



Article

Thermal Effect of Cylindrical Heat Sink on Heat Management in LED Applications

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Abstract: Light Emitting Diode (LED) applications are increasingly used in various microelectronic devices due to their efficient light generation. The miniaturisation of the LED and its integration into compact devices within the weight limit have resulted in excessive heat generation, and inefficient management of this heat could lead to the failure of the entire system. Passive and/or active heat sinks are used for dissipating heat from the system to the environment to improve performance. An ANSYS design modeller and transient thermal conditions were utilised in this study to design and simulate the LED system. The modeller performs its function by utilising the Finite Element Method (FEM) technique. The LED system considered in this work consists of a chip, thermal interface material, and a cylindrical heat sink. The thickness of the Cylindrical Heat Sink (CHS) fins used in the investigation is between 2 mm and 6 mm, whilst ensuring the mass of heat sinks is not more than 100 g. The input power of the LED chip is between 4.55 W and 25.75 W, as required by some original equipment manufacturers (OEMs). A mesh dependency study was carried out to ensure the results were synonymous with what can be obtained practically. The simulation results suggest that the power ratings did not affect the thermal resistance of the CHS. In addition, the thermal resistance increased with the increased thickness of the CHS fin. The efficiencies of the heat sink were found to increase with an increased thickness of the cylindrical fin and the accuracy between the calculated and simulated thermal efficiency ranges from 84.33% to 98.80%. Evidently, the CHS fin of 6 mm thickness is more efficient than the other CHS fins, as depicted in this study.

Keywords: LED; cylindrical heat sink; heat management; transient condition; thermal analysis

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1. Introduction

Light Emitting Diodes (LEDs) convert electrical energy directly into light and deliver efficient light generation with little waste of electricity in comparison to conventional light sources such as the incandescent and halogen lamps that first convert electrical energy into heat, and then into light [1]. LEDs are increasingly used in domestic and industrial lighting systems, including in lamps for indoor and outdoor use [1]. These LEDs generate heat during operation, and if not properly managed, this heat may lead to performance deterioration and the shortened life of the device [2]. Costa and Lopes [3] suggested an improved radial heat sink for LED lamp cooling for the purpose of increasing the life span of such devices. The failure of devices can be attributed to the accumulation of excess heat in the system. To avoid failure in such devices, heat sinks are introduced. The application of heat sinks with different configurations has been utilised to improve the life of LED applications [4]. Barbosa et al. [5] used a heat sink as the passive heat dissipation device when the design optimisation of a high-powered LED matrix luminaire was investigated, whilst Tang et al. [6] developed an integrated heat sink with a vapour chamber for the thermal management of high-powered LEDs. Typically, heat sinks dispel the heat from

the LED device to the environment using the methods of conduction, convection, and radiation. The conduction technique is the most preferred, with the heat sink bonded to the LED chip/chips using Thermal Interface Materials (TIMs), whilst the convection method to dissipate heat occurs between the heat sink and the environment.

Numerical and computational methods have been used to analyse heat sinks (heat sink fins) in microelectronic applications. Sobamobo et al. [7] investigated the impact of Lorentz force on the thermal behaviour of a convective–radiative porous fin using the differential transformation method. Their findings suggested that increases in the magnetic field, porosity, convective, and radiative parameters increase the rate of heat transfer from the fin and consequently the efficiency of the fin is improved. In the analysis conducted by Ekpu [8], ANSYS was used to study the effect of fin arrangement on thermal performance in microelectronic devices and the numerical results were satisfactory. Staliulionis et al. [9] used COMSOL to investigate heat sink efficiency for electronic component cooling applications. Arshad et al. [10], who studied the thermal transmission comparison of nano-fluids over a stretching surface under the influence of a magnetic field, used MATLAB for their analysis. This method of analysis has reduced the costs of experimental work by researchers. However, the need to verify the simulation results with practical work cannot be overemphasised. Considering the study by Ranjith et al. [11], it seems that the heat transfer features of LED modules using passive heat sinks have some advantages such as energy efficiency, performance, versatility, and prolonged life. Furthermore, it was stated that LEDs could only convert about 20–30% of the power supplied to the chip, leaving about 70–80% of the energy being converted into heat that must be dissipated from the system.

The study by Mjallal et al. [12] discussed ways of using Phase Change Materials (PCMs) to improve electronic device heat sinks' cooling efficiency. They stated that PCM-based heat sinks could efficiently absorb the heat generated by the electronic device, thereby delaying the peak temperature of the device. This absorbed energy is later released when the device is turned off. In their research, two PCMs, salt hydrate and wax, were compared with a heat sink without a PCM. It was inferred that using PCMs will delay the device from reaching its peak temperature by a couple of minutes (approximately 42 min, compared to 10 min for heat sinks without PCM) for a heat flux input of 1250 W/m². The studies carried out by Salah and Hamida, [13] also adduced a similar pattern and substantiated the finding of Mjallal et al. [12].

In another study by Chu et al. [14] using the LED desk lamp to develop a new heat sink design, they used both simulation and experiment to analyse four different heat sink designs with fins in transverse or longitudinal directions and with or without vents on the heat sink base. Their analysis revealed only about a 4% difference between the experimental and simulation results. However, the researchers adopted a design with 12 vents on both sides of the heat sink base to create a chimney effect through natural convection. The temperature of the LED desk lamp was reduced by about 5 °C based on the novel heat sink design. Based on the material used for the prototype heat sink, the weight of the LED desk lamp and the overall production costs were significantly reduced.

The thermal performance of LED array heat sink using simulation and experimental validation was investigated in [15]. The design and thermal analysis were conducted using natural convection conditions. Their findings suggested that when the number of heat sink fins increased, the thermal resistance and the convection heat transfer coefficient decreased accordingly. Likewise, increasing the height of the heat sink fins reduces the convective heat transfer coefficient and thermal resistance. However, the study indicated that the input power and inlet air could increase the convective heat transfer coefficient and decrease the thermal resistance. A comparison of the experimental and the numerical simulation results suggested that the developed mathematical model could be used to predict the thermal characteristics of LED array heat sinks.

In other applications, such as thermal plants and automobile industries, heat exchangers and radiators are used for energy recovery and heat dissipation. The study conducted by

Jamil et al. [16] on energy recovery systems using offset strip-fin compact heat exchangers suggested that the geometry of the fins and fluid velocity are the most critical parameters in managing heat. In another study, the thermal–hydraulic characteristics of gasketed plate heat exchangers as a preheater for thermal desalination systems were investigated [17]. The findings suggest that salinity does not affect the performance of heat exchangers, but fouling resistance is critical to the overall design parameters and cost.

In this study, an improved approach to the thermal management of the heat generated by LED applications is presented involving different combinations of cylindrical heat sink designs. In addition, different power ratings of the LED chips were used in the analysis of the cylindrical heat sinks. The findings from this study are of significance to developing new thermal management solutions for differently rated power LED applications.

2. Materials and Methods

2.1. Description of Model

The model considered in this study is surface mounted, and the assembly comprises the LED chip, thermal interface material, and a cylindrical heat sink. The dimension of the LED chip is 10 mm × 10 mm × 0.5 mm, and the thermal interface material is 10 mm × 10 mm × 0.035 mm. The heat sink is 50 mm × 50 mm × 20 mm. The base thickness is 5 mm, the fin height is 15 mm, and the fin thickness varies from 2 mm to 6 mm with an increment interval of 1 mm. However, the diameter of the fin varied according to the thickness of the fin, whilst the number of cylindrical fins changed according to the thickness of the fins. A schematic diagram of the assembled model is shown in Figure 1a, whilst Figure 1b is showing the expanded view of the silicon chip, the TIM, and the base of the heat sink.

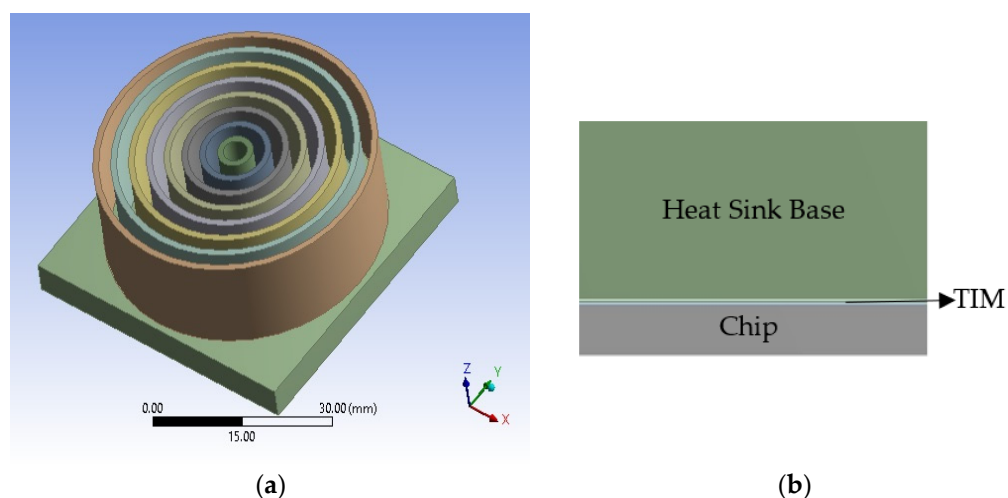


Figure 1. (a) Geometry of the developed model (b) Expanded view showing components.

2.2. Materials

The heat sink used in this study is aluminium, the LED chip is silicon, and the thermal interface material is Sn-Ag-Cu (SAC 405) [18]. The properties of the materials used in the simulation work are presented in Table 1. Based on the information presented in Table 1, the mass of the different cylindrical heat sinks designed could be calculated. It is practical evidence that the density of an object is given as:

$$\rho = \frac{M}{V} \quad (1)$$

$$M = \rho V \quad (2)$$

where ρ is the density, M is the mass, and V the volume; Table 2 presents the mass for each of the designed cylindrical heat sinks.

Table 1. Properties of materials [4,19].

Material	Density (kg/m ³)	Thermal Conductivity (W/mK)	Specific Heat (J/kgK)
Aluminium	2689	237.5	951
Silicon	2330	148	712
SAC 405	7440	62	236

Table 2. Mass of different cylindrical heat sinks.

Heat Sink Fin Thickness (mm)	Number of Fins	Density (kg/m ³)	Volume of Heat Sink (mm ³)	Mass of Heat Sink (g)
2	8	2689	22,301.69	59.97
3	7	2689	25,117.48	67.54
4	6	2689	27,202.69	73.15
5	5	2689	28,698.9	77.17
6	5	2689	30,171.46	81.13

Note: The volume (12,500 mm³) of the heat sink base is added to the volume of the heat sink.

2.3. Load and Boundary Conditions

In this study, transient thermal analysis is used to evaluate the thermal characteristics of the different cylindrical heat sinks. The ambient temperature used for the simulation is 22 °C (the temperature is within the range practically acceptable). A natural convection coefficient (20 W/m²K) was applied to the surface of the heat sink. The power supplied through the LED chip is as follows: 4.55 W, 9.7 W, 15.03 W, 20.6 W, and 25.75 W, respectively. The simulation time was set at 3600 s (this time is enough for the heat sink to reach steady state temperature), whilst the simulation step increase was determined automatically by the ANSYS simulation machine after the initial start time, number of steps, and end time were specified. In fact, ANSYS Workbench has the capacity to determine the solver steps to ensure the solution converges. However, if the solution does not converge within the specified conditions, it will flag the results obtained to be checked and settings updated.

Governing Equation

The conduction and convection conditions with the radiation method are assumed negligible and neglected. The heat convection condition is a three-dimensional and incompressible fluid. The fluid in this study is air, which is used for the momentum equation, whilst the density is temperature dependent. The governing simulation equations followed in this study are given as [14,15]:

$$\frac{\partial(\rho u)}{\partial x} + \frac{\partial(\rho v)}{\partial y} + \frac{\partial(\rho w)}{\partial z} = 0. \quad (3)$$

Equation (3) represents the continuity equation and the momentum equations for directions x , y , and z are given in Equations (4)–(6), respectively:

$$u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} + w \frac{\partial u}{\partial z} = -\frac{1}{\rho} \frac{\partial P}{\partial x} + \nu \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2} \quad (4)$$

$$u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} + w \frac{\partial v}{\partial z} = -\frac{1}{\rho} \frac{\partial P}{\partial y} + \nu \frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} + \frac{\partial^2 v}{\partial z^2} \quad (5)$$

$$u \frac{\partial w}{\partial x} + v \frac{\partial w}{\partial y} + w \frac{\partial w}{\partial z} = -\frac{1}{\rho} \frac{\partial P}{\partial z} + \nu \frac{\partial^2 w}{\partial x^2} + \frac{\partial^2 w}{\partial y^2} + \frac{\partial^2 w}{\partial z^2} + g\beta(T - T_\infty) \quad (6)$$

The conservation of energy equation for the three-dimensional space is given as:

$$\rho C_p \frac{\partial T}{\partial t} = k \left(\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2} \right) + Q. \quad (7)$$

Equation (7) applies to the subdomains (chip, thermal interface, and heat sink). The working fluid energy equation is given as:

$$u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} + w \frac{\partial T}{\partial z} = \alpha \left(\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2} \right). \quad (8)$$

The solid side energy equation is given as:

$$\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2} = 0. \quad (9)$$

Equation (9) is a steady state boundary equation. When this boundary condition is achieved, the solver ends its iteration.

The values u , v , and w represent the x , y , and z directions of the velocity vector; P is the fluid pressure, T is the liquid temperature, g is the acceleration due to gravity, ρ is the fluid density, C_p is the specific heat capacity, β is the coefficient of thermal expansion; T_∞ , the ambient temperature, α is the thermal diffusivity, Q is the power output, and k is the thermal conductivity.

3. Results and Discussion

3.1. Mesh Dependency Study

Solving or simulating the model requires that a mesh is carried out to ensure the simulation results are adequate and closely related to what is practically obtainable. Hence, the mesh dependency study carried out by [20] and the mesh sensitivity study carried out by [21] were used as a guide in the present study. According to the work of Okereke and Ling [21], the higher the number of elements, the finer the mesh; this thereby improves the results of the simulation work. In addition, Jeong et al. [22], confirms that the higher the number of grid cells, the better the result obtained. The work also demonstrates the stability of the results as the difference tends to be less than 0.18%. The study carried out by [20] suggested that a mesh within 20% to 40% of the initial size of the model in some applications is adequate to achieve a good simulation result. In this regard, a mesh dependency study was carried out for the present model. Figure 2a presents the mesh dependency of the present model. It was observed that the results were unstable for mesh elements of less than 6000. Therefore, to obtain stable and good results, the mesh used in the present study was above 20,000. However, it is important to note that the number of nodes and elements are functions of the capacity of the simulation machine. In addition, the higher the number of nodes and elements, the longer it takes for the simulation to converge. Figure 2b presents the meshed model with 108,813 nodes and 27,313 elements.

3.2. Effect of Power on Heat Sink Temperature

The temperature contour plot at 4.55 W is presented in Figure 3. In Figure 3a, the isometric view of the cylindrical heat sink is shown, and it is observed that the outer cylindrical fins recorded a lower temperature than the fins closest to the LED chip. This is identified by the blue contour legend in Figure 3. In addition, the red contour legend signifies the part of the model with the highest temperature (this is usually the LED chip because it is the heat source). The isometric and back view of the heat sink shown in Figure 3a,b, respectively, indicate that the temperature contour distribution is concentric. This signifies that heat spreads from the LED chip to the heat sink's base. This phenomenon confirms that heat is conducted from a hotter source to a colder one within the same environment or medium.

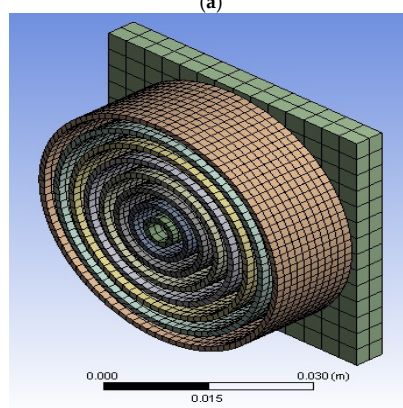
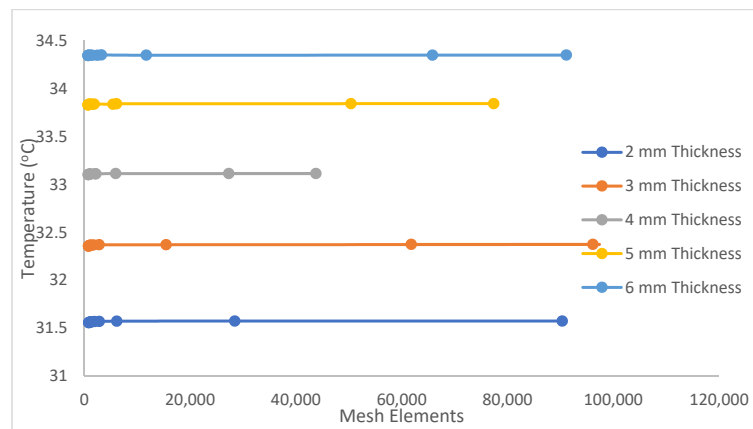


Figure 2. (a) Mesh dependency study of the present model. (b) Meshed with 108,813 nodes and 27,313 elements.

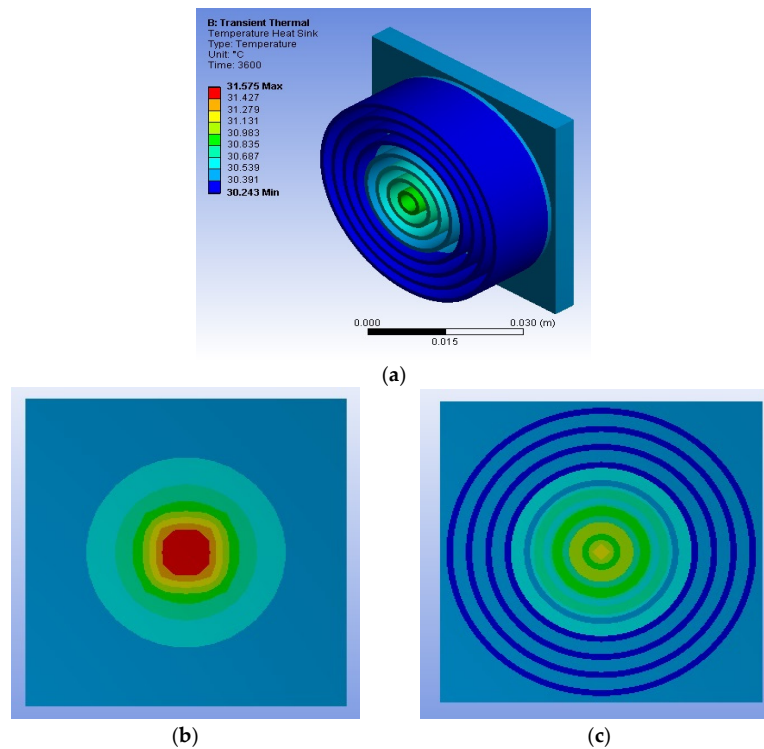


Figure 3. Temperature contour plot at 4.55 W: (a) Isometric view of the heat sink, (b) Back view of the heat sink, and (c) Front view of the heat sink.

In Figures 4–8, the maximum temperatures of the cylindrical heat sink with time at 4.55 W, 9.7 W, 15.03 W, 20.6 W, and 25.75 W for the different cylindrical heat sink fins, respectively, are presented. The graph pattern in Figures 4–8 corresponds to the graph pattern presented by Mjallal et al. [12] for temperature against time. This shows that the heat generated by the LED chip was dissipated to the environment through conduction and convection. It also, signifies that the heat generated by the system was effectively managed with acceptable limits to avoid the early failure of the LED system. It is observed from Figures 4–8 that the highest and lowest temperatures for the different power ratings were recorded at 6 mm and 2 mm cylindrical heat sink fins, respectively. This could be directly related to the volume of the respective heat sinks, which is a factor of thermal resistance. The bigger the heat sink volume, the longer the temperature travel path. However, this might lead to heat retention in the system but may not necessarily lead to overheating because the heat is gradually dissipated to the environment.

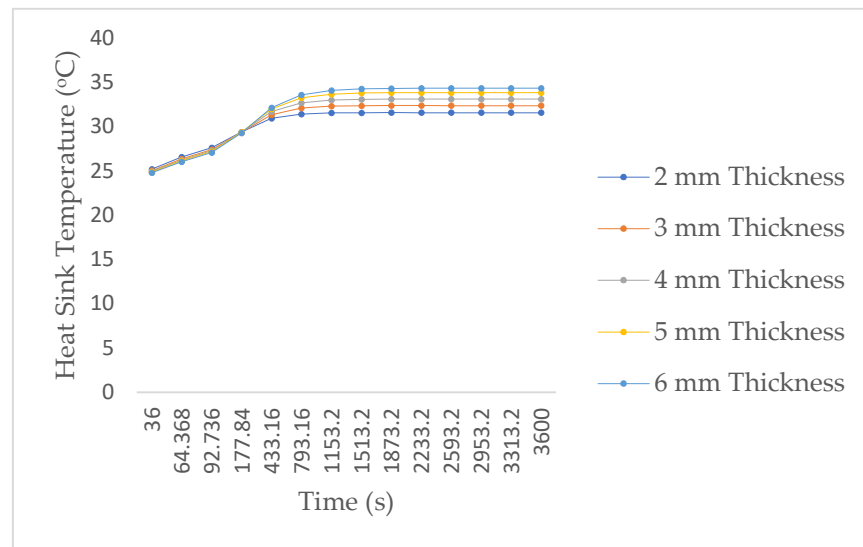


Figure 4. Temperature plot of heat sink at 4.55 W.

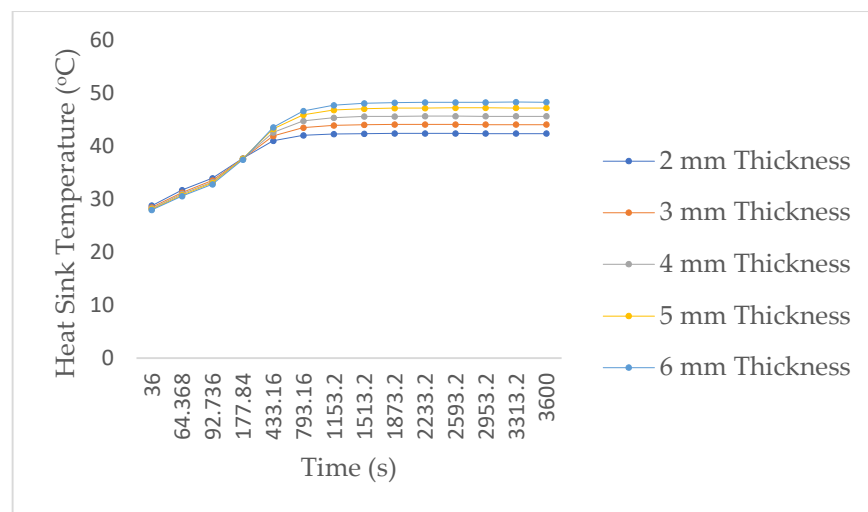


Figure 5. Temperature plot of heat sink at 9.7 W.

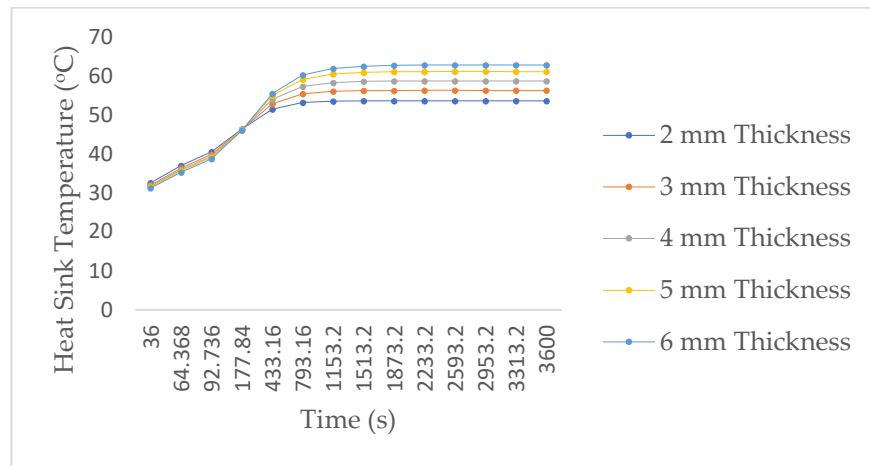


Figure 6. Temperature plot of heat sink at 15.03 W.

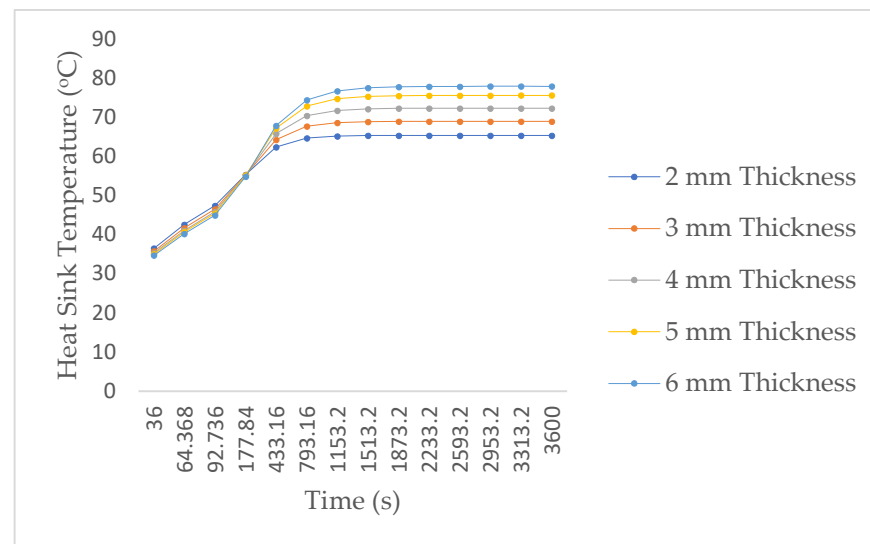


Figure 7. Temperature plot of heat sink at 20.6 W.

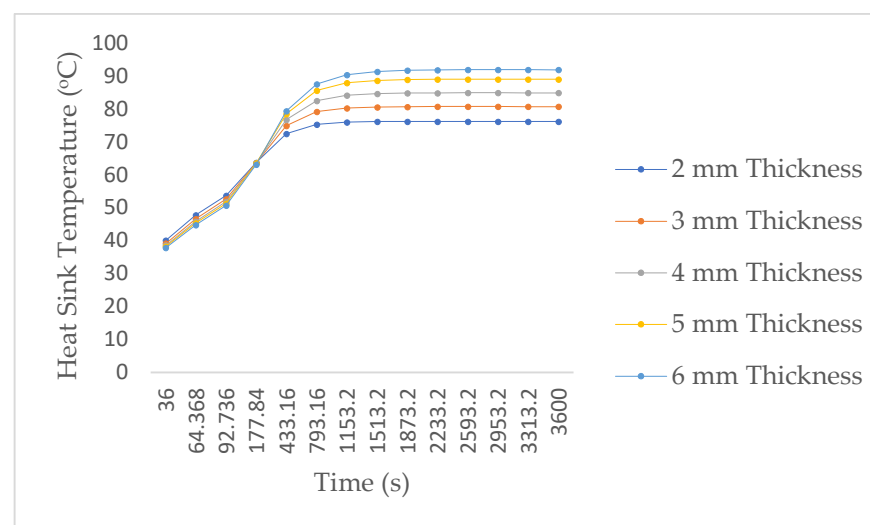


Figure 8. Temperature plot of heat sink at 25.75 W.

Furthermore, it demonstrated that 6 mm cylindrical heat sink fins could accommodate more heat without affecting the LED application. This is a major objective of this study, and it was achieved with a heat sink having a mass of less than 100 g. The goal of the study was to ensure that the heat sink recommended is less than 100 g. This is because most LED applications are miniaturised and the total weight for some applications is about 500 g including the heat sink device. Again, the maximum temperature from Figures 4–8 appears to be approximately stable or constant after 793.16 s for each cylindrical heat sink fin at various power ratings. This means that steady state temperature was reached, and the solution started to converge after 793.16 s. The constant temperatures after some time in different power ratings are observed in the experimental work carried out by Ranjith et al. [11]. In their empirical work, diagonal, cylindrical, and spiral heat sinks were considered for managing heat in LED modules.

3.3. Effect of Thermal Resistance on the Cylindrical Heat Sink

The thermal resistance of the cylindrical heat sink was calculated using Equation (10):

$$R = \frac{\Delta T}{Q} \quad (10)$$

where R is the thermal resistance in (K/W), $\Delta T = T_{max} - T_{ambient}$ and Q is the power in (W). Figure 9 presents the thermal resistances for the different fin thicknesses of the cylindrical heat sinks. As observed in Figure 9, the thermal resistance of the heat sinks slightly increased from 2.104 K/W to 2.715 K/W for a thickness of 2 mm to 6 mm, respectively. This accounts for a 29.04% increment in thermal resistance. This was expected because the higher the volume of a heat sink, the higher the thermal resistance. However, this might not translate to effective heat dissipation or heat removal. Furthermore, Figure 10 presents the thermal resistance of different cylindrical heat sink fin thicknesses at various power ratings. Figure 10 shows that the thermal resistance at 2 mm, 3 mm, 4 mm, 5 mm, and 6 mm are approximately 2.104 K/W, 2.28 K/W, 2.442 K/W, 2.603 K/W, and 2.715, respectively, for different power ranges. In addition, it was also observed that the power ratings of the LED chip did not impact negatively on the thermal resistance of the cylindrical heat sink. In other words, at 2 mm cylindrical heat sink thickness, the thermal resistance was approximately the same for 4.55 W, 9.7 W, 15.03 W, 20.6 W, and 25.75 W. Evidently, a similar trend was observed for the other thicknesses studied with our approach.

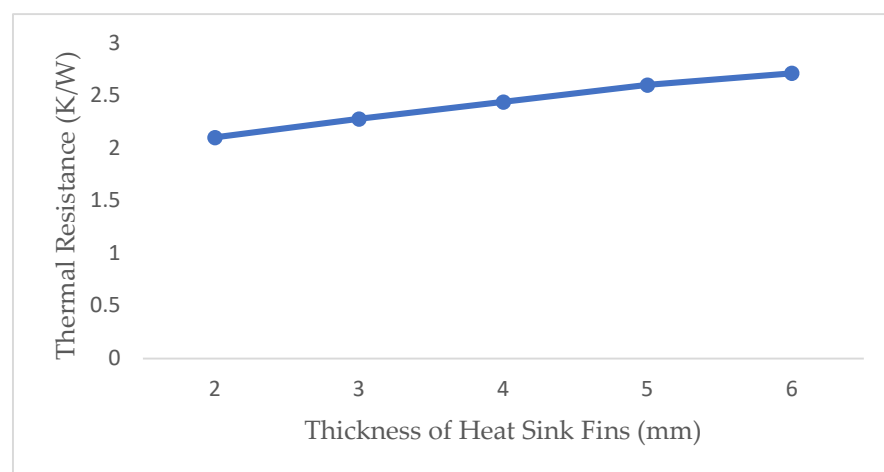


Figure 9. Thermal Resistance of Heat Sink.

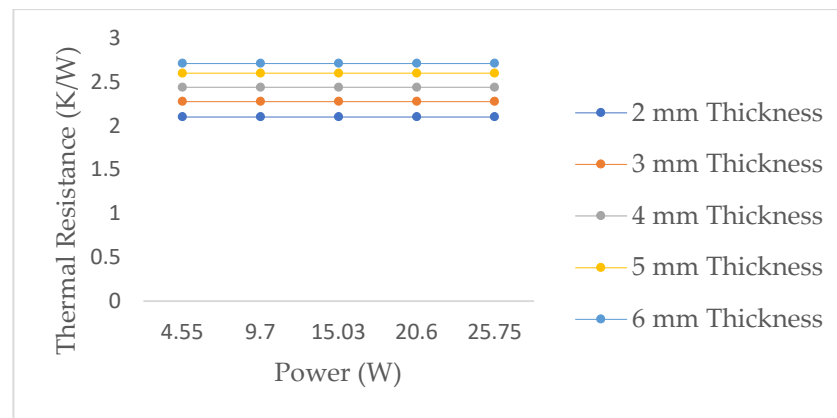


Figure 10. Thermal resistance relative to the power input.

3.4. Thermal Efficiency Analysis

The thermal efficiency calculations of the cylindrical heat sink are analysed and presented in Equations (11)–(13). The simulation thermal efficiency is given as:

$$\text{Thermal Efficiency } (\eta_T) = 1 - \frac{T_a}{T_{max}} \quad (11)$$

whilst the calculated thermal efficiency is given as [23]:

$$\text{Thermal Efficiency } (\eta_T) = \frac{\tanh(mL_c)}{mL_c} \quad (12)$$

$$\text{where } mL_c = \sqrt{\frac{2h_f L_f}{Kt_f}}. \quad (13)$$

The T_a represents the ambient temperature, T_{max} , the temperature maximum of the heat sink, h_f , the convection coefficient of the cylindrical heat sink fins; L_f denotes the height of the cylindrical heat sink fin and t_f , the thickness of the cylindrical heat sink fin. In Figure 11, the thermal efficiency at different thicknesses for different power inputs is shown to follow a similar pattern (increasing with power). It is observed that the thermal efficiency increased with the increased power input for the different cylindrical heat sink fin thicknesses. This is valid since the power inputs had no effect on the thermal resistance of the heat sink. This meant that as the power is increased, the heat transfer rate is increased, thereby increasing the thermal efficiency. The thermal efficiency is a factor of how fast heat is removed from the system to the environment. Therefore, a high heat transfer rate will improve the system, whilst a slow heat transfer rate could lead to heat retention and the possible failure of the system. As shown in Figure 12, the comparison between the calculated and simulated thermal efficiencies at a power rating of 25.75 W is presented. The calculated and simulated thermal efficiencies were observed to increase with increased cylindrical heat sink fin thickness (this is a function of the volume). According to Wakefield-Vette [24], the efficiency of fins will increase when the fin thickness increases; this is observed in Figures 11 and 12. At 6 mm, 5 mm, 4 mm, 3 mm, and 2 mm thickness, the calculated thermal efficiency was higher than the simulated thermal efficiency with 15.67%, 14.20%, 12.27%, 8.58%, and 1.2%, respectively. Therefore, the accuracy between the calculated and simulated thermal efficiency ranges from 84.33% to 98.80%. It could be contingent that an increase in the cylindrical heat sink thickness may cause the calculated thermal efficiency to further drift away from the simulated thermal efficiency.

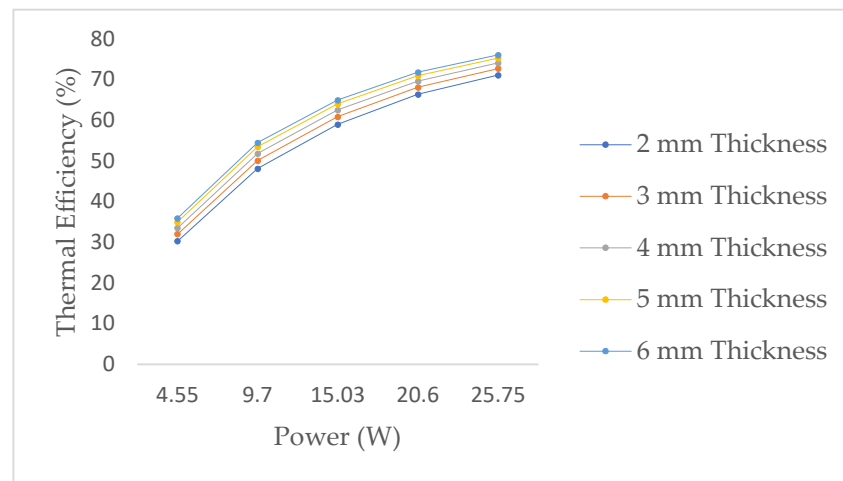


Figure 11. Thermal efficiency relative to the power input.

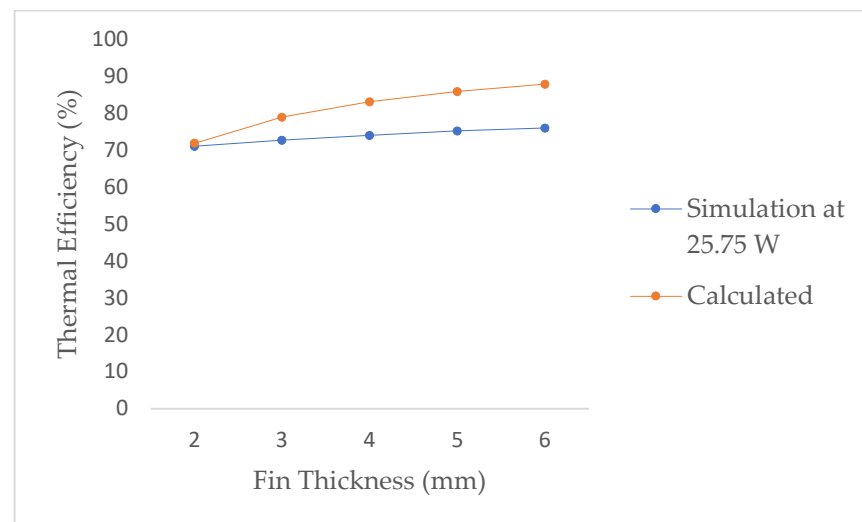


Figure 12. Comparison between simulation and calculated efficiency.

4. Conclusions

In this study, we have demonstrated the thermal impact of a cylindrical heat sink fin on the management of heat in LED applications with an improved technique using different cylindrical configurations, thicknesses, and power ratings to analyse the heat dissipation effects. The mesh dependency study suggested that adequate meshing was employed to achieve the desired temperature values. The findings suggest that a cylindrical heat sink fin with a 6 mm thickness and a mass of 81.13 g is more efficient than a cylindrical heat sink fin with lesser thickness, despite having a slightly higher thermal resistance. This could be because the higher cylindrical heat sink fin thickness accommodates more heat without causing failure to the LED application. Furthermore, the power ratings of the LED chips were found to have no effect on the thermal resistance of the heat sink investigated. The thermal efficiency of the heat sink was high for the increased volume of the cylindrical heat sink. Likewise, high thermal efficiency was evident in the 6 mm thick heat sink. Additionally, it was shown in this work that the LED performance in electronic circuits could be significantly improved with the choice of the cylindrical heat sink fin considered during the assembly process. Finally, future work will involve the investigation of other types of heat sink configurations and the different materials used in LED systems. This will help to give better information on heat management in microelectronic devices.

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Conflicts of Interest: The authors declare no conflict of interest.

Nomenclature

C_p	constant pressure specific heat [J/(kg.°C)]
g	gravitational acceleration [m/s ²]
h_f	the convection coefficient
k	thermal conductivity [W/(m.°C)]
L_f	the height of fin [m]
M	mass [kg]
n	number of fins
p	pressure [Pa]
Q	heat flow/power [W]
R	thermal resistance [°C/W]
t_f	the thickness of fin
T	temperature [°C]
T_∞	the ambient temperature
u, v, w	Cartesian velocity components [m/s]
x, y, z	Cartesian coordinates [m]
V	the volume [m ³]
Greek symbols	
α	thermal diffusivity [m ² /s]
β	coefficient of thermal expansion [1/K]
ρ	density [kg/m ³]

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