]:

$$\begin{aligned} a_n D^{\lambda_n} y(t) + a_{n-1} D^{\lambda_{n-1}} y(t) + \dots + a_0 D^{\lambda_0} y(t) = \\ b_m D^{\mu_m} u(t) + b_{m-1} D^{\mu_{m-1}} u(t) + \dots + b_0 D^{\mu_0} u(t) \end{aligned} \quad (8)$$

where,  $a_i, \lambda_i$  ( $i = 0, 1, \dots, n$ ),  $b_k, \mu_k$  ( $k = 0, 1, \dots, m$ ), are real constants,  $n$  and  $m$  are positive integers. The Laplace transform of the fractional derivative of  $f(t)$  for zero conditions given by:

$$L(aD_t^\alpha f(t)) = S^\alpha f(t) \quad (9)$$

Therefore, the Laplace transform on both sides of Eq. (10) for zero initial conditions leads to the following transfer function:

$$\frac{Y(s)}{U(s)} = \frac{b_m D^{\mu_m} + b_{m-1} D^{\mu_{m-1}} + \dots + b_0 D^{\mu_0}}{a_n D^{\lambda_n} + a_{n-1} D^{\lambda_{n-1}} + \dots + a_0 D^{\lambda_0}} \quad (10)$$

These concepts can be employed to design fractional order controllers such as fractional order PI controller (FOPI). FOPI exhibits excellent performance and robustness and has been successfully employed in several applications. FOPI has an additional tuning parameter as compared to the classical PI controller which provides more flexibility in the design [28]. The continuous transfer function of FOPI is obtained through Laplace transform is given by:

$$G_s(s) = K_p + K_i s^{-\lambda} \quad (11)$$

### 4. OPTIMIZATION OF PI AND FOPI PARAMETERS USING PSO AND GA ALGORITHMS

The selection of appropriate gains,  $K_p, K_i$  for the PI controller and  $K_p, K_i, \lambda$  for the FOPI controller which is tuned according to the system specifications and which satisfies the robustness of closed loop performance over a wide frequency range is the main objective of the PI controller optimizer. Figure 5 shows the structure of the PI and FOPI controllers optimization process. PSO and GA are used to adjust parameters of PI and FOPI controllers repeatedly until they reach a satisfactory performance level.

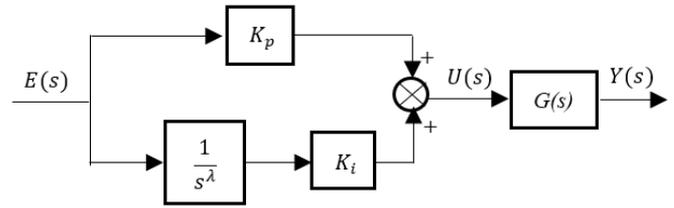


Figure 4. Block diagram of fractional order PI controller (PI<sup>λ</sup>)

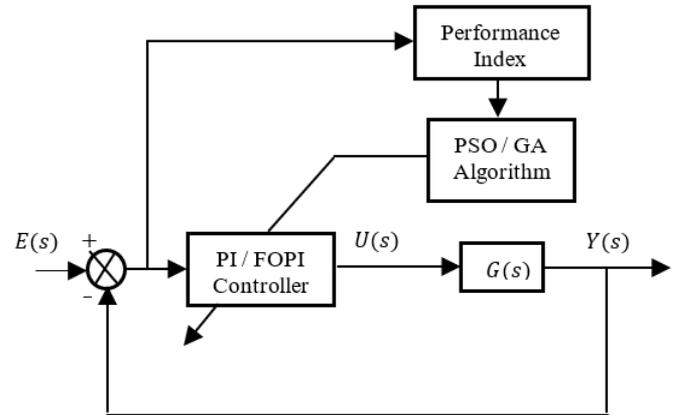


Figure 5. Block diagram of PI and FOPI tuning

$G(s)$  represents the transfer function of the turbine  $G_1(s)$  and the PMSG  $G_2(s)$ , they are given from Figure 2 and Figure 4 respectively by:

$$\begin{cases} G_1(s) = \frac{1}{Js + f} \\ G_2(s) = \frac{1}{ls + R} \end{cases} \quad (12)$$

## 4.1 Overview of heuristic optimization

### 4.1.1 Particle Swarm Optimization (PSO)

Particle Swarm Optimization (PSO) technique, proposed by Kennedy and Eberhart in 1995 is an evolutionary-type global optimization technique developed due to the inspiration of social activities in flock of birds and school of fish and is widely applied in various engineering problems due to its high computational efficiency. It has been proven that PSO is simple and robust against nonlinearity, non-differentiability and high dimensionality.

The advantages of PSO compared to other optimization techniques are as follow: easy implementation, few parameters to be adjusted and no gradient information is required [29]. Each particle generated by the PSO algorithm has the potential to be the best solution for the problem. At the beginning, each particle of the population is distributed randomly through the search space. The velocity and position are updated by the following two best values. The best value achieved for each particle is the best solution which is called personal best (*pbest*) and the best value achieved so far among all particles is called 6 global best (*gbest*). The modified velocity of each particle can be calculated via the present velocity and distance form (*pbest*) and (*gbest*) as shown in following equation:

$$V_i^{t+1} = wV_i^t + c_1R_1(p_{pbest}^t - X_i^t) + c_2R_2(g_{gbest}^t - X_i^t) \quad (13)$$

The new position is then determined by the sum of the previous position and the new velocity:

$$X_i^{t+1} = X_i^t + V_i^t \quad (14)$$

where, *c1* and *c2* are acceleration constants, *R1* and *R2* represent random values in the range [0 1],  $V_i^t$  and  $X_i^t$  denote the velocity and position of the  $i^{th}$  particle at iteration *t*, *w* is inertia weight factor, (*pbest*) are the best position for each particle, (*gbest*) are the global best value of the group. A detailed flowchart of PSO considering the above steps is shown in Figure 6.

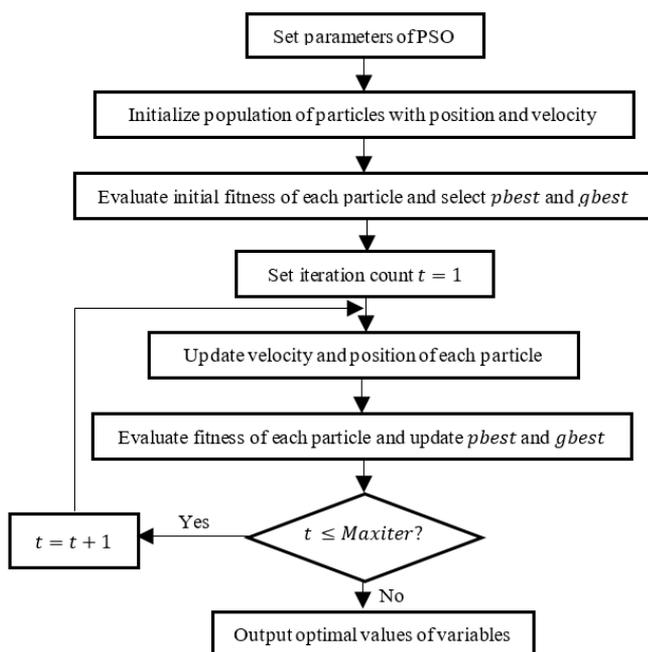


Figure 6. Flowchart of PSO

### 4.1.2 Genetic Algorithm (GA)

Genetic Algorithm (GA) is a stochastic optimization algorithm that mimics the process of natural evolution and which are developed based on the Darwinian theory of “survival of fittest”. GA has three basic operators: selection, crossover and mutation. It has been recognized as an effective and efficient technique to solve optimization problems [29]. Figure 7 shows flowchart of GA.

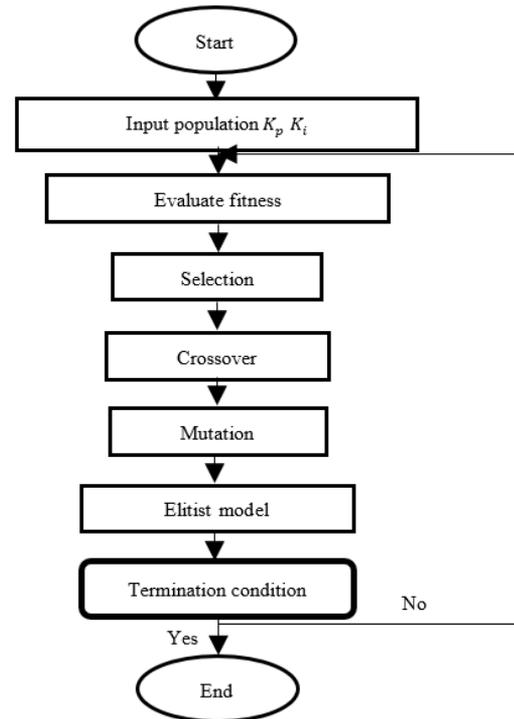


Figure 7. Flowchart of GA

We can cite the advantages and disadvantages of PSO and GA algorithms in the following Table 1:

Table 1. The advantages and disadvantages of PSO and GA algorithms

Advantages	disadvantages
<ul style="list-style-type: none"> <li>- They are easy to implements and there are few parameters to adjust.</li> <li>- have already been a new and fast developing research topic</li> </ul>	<ul style="list-style-type: none"> <li>-Despite the simplicity and ease of use of the PSO and GA algorithms it presents a risk of divergence or rapid convergence which allows to stagnate in a local optimum, therefore several improvements have been made to the base algorithm</li> </ul>

## 4.2 Performance indices

Table 2. Performance indices

Performance index	Definition
Integral of Square Error (ISE)	$\int_0^{tss} e^2(t)dt$
Integral of Absolute Error (IAE)	$\int_0^{tss}  e(t) dt$
Integral of Time Absolute Error (ITAE)	$\int_0^{tss} t e(t) dt$
Integral of Time Square Error (ITSE)	$\int_0^{tss} te^2(t)dt$

The performance index is defined as a quantitative measure to describe the performance of the designed PI controller system. The goal of optimization based on PSO and GA is to find a set of parameters  $K_p$ ,  $K_i$  and  $\lambda$  such that the feedback control system that minimizes the performance index [30]. There are four commonly used indices to describe system performance are listed in Table 2 [31].  $t_{ss}$  is total simulation time and we his tacked 01 second with a step  $t_{ss}=0.01$ second.

For the fractional PI and  $PI^\lambda$  tuning based on PSO and GA, the ITAE performance index produced the best result over the other indices and it will be used as an objective function. Note: interval chosen to determine the best performance index among the four is ranges from [0 0] to [1000 1000].

### 5. SIMULATION RESULTS AND DISCUSSION

The PSO and GA parameters used in the simulation are given in Tables 3 and 4 in the Appendix. PSO and GA optimization algorithms have been tested using the performance indices given Table 2, and the results are summarized in Tables 5 and 6.

**Table 3.** PSO parameters

Parameters	Values
Population size	49
Number of iterations	50
Number of variables	$2(K_p, K_i)$ and $3(K_p, K_i, \lambda)$
Inertia weight w	0.9
Acceleration constant $c1, c2$	2
Range of variables $(K_p, K_i, \lambda)$	[200 200] and [200 200 1]

**Table 4.** GA parameters

Parameters	Values
Population size	50
Number of variables	$2(K_p, K_i)$ and $3(K_p, K_i, \lambda)$
Range of variables $(K_p, K_i, \lambda)$	[200 200] and [200 200 1]
Generation	100
Crossover	Single point
Mutation	0.01
Encoding	Binary

**Table 5.** PI parameters optimization for transfer function  $G_1(s)$

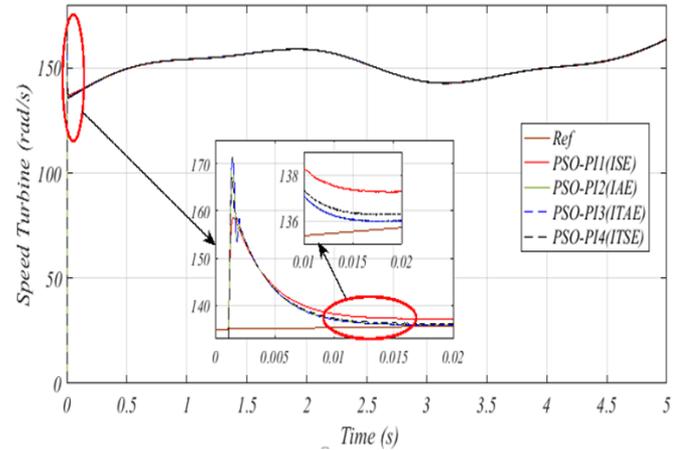
Tuning method	$K_p$	$K_i$	Best fitness	iteration
GA-PI1 (ISE)	3.494	900.554	-0.4707	73
GA-PI2 (IAE)	979.423	998.552	0.0118	51
GA-PI3 (ITAE)	1.85	957.365	8.1873e-7	51
GA-PI4 (ITSE)	1.157	524.559	-0.4961	54

**Table 6.** PI parameters optimization for transfer function  $G_2(s)$

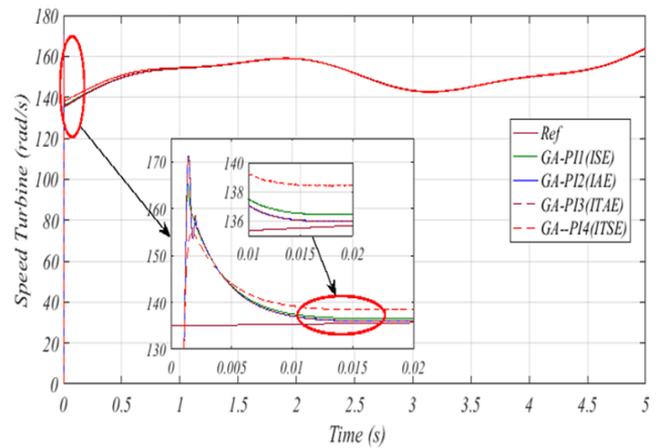
Tuning method	$K_p$	$K_i$	Best fitness	iteration
PSO-PI1 (ISE)	0	673.2058	-0.8300	73
PSO-PI2 (IAE)	1000	1000	0.0118	51
PSO-PI3 (ITAE)	0	662.5512	9.3902e-06	51
PSO-PI4 (ITSE)	0	847.1597	-0.4872	54

From Figures 8 and 9, it can be seen that the ITAE performance index gives better optimization results compared

to other indices and it will subsequently used in the rest of the paper for the comparison of the proposed controllers. A detailed comparative study between PI and FOPI optimized by PSO, and PI and FOPI optimized by GA is performed to determine best control approach for our wind energy system. The results are presented in Figures 10-13.

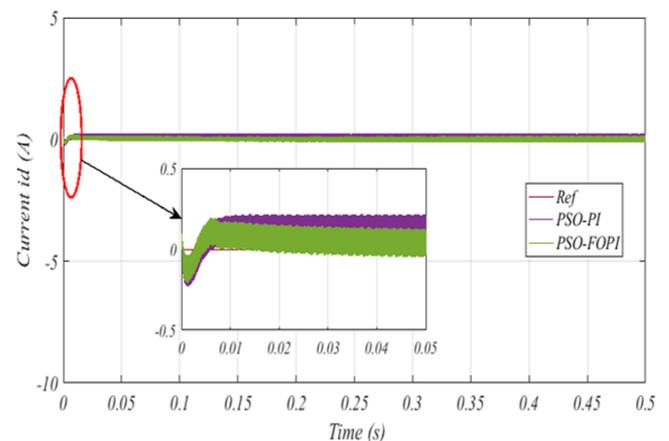


**Figure 8.** Speed turbine response for ISE, IAE, ITAE and ITSE using PSO

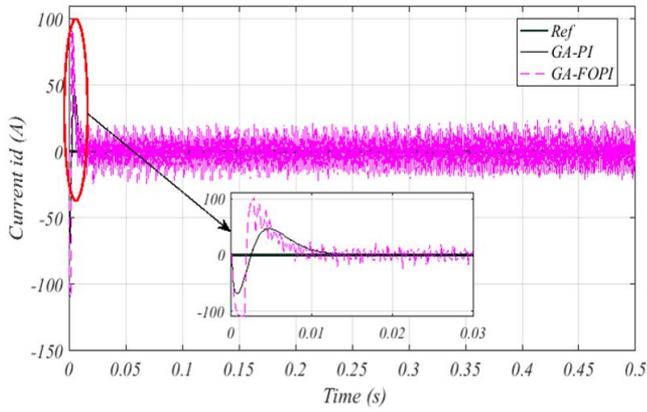


**Figure 9.** Speed turbine response for ISE, IAE, ITAE and ITSE using GA

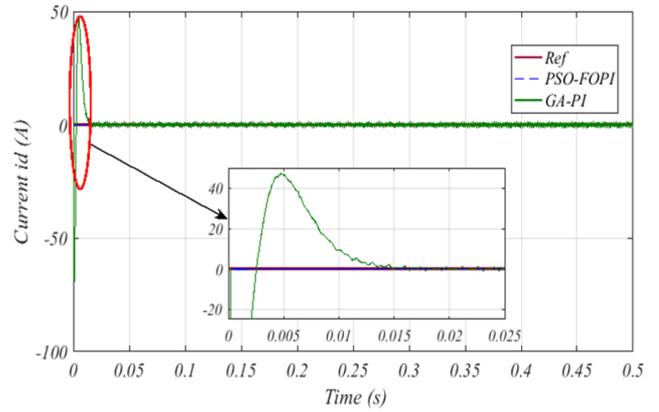
**Note:** the controllers are applied to adjust the currents  $i_d$  and  $i_q$  of the PMGS.



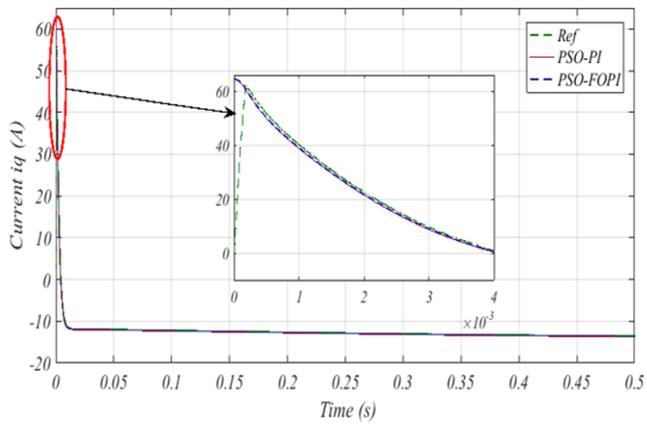
**Figure 10.** Response of the current  $i_d$  with PI and FOPI optimized using PSO



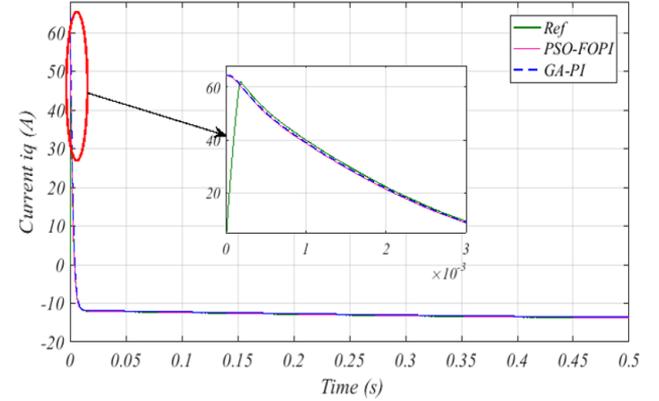
**Figure 11.** Response of the current  $i_d$  with PI and FOPI optimized using GA



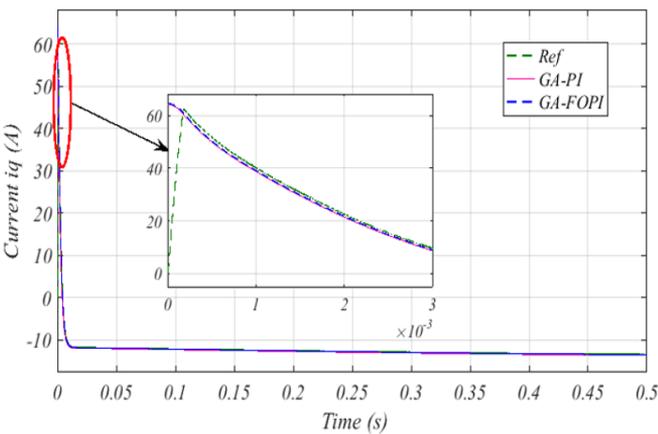
**Figure 14.** Response of the current  $i_d$  with PI and FOPI optimized using PSO and GA



**Figure 12.** Response of the current  $i_q$  with PI and FOPI optimized using PSO



**Figure 15.** Response of the current  $i_q$  with PI and FOPI optimized using PSO and GA



**Figure 13.** Response of the current  $i_q$  with PI and FOPI optimized using GA

From Figures 10, 11, 12 and 13, it can be noticed that FOPI optimized by the PSO gives better performance compared to the PI optimized by the PSO while FOPI optimized by GA leads to a poor performance compared to the optimized PI by GA.

Finally, a comparative study between PSO-FOPI and GA-PI is undertaken to determine the best controller among all the proposed controllers. The results are presented in Figures 14 and 15. To confirm all the results of the simulation for all figures, Tables 7 and 8 shows the parameters of PI and FOPI regulators and performance of the two algorithms PSO and GA.

## 6. CONCLUSION

This paper proposed the control of a wind energy conversion system using PI and fractional-order PI (FOPI) optimized using generic algorithm (GA) and particle swarm optimization (PSO) techniques. Four controllers have been evaluated with different performance indices ITAE, IAE, ISE and ITSE for the optimal tuning of the maximum power point (MPPT) of the wind turbine and the regulation of the currents of the permanent magnet synchronous generator (PMSG). The ITAE method gave better results. The designed controllers have been compared based on a set of time domain and frequency domain criteria including overshoot, rise time and settling time. The results obtained have showed that the fractional order PI controller optimized by the PSO leads to better performance in terms of the transient response characteristics. For example, the error bar of GA for FOPI is 0.00356 while the error of PSO for FOPI is 3.0789e-04. The Tables 7, 8 and Figures 14, 15 show the differences between the two algorithms.

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## APPENDIX

Tables 7 and 8 show a comparative study in terms of the dynamic and robustness of the PSO and GA controls for both PI and FOPI regulators. The +, - and 0 signs are used to measure the performance of each command.

- ++: very good performance
- +: good performance
- 0: average performance
- : poor performance
- : very poor performance

**Table 7.** Comparison between PSO and GA methods for PI controller

Methods	Transfer function	Dynamic	Robustness	Rapidity	$K_p$	$K_i$	Best fitness
PSO	G1(s)	+	+	+	133.6583167.2180	1.4855e-09	
	G2(s)	+	+	+	200	200	0.0038
GA	G1(s)	0	0	0	115.413	144.266	7.3066e-15
	G2(s)	0	0	0	133.6583167.2180	1.5512e-4	

**Table 8.** Comparison between PSO and GA methods for FOPI controller

Methods	Transfer function	Dynamic	Robustness	Rapidity	$K_p$	$K_i$	$\lambda$	Best fitness
PSO	G1(s)	++	++	++	159.9851	200	1	5.0163e-08
	G2(s)	++	++	++	0	200	1	3.0789e-04
GA	G1(s)	+	+	+	147.346	184.191	1	5.4366e-8
	G2(s)	+	+	+	200	200	0.394	0.00356