INTRODUCTION

The leading candidate progenitor model for short duration Gamma-Ray Bursts (sGRBs) is the merger of two compact objects, neutron star-neutron star (NS-NS) or neutron star-black hole \([1\). However the initial spike in a giant flare from a Soft Gamma Repeater (SGR) in a relatively nearby galaxy would also appear as a sGRB. For example, the December 27th 2004 event from SGR1806-20 would have been visible by BATSE (the Burst and Transient Source Experiment) out to \(\approx 50\) Mpc \([1,2]\). Thus it is plausible that some fraction of sGRBs are extragalactic SGR giant flares. Previously, Tanvir et al. \([3\) demonstrated that between 10 and 25 per cent of BATSE sGRBs were correlated on the sky with galaxies within \(\approx 113\) Mpc. The Luminosity Function (LF) of SGRBs has been investigated previously assuming a single population \([4\) in order to determine the intrinsic sGRB rate and most likely LF parameters. Here we assume intrinsic rates given by both the observed Galactic SGR flare rates and modelled NS-NS merger rates in order to investigate single and dual population LF parameters. Obviously there are significant uncertainties in these rates: the Galactic giant flare rate in particular is estimated from only 3 observed events. Regardless of these uncertainties and the exact form of LF for a second population, we find a single progenitor population constrained by overall number counts cannot produce sufficient local events. We present preliminary results that show only a dual population can reproduce the likely local sGRB distribution as well as the overall number counts.

METHODS

The number of sGRBs, \(N\), observed above threshold \(p\) in time \(T\) and solid angle \(\Omega\) is given by equation \([1\) where \(\Phi(L)\) is the sGRB LF, \(R_{\text{GRB}}(z)\) is the sGRB event rate at redshift \(z\), \(dV(z)/dz\) is the comoving volume element at \(z\) and \(\Delta \min\) for a burst of luminosity \(L\) is determined by the detector flux threshold and the luminosity distance of the event. We assume a spectral photon index of \(1.1\) in the BATSE energy range to convert photon flux to energy flux.

\[
N(> p) = \frac{\Omega T}{4 \pi} \int_{\min}^{\max} \Phi(L) dL \int_{0}^{\Delta \min} R_{\text{GRB}}(z) \frac{dV(z)}{1 + z} dz
\]

The sGRB rate, \(R_{\text{GRB}}(z)\) is given by equation \([2\) where \(\rho_{\text{GRB}}\) is the rate of sGRBs per progenitor, \(\rho_{p}(0)\) is the intrinsic progenitor formation rate and \(F(z)\) describes the progenitor production rate as a function of \(z\).

\[
R_{\text{GRB}} = \rho_{\text{GRB}} \times \rho_{p}(0) \times F(z)
\]

For NS-NS mergers, \(\rho_{\text{GRB}} = 1\) and \(F(z)\) is the delayed rate given by the convolution of the Star Formation Rate at \(z\) (SFR\((z)\)) with a distribution of delay times to repre-
sent merger formation. For SGR flares, \( \rho_{\text{GRB}} = 3 \times 10^{-2} \) (the observed local rate of giant flares per Galactic SGR) and \( F(z) \) follows both SFR\((z)\) for magnetar production from supernovae and the delayed SFR\((z)\) to allow for production by White Dwarf binary mergers [5]. We take SFR\((z)\) as given by the SF2 model of Porciani and Madau [6], with the local SFR from [7]. \( \rho_{\text{P}(0)} \) SGR rates per Milky Way equivalent galaxy are from Levan et al. [5], and we follow Kalogera et al. [8] for a NS-NS merger rate of \( 10^{-5} \) yr\(^{-1} \).

LFs for SGR giant flares and NS-NS mergers are not well constrained. A log-normal LF approximates the theoretical NS-NS merger distribution [9], and is also plausible for SGR giant flares. Here we assume sGRBs (of differing luminosities) to arise from both SGRs and NS-NS mergers. We also investigate a single merger population with Schechter function and log-normal LFs. Merger time distributions are similarly unknown, and we assume \( P(\log(\tau))d\log(\tau) = \) constant between \( 10^7 \) and \( 10^{10} \) years, approximating theoretical distributions [10].

The \( C_{\text{max}}/C_{\text{min}} \) table from the BATSE catalogue[11] provides peak count rate for bursts in units of threshold rate. The BATSE threshold was varied historically, and to analyse a consistent set of bursts we restricted the table to only those sGRBs recorded when the threshold was set to \( 5.5\sigma \) above background in at least 2 detectors in the 50 – 300 keV range. The all sky equivalent period this represents is \( \sim 1.3 \) years. By varying the parameters of the LFs (median and sigma for log-normal, slope and \( L_\ast \) for Schechter) and fitting the predicted \( N(>p) \) to the \( C_{\text{max}}/C_{\text{min}} \) distribution, we found the best fit LF parameters by \( \chi^2 \) minimization. Figure 1 shows an example of such a fit. Having obtained the best fit LF parameters, the redshift distribution of predicted sGRBs can be calculated, as shown in Figures 2-7.

### RESULTS AND CONCLUSIONS

Although a single NS-NS merger population luminosity function can produce reasonable fits to the overall number counts, only samples with two populations of differing luminosity distributions reproduce the likely local population of sGRBs (Figures 3 and 5) - even Schechter type single luminosity functions, which are dominated by low-luminosity events, fail to reproduce the nearby population (Figure 7). Furthermore, the overall redshift distribution of the dual population samples are consistent with the handful of redshifts known for sGRBs[12]. Despite large uncertainties in assumed intrinsic rates, the best fit LF parameters also agree well with the few peak luminosities currently known for both SGR giant flares and cosmological sGRBs.
FIGURE 4. Cumulative distribution of bursts out to $z = 3$ using best fit dual population log-normal LFs results from Figure 2. Also shown (solid line) is the cumulative distribution of the handful of sGRBs with known redshifts [15]. Other details as Figure 1.

FIGURE 5. Cumulative distribution of bursts within 500Mpc using best fit dual population with log-normal LF for the SGR flares ($\log(E_p) = 45.0, \sigma_{\log} = 0.75$), and a Schechter function ($L_* = 50.0, \text{slope} = -0.9$) for the NS-NS merger population. Reduced $\chi^2 = 2.36$, other details as Figure 1.

FIGURE 6. Cumulative distribution of bursts out to $z = 3$ using best fit dual population (lognormal SGR, Schechter mergers) as Figure 5. Other details as Figure 4.

FIGURE 7. Cumulative distribution of bursts within 500Mpc using best fit single Schechter function ($L_* = 50.25, \text{slope} = -0.9$, reduced $\chi^2 = 2.53$) for the NS-NS merger population. Other details as Figure 6.

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REFERENCES