

FR II radio galaxies at low frequencies – II. Spectral ageing and source dynamics

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ABSTRACT

In this paper, the second in a series investigating Fanaroff–Riley type II (FR II) radio galaxies at low frequencies, we use LOw Frequency ARray (LOFAR) and Very Large Array (VLA) observations between 117 and 456 MHz, in addition to archival data, to determine the dynamics and energetics of two radio galaxies, 3C 452 and 3C 223, by fitting spectral ageing models on small spatial scales. We provide improved measurements for the physical extent of the two sources, including a previously unknown low surface brightness extension to the northern lobe of 3C 223, and revised energetics based on these values. We find spectral ages of $77.05^{+9.22}_{-8.74}$ and $84.96^{+15.02}_{-13.83}$ Myr for 3C 452 and 3C 223, respectively, suggesting a characteristic advance speed for the lobes of around 1 per cent of the speed of light. For 3C 452, we show that, even for a magnetic field strength not assumed to be in equipartition, a disparity of a factor of approximately 2 exists between the spectral age and that determined from a dynamical standpoint. We confirm that the injection index of both sources (as derived from the lobe emission) remains steeper than classically assumed values, even when considered on well-resolved scales at low frequencies. However, we find an unexpected sharp discontinuity between the spectrum of the hotspots and the surrounding lobe emission. We suggest that this discrepancy is a result of the absorption of hotspot emission and/or non-homogeneous and additional acceleration mechanisms; as such, hotspots should not be used in the determination of the underlying initial electron energy distribution.

Key words: acceleration of particles – radiation mechanisms: non-thermal – galaxies: active – galaxies: jets – radio continuum: galaxies – X-rays: galaxies.

1 INTRODUCTION

Over the previous decades, radio-loud active galaxies, while only constituting a small fraction of the population as a whole, have become an increasingly important part of our understanding of how galaxies evolve to form the Universe we observe today. Models of galaxy evolution have historically been unable to unify simulations with observations, giving an excess of cold gas, a

deficit in hot gas and an overestimation of the star formation rate (e.g. Balogh et al. 2001). In order to correct these discrepancies, it is generally agreed that an additional energy input is required in order to expel cold gas from galaxies and to increase the cooling time-scales of hot gas, if one is to correctly determine the evolutionary path of galactic populations (e.g. Cowie & Binney 1977; Fabian & Nulsen 1977). Radio galaxies, highly energetic structures that are observed on scales of up to a few Mpc in size (e.g. Bridle et al. 1976; Leahy 1991; Mullin, Hardcastle & Riley 2006; Marscher & Jorstad 2011), are therefore one of the currently favoured mechanisms by which energy can be transferred to the surrounding

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environment in a self-regulating manner (Croton et al. 2006; Bower et al. 2006; Fabian 2012; McNamara & Nulsen 2012; Morganti et al. 2013; Heckman & Best 2014). An understanding of what drives these powerful radio sources, of the time-scales on which they operate and of the effect they have on their external environment is therefore crucial in our understanding of galaxy evolution as a whole.

Because of their steep radio spectra ($\alpha \geq 0.5$),¹ the energetics of the lobes of Fanaroff–Riley type II (FR II) radio galaxies are dominated by the low-energy electron population. Recent studies have suggested that this population may have a significantly higher total energy content (the combined particle and magnetic field energies) than has previously been assumed when considered using modern analytical methods (Harwood et al. 2013, 2016; Harwood, Hardcastle & Croston 2015, hereafter, H13, H16 and H15, respectively). This potentially affects our understanding of not only the energetics of FR IIs but also their age and dynamics. However, such studies have still been able to directly probe the low-frequency spectrum on well-resolved scales. The limited sensitivity, image fidelity and frequency coverage of the previous generation of radio interferometers has historically restricted earlier studies of FR IIs to ~ 1 -arcsec resolution observations at GHz frequencies and low-resolution observations at metre wavelengths, leaving well-resolved studies of FR IIs at low frequencies a relatively unexplored region of parameter space. New instruments, such as the LOw Frequency ARray (LOFAR; van Haarlem et al. 2013) and the recently upgraded Karl G. Jansky Very Large Array (VLA), are now able to resolve this issue by providing the high-quality, high-resolution observations at MHz frequencies required to undertake studies that are critical to our understanding of this population.

Spectral ageing in FR II radio galaxies

One of the key values required for deriving the properties of radio galaxies, such as their total power output and the speed at which their hotspots are advancing through the external medium, is the duration for which the source has been in its active phase. As the lobes of FR II radio galaxies radiate via the synchrotron process, in theory, for an electron population with a power-law energy distribution that is initially described by

$$N(E) = N_0 E^{-\delta}, \quad (1)$$

and knowing that in a fixed magnetic field a single electron will have energy losses, τ , that scale as a function of frequency such that

$$\tau = \frac{E}{dE/dt} \propto \frac{1}{E} \propto \frac{1}{\nu^2} \quad (2)$$

at later times (assuming that no further particle acceleration is present), the observed population can be described by

$$N(E, \theta, t) = N_0 E^{-\delta} (1 - E_T E)^{-\delta-2}, \quad (3)$$

where E_T are model-dependent losses that are a function of the pitch angle of the electrons to the magnetic field, θ , and the time since they were accelerated, t . Through modelling of the resulting curvature, known as spectral ageing, one is able to determine the time since the acceleration of a given region of plasma, and hence the age of the source as a whole.

These single-injection spectral ageing models and their application have recently been discussed in detail by H13 and H15 and are one of the most commonly used observationally driven methods for determining the age of radio galaxies (e.g. Jamroz et al. 2005; Kharb et al. 2008; de Gasperin et al. 2012). However, it has recently been shown that many of the assumptions that go into these models are not as robust as had been previously thought. The general reliability of these models in determining the intrinsic age of a source has long been a matter of debate (e.g. Alexander & Leahy 1987; Eilek & Arendt 1996; Eilek, Melrose & Walker 1997; Blundell & Rawlings 2000), although it has been shown that through a combination of revised parameters (H13; H15; H16; Turner, Shabala & Krause, submitted) and more complex ageing models (e.g. the Tribble model; Tribble 1993; Hardcastle 2013; H13), many of these issues can be resolved, new questions have come to light and assumptions must still be made about the low-frequency spectrum on small spatial scales.

One of the key questions raised by recent studies is the correct value of the power-law index for the low-energy electron distribution described by equation (1) used within models of spectral ageing. At the point of acceleration, δ is assumed to be directly related to the observable spectrum of the plasma with an index (known as the injection index) given by²

$$\alpha_{\text{inj}} = \frac{\delta - 1}{2}. \quad (4)$$

This parameter has a significant affect not only on the determination of the energetics of a source (e.g. Croston et al. 2004, 2005; H16) but also on its derived age, hence the dynamics. Based on theoretical arguments (e.g. Blandford & Ostriker 1978) and observations of hotspots (Meisenheimer et al. 1989; Carilli et al. 1991), values of around $\alpha_{\text{inj}} = 0.5$ – 0.6 have traditionally been adopted. However, through derivation of the injection index at GHz frequencies (H13; H15), it has been suggested that it may be significantly steeper than previously thought, taking values of around 0.7 – 0.8 . Such steep spectral indices have previously been seen in observations of the integrated flux of FR IIs (e.g. the 3CRR sample; Laing et al. 1983) but were generally attributed to curvature downstream because of ageing in the oldest regions of plasma. However, as shown by H16, their spectrum can remain steep down to very low frequencies (≈ 10 MHz) where such ageing effects should be negligible. Determining the well-resolved, low-frequency spectrum of these sources is therefore key if we are to reliably determine the injection index and to understand the particle acceleration processes occurring in FR IIs, a vital step in advancing our understanding of radio galaxy physics and galaxy evolution as a whole.

In this paper, the second in a series examining FR II radio galaxies at low frequencies, we use LOFAR and VLA observations to explore the spectrum, dynamics and particle acceleration processes of two powerful radio sources on well-resolved scales. We address four primary questions.

- (i) What is the spectrum of FR II radio galaxies on small spatial scales at low frequencies?
- (ii) What are the model parameters and spectral age of our sample when tightly constrained at low frequencies?

² At near minimum energy for first-order Fermi acceleration, the spectrum is not a power law in momentum, which further complicates this relation (e.g. Brunetti et al. 2002; Amato & Arons 2006). Here, we use the classical assumption but note this effect likely needs to be addressed in future models.

¹ We define the spectral index such that $S \propto \nu^{-\alpha}$.

Table 1. List of target sources and galaxy properties. ‘Name’ and ‘IAU name’ are the 3C and IAU names of the galaxies. ‘Spectral index’ lists the low-frequency spectral index between 178 and 750 MHz. ‘LAS’ is the largest angular size of the source and ‘Size’ is its largest physical size. The values in the ‘Redshift’, ‘178-MHz flux’, ‘5-GHz core flux’, ‘Spectral index’, ‘LAS’ and ‘Size’ columns are taken directly from the 3CRR data base (<http://3crr.extragalactic.info/cgi/database>; Laing, Riley & Longair 1983). ‘Revised’ values of the source sizes are listed in the last two columns and are measured from the 368-MHz P-band VLA images presented in this paper.

Name	IAU name	Redshift	178-MHz flux (Jy)	5-GHz core flux (mJy)	Spectral index (178–750 MHz)	LAS (arcsec)	Size (kpc)	Revised LAS (arcsec)	Revised size (kpc)
3C 223	J0936+361	0.137	9.0	16.0	0.74	306	740	329	796
3C 452	J2243+394	0.081	130	59.3	0.78	280	428	287	438

(iii) How do these observational findings compare to dynamical models of FR IIs?

(iv) What effect does this have on our understanding of the age, dynamics and energetics of FR IIs?

In Section 2, we give details of target selection, data reduction and the analysis undertaken. In Section 3, we present our results, and in Section 4, we discuss these findings in the context of the aims outlined above. Throughout this paper, we use a concordance model in which $H_0 = 71 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_m = 0.27$ and $\Omega_\Lambda = 0.73$ (Spergel et al. 2003).

2 DATA REDUCTION AND SPECTRAL ANALYSIS

2.1 Target selection and data reduction

To investigate the dynamics of powerful radio galaxies at low frequencies, we use the sample presented by H16 in the first paper of this series of two nearby FR IIs: 3C 223 and 3C 452 (Table 1). These sources were observed as part of the LOFAR surveys key science project (KSP) and comprise 10 h of observations of each source at Low-Band Antenna (LBA; 10–90 MHz) and High-Band Antenna (HBA; 110–250 MHz) frequencies using the Dutch stations, giving a maximum baseline of $\sim 100 \text{ km}$. Because, within this paper, we are interested in the spectrum and dynamics on well-resolved scales, we limit ourselves to the higher-frequency HBA observations, which provide a spatial resolution of $\sim 7 \text{ arcsec}$. We use the same data as H16, so we do not repeat details of the reduction process here, but note that because of ionospheric effects and heavy flagging on the longest baselines in certain bands, the 3C 223 data were reimaged at 13-arcsec resolution in order to obtain good image fidelity on small scales whilst maintaining the maximum possible frequency coverage.

To tightly constrain any curvature present in the spectrum of the sources at low frequencies, VLA P-band (224–480 MHz) observations were undertaken. To recover the most diffuse emission and to obtain a resolution comparable to that of LOFAR, observations were made in A and B array configurations for 3C 223 with an additional pointing in the C configuration for 3C 452, using the full 256-MHz bandwidth centred at a frequency of 352 MHz. The data were reduced using CASA in the standard manner and following the guidelines set out in the online tutorial for continuum P-band data.³ We note that as the P-band receivers were recently upgraded, the data were inspected for swapped polarizations, although none was found.

In order to apply the small-scale spectral analysis described in Section 2.2, multiple images were required across the observed

frequency range. The full bandwidth was therefore split on a spectral window (SPW) basis (16 MHz per SPW) giving a total of 16 images. To reduce computational overheads during imaging, each SPW was averaged down in frequency to 16 channels of 1-MHz bandwidth. No averaging-in time was undertaken.

To allow a combination of the different array configurations, phase-only self-calibration was undertaken on the A-configuration data before being CLEANED to convergence. These images were then used as a model in order to cross-calibrate the B-configuration data and, for 3C 452, the combined A- and B-configuration images were used to calibrate the C-configuration data. The multiscale clean algorithm (MSCLEAN; Cornwell 2008; Rau & Cornwell 2011) was used to produce all images at scales of 0, 5, 15 and 45 times the cell size, where the cell size was set to one-fifth of the beam size. To perform the required spectral analysis, the P-band imaging parameters must be matched to those of the LOFAR maps. Therefore, we use the same image size and resolve the beam of each map to the lowest LOFAR frequency as defined by H16. In addition, radio maps were also made using the full bandwidth at a central frequency of 368 MHz. As this required imaging over a large fractional bandwidth, we used the CASA multifrequency synthesis CLEAN parameter $n_{\text{terms}} = 2$ (Rau & Cornwell 2011), which determines the spectral index of the source over the observed bandwidth in order to scale the observed flux to the central frequency and to produce a more realistic image of the target. The resulting images are shown in Fig. 1.

To constrain curvature at higher frequencies, we also obtained archival VLA images from the atlas of DRAGNs⁴ (Leahy & Perley 1991). As these images were already of a high quality, it was only necessary to regrid to J2000 coordinates and match to the LOFAR and VLA P-band imaging parameters. For 3C 452, the 610-MHz Giant Metrewave Radio Telescope (GMRT) image produced by H16 was also included in our analysis. While other archival data were also available, they are unable to match the images described above in terms of either resolution, uv coverage or sensitivity. A summary of all of the data used (both new and archival) is given in Table 2.

While all of the images are matched in terms of sky coordinates, small frequency-dependent shifts during calibration and imaging mean that an accurate alignment in image space is crucial to performing the small-scale spectral analysis used in this paper. Therefore, we align the images using the Gaussian fitting method detailed by H13 and H15, which has previously proved successful for this form of analysis. As the radio core is not visible at all frequencies, Gaussians were instead fitted to point sources close to the target using CASAVIEWER. A suitable reference pixel was then chosen and

³ <https://safe.nrao.edu/wiki/bin/view/Main/HuibIntemaPbandCasaGuide>

⁴ See the web site <http://www.jb.man.ac.uk/atlas/> edited by Leahy, Bridle & Strom.

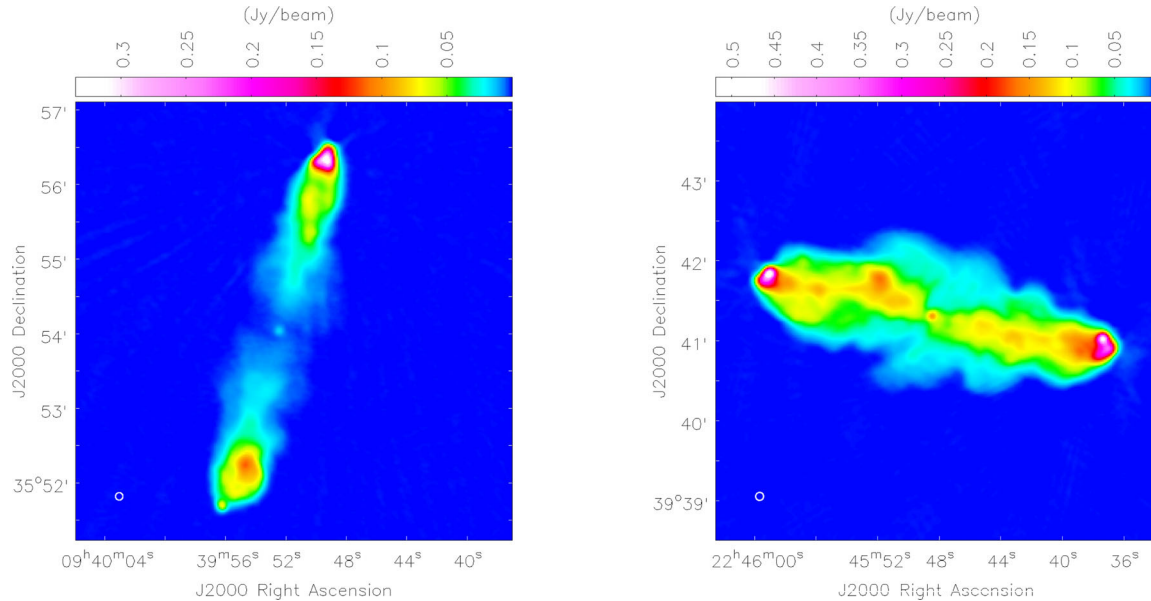


Figure 1. Full-bandwidth radio maps of 3C 223 (left) and 3C 452 (right) at 368 MHz, imaged in CASA using multiscale CLEAN and $n_{\text{terms}} = 2$. The off-source rms noise is $0.16 \text{ mJy beam}^{-1}$ for 3C 223 and $0.17 \text{ mJy beam}^{-1}$ for 3C 452. The restoring beam of 6 arcsec is indicated in the bottom-left corner of the images.

each image was aligned using the AIPS⁵ OGEOM task. To check the accuracy of the alignment, Gaussians were again fitted to the resulting images where we found a difference between the maps of only around 0.01 pixels. We can therefore be confident that the effects of misalignment are likely to be negligible in our analysis.

2.2 Spectral analysis

In order to achieve the aims of this paper, we have used the Broad Radio Astronomy Tools⁶ software package (BRATS), which provides a suite of tools designed for the fitting of spectral ageing models and spectral indices on a range of spatial scales, as well as various statistical and mapping tools. Details of the methods underlying the software have been discussed extensively by H13 and H15 and, as our analysis follows the standard procedures laid out in the BRATS cookbook,⁷ we do not repeat such a discussion here. Instead, we highlight the specific functions and parameters used for the analysis of our data.

In order to ensure that only the target source was included in our analysis, and to reduce computational overheads, a region that loosely encompasses the source was initially defined for both 3C 452 and 3C 223 using ds9.⁸ The core of each target, which is not expected to be described by models of spectral ageing, was excluded in both cases so that our analysis is not biased by this region. To determine the off-source thermal noise, a background region was also defined for each field in a blank area of sky well away from the target. The data were then loaded into BRATS and an initial source detection performed based on a 5σ cut-off for each image. To account for the increased rms noise associated with uncertainty in the modelling of extended emission during imaging, we adopt an on-source noise multiplier of 3 as described by H13 and H15 for determining statistical values and for the final region selection process. For the uncertainty introduced due to flux calibration errors,

we have assumed at LOFAR frequencies the value of 10 per cent presented by H16, for GMRT observations a 5 per cent uncertainty (Scaife & Heald 2012) and for VLA observations the standard values of 5 and 2 per cent at the P and L bands, respectively (Scaife & Heald 2012; Perley & Butler 2013). To reduce the effects of the superposition of spectra (H13; H15), the BRATS *setregions* command was set to define regions on a pixel-by-pixel basis, resulting in a total of 9272 regions for 3C 452 and 2620 regions for 3C 223.

To determine the age of the observed emission, three models of spectral ageing were fitted to the spectrum of both 3C 452 and 3C 223. The first two are the standard models proposed by Kardashev (1962) and Pacholczyk (1970) (KP model) and by Jaffe & Perola (1973) (JP model), which assume a single initial injection of particles described by a power law (equations 1 and 4). These models are then subject to radiative losses via the synchrotron process and inverse-Compton scattering on the cosmic microwave background (CMB). They differ only in that the KP model assumes a fixed pitch angle of the electrons with respect to the magnetic field, whereas the JP model assumes a variation in this angle, averaged over its radiative lifetime. As a consequence, the KP model displays much less curvature for an equivalent age than the exponential cut-off seen in the JP model. This is because there is always a supply of high-energy electrons maintaining a small pitch angle to the magnetic field, and hence lower losses at higher frequencies.

While both the JP and KP models assume that the electrons are subject to a uniform magnetic field over their lifetimes, the third model tested attempts to account for a potentially more realistic scenario in which the field is spatially non-uniform. First proposed by Tribble (1993), the requirement for ageing models to be fast fitting (of the order of a few seconds) so that the parameter space can be fully explored and the need to be well constrained in frequency space to make a reasonable comparison to the standard models have historically limited its application to observations. However, it has recently been shown that in the free-streaming (i.e. weak field, high diffusion) case, the observed spectrum is simply the JP model integrated over the Maxwell–Boltzmann distribution. Thus, it can be comfortably handled by current computational capabilities (Hardcastle 2013; H13). Using the new generation of broad

⁵ <http://www.aips.nrao.edu/index.shtml>

⁶ <http://www.askanastronomer.co.uk/brats>

⁷ <http://www.askanastronomer.co.uk/brats/downloads/bratscookbook.pdf>

⁸ <http://ds9.si.edu>

Table 2. Summary of images by frequency. ‘Frequency’ refers to the frequency of the map. ‘Off-source rms’ refers to rms noise measured over a large region well away from the source. ‘Integrated flux’ values are listed at each frequency for the two lobes and for the whole source, where ‘Lobe 1’ refers to the northern and eastern lobes of 3C 223 and 3C 452, respectively, and ‘Lobe 2’ refers to the southern and western lobes of 3C 223 and 3C 452, respectively. The associated uncertainties are the combined rms and flux calibration errors. ‘Reference’ lists the origin of the images used to measure each value as follows: (1) H16; (2) this paper; (3) Leahy & Perley (1991); (3) atlas of DRAGNs (see the web site <http://www.jb.man.ac.uk/atlas/>, edited by Leahy, Bridle & Strom).

Source	Frequency (MHz)	Off-source rms (mJy beam ⁻¹)	Lobe 1		Integrated flux (Jy)		Total		Reference
				±	Lobe 2	±		±	
3C 223	118.4	1.08	13.69	1.37	11.00	1.10	24.69	2.47	1
	125.4	0.947	12.89	1.29	10.28	1.03	23.17	2.32	1
	132.5	0.910	12.03	1.20	9.76	0.98	21.79	2.18	1
	146.5	0.784	10.88	1.09	8.85	0.89	19.65	1.97	1
	153.6	0.840	10.38	1.04	8.40	0.84	18.78	1.88	1
	160.6	0.834	9.63	0.96	7.84	0.78	17.47	1.75	1
	280.0	0.462	6.34	0.32	4.89	0.24	11.23	0.56	2
	296.0	0.311	6.33	0.32	4.88	0.24	11.21	0.56	2
	312.0	0.274	5.97	0.30	4.67	0.23	10.64	0.53	2
	328.0	0.264	5.70	0.29	4.44	0.22	10.14	0.51	2
	344.0	0.277	5.54	0.28	4.36	0.22	9.89	0.49	2
	360.0	0.741	5.45	0.27	4.21	0.21	9.66	0.48	2
	392.0	0.344	5.15	0.26	4.04	0.20	9.19	0.46	2
	408.0	0.720	5.07	0.25	3.96	0.20	9.03	0.45	2
	424.0	0.348	4.83	0.24	3.80	0.19	8.63	0.43	2
	1477	0.102	1.96	0.04	1.52	0.03	3.49	0.07	3
3C 452	116.9	1.46	44.27	4.43	41.65	4.17	85.92	8.59	1
	121.8	1.41	43.39	4.34	40.96	4.10	84.85	8.49	1
	124.7	1.37	42.56	4.26	40.67	4.07	83.23	8.32	1
	128.6	1.28	41.87	4.19	39.90	3.99	81.77	8.18	1
	132.5	1.21	41.28	4.13	39.55	3.96	80.83	8.08	1
	136.4	1.23	40.06	4.01	38.88	3.89	78.94	7.89	1
	140.3	1.05	39.71	3.97	38.49	3.85	78.20	7.82	1
	152.0	1.08	38.07	3.81	37.10	3.71	75.17	7.52	1
	155.9	1.00	37.64	3.76	36.66	3.67	74.30	7.43	1
	159.9	0.947	37.15	3.72	36.30	3.63	73.45	7.35	1
	280.0	0.696	21.37	1.07	20.18	1.01	41.55	2.08	2
	296.0	0.458	20.79	1.04	19.69	0.98	40.48	2.02	2
	312.0	0.394	19.90	1.00	18.86	0.94	38.76	1.94	2
	328.0	0.412	19.04	0.95	18.02	0.90	37.06	1.85	2
	344.0	0.392	18.28	0.91	17.29	0.86	35.57	1.78	2
	360.0	0.682	17.48	0.87	16.45	0.82	33.93	1.70	2
	392.0	0.438	16.45	0.82	15.52	0.78	31.97	1.60	2
	408.0	0.763	16.12	0.81	15.24	0.76	31.36	1.57	2
	424.0	0.478	15.48	0.77	14.59	0.73	30.07	1.50	2
	456.0	0.857	14.53	0.73	13.66	0.68	28.19	1.41	2
	606.3	0.825	11.55	1.16	11.14	1.11	22.69	2.27	2
	1413	0.209	5.32	0.11	5.21	0.10	10.54	0.21	4

bandwidth interferometers, this model has proved successful in combining the physical plausibility of the time-averaged pitch angle provided by the JP model with the often better goodness-of-fit provided by the KP model (e.g. H15). However, it has yet to be investigated at low frequencies.

In the fitting of these models, we have used the magnetic field strengths determined by H16 from synchrotron/inverse-Compton fitting of 0.45 nT and 0.34 nT for 3C 452 and 3C 223, respectively. We assume standard values of $\gamma_{\min} = 10$ and $\gamma_{\max} = 1 \times 10^6$ for the minimum and maximum Lorentz factors, respectively (Carilli et al. 1991; Hardcastle, Birkinshaw & Worrall 1998; Godfrey et al. 2009; H16). In order to determine the injection index, we use the `BRATS mininject` command. By setting the injection index as a free parameter, this function uses χ^2 minimization to determine which injection index best describes the source and it allows any curvature found within the spectrum due to ageing to be accounted

for (see H13 for a detailed description). We performed a grid search between $\alpha_{\text{inj}} = 0.5$ and a reasonable upper limit of $\alpha_{\text{inj}} = 1.0$ using an initial step size of 0.05. A second fitting was then performed for each source around the minimum value using a decreased step size of 0.01. Fitting of the three models described above was then performed and the relevant images, data and statistical values were exported for analysis. Note that the analysis considers only the current episode of activity. The potential impact of multiple episodes on the intrinsic age of radio galaxies is discussed further in Section 4.4.

3 RESULTS

3.1 Data quality

Of the 16 spectral windows that make up the new VLA P-band observations, 10 SPWs for 3C 452 and 9 SPWs for 3C 223 were

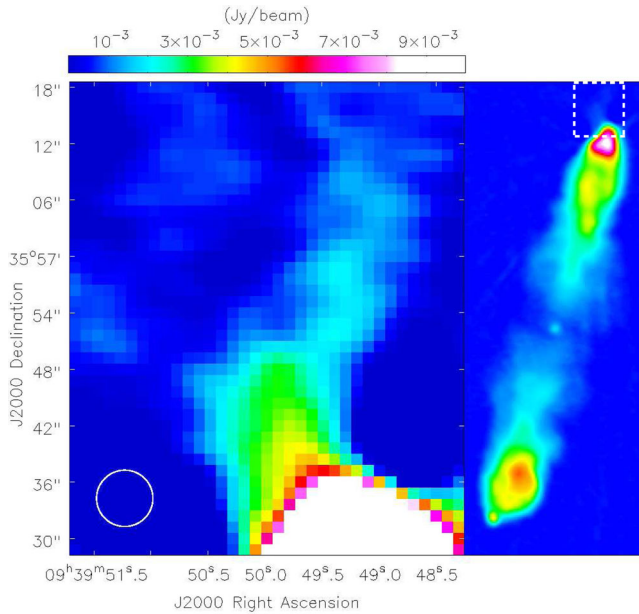


Figure 2. The northern extension observed in 3C 223 at 368 MHz. The dashed region of the full source (right) indicated the zoomed region (left) of the combined bandwidth image. The colour scale of the zoomed region set to highlight the diffuse, low surface brightness emission. The restoring beam of 6 arcsec is indicated in the bottom-left corner of the image.

found to have high-quality data in all array configurations. The spectral windows between 224 and 272 MHz (SPWs 0–2), 376 MHz (SPW 9) and 472 MHz (SPW 15) are purposely positioned at frequency ranges heavily affected by known radio frequency interference (RFI) sources. Thus, they were of extremely poor quality for both targets in all array configurations and were excluded from our analysis. At 440 MHz (SPW 13, both sources) and 456 MHz (SPW 14, 3C 223 only), heavy flagging was required in at least one array configuration, and so these data were also excluded from consideration.

3.2 Morphology and size

From the resulting combined P-band images (Fig. 1) we see that, as expected, the large-scale morphology matches that of previous studies (e.g. Nandi et al. 2010; Orrú et al. 2010) and of H16 at LOFAR frequencies. Measuring the largest angular extent of the sources from the 3σ contour at the tips of each lobe (Table 1), we find an increase in size compared to those of the 3CRR catalogue (Laing et al. 1983). 3C 452 increases only marginally from 428 to 438 kpc with a greater difference observed in 3C 223, which increases from 740 to 796 kpc, placing it comfortably within the giant radio galaxy classification range.

While the large-scale structure is generally in good agreement with previous findings, one notable exception is a faint, approximately 30 arcsec (72 kpc) northern extension to 3C 223 (Fig. 2). The faint nature of this emission means that it is not visible in archival images at GHz frequencies but hints of this structure were originally evident in the LOFAR image of H16. As it has a surface brightness around the noise level of the LOFAR image and is not observed at higher frequencies, it could not be confidently confirmed. However, this emission is clearly visible in the VLA P-band images at a location coincident with the tenuous detection in the LOFAR maps, so it is unlikely to be an imaging artefact. Taking the 3σ noise local to the northern lobe from the full bandwidth

LOFAR HBA image at 368 MHz of H16 and correcting for the differing beam sizes, we can place upper limits on the spectral index of $\alpha < 1.5$ for emission closest to the tip of the lobe, and $\alpha < 2.0$ at its furthest extent. While not particularly constraining, these upper limits suggest that the emission is not unphysically steep. No optical counterpart is found in the Sloan Digital Sky Survey (SDSS) catalogue (Alam et al. 2015) and so, given the morphology, it is reasonable to assume that it is associated with 3C 223. The underlying cause of this extended structure is unclear but it might be the result of a low-density region of the surrounding medium, which has subsequently filled with plasma from the radio galaxy lobes. We note that as this structure is not visible at higher frequencies and is tenuous in the LOFAR image, it has not been included in the determination of the source size or in our ageing analysis.

3.3 Model fitting and parameters

The results of the injection index determination are shown in Fig. 3. Both sources have a similar minimum of $\alpha_{\text{inj}} = 0.70 \pm 0.01$ and 0.68 ± 0.01 for 3C 452 and 3C 223, respectively, with all models converging to their respective values.

While the recent study by H15 at GHz frequencies, using the same methods applied here, notes that such a determination is model-dependent, so that some difference is expected, this convergence at LOFAR and P-band frequencies is not surprising. We see from equation (2) that as energy losses scale as $\tau \propto 1/\nu^2$, low-frequency observations are less affected by curvature due to spectral ageing for all but the oldest regions of plasma. Hence, all models should converge to a power law described by the injection index. It is therefore consistent with what one would expect for such low-frequency observations. However, the observed difference between the injection index determined from the integrated spectrum by H16 (0.85 and 0.71 for 3C 452 and 3C 223, respectively) and that derived here is much more unexpected.

Comparing these values to those presented by H16, we see that the value determined from the integrated spectrum of 3C 223 is only slightly steeper than the injection index presented here ($\Delta\alpha = 0.03$) and, given that the source is relatively old (Section 3.3), it is easily accounted for by curvature due to spectral ageing in the oldest regions of plasma. However, the large disparity between the value determined from the integrated spectrum of 3C 452 and the injection index presented within this paper ($\Delta\alpha = 0.15$) cannot be explained simply via radiative losses in homogeneous models. A steeper injection index ($\alpha_{\text{inj}} = 0.78$) was also derived by Nandi et al. (2010) who use a similar method of setting α_{inj} as a free parameter but over spatially larger regions. This results in a superposition of spectra, which is known to have a significant impact on the observed spectral index (e.g. Stroe et al. 2014; Kapinska et al. 2015). As the method for determining the injection index used here should reduce such effects, it is this value that we apply in the subsequent model fitting. We discuss in detail these results and the possible physical causes in Section 4.1.

Figs 4 and 5 show the spectral ageing maps for 3C 223 and 3C 452, respectively, along with their corresponding χ^2 and errors as a function of position. The general distribution of spectral ages for all three models is consistent with what one would expect for powerful FR IIs, with low age regions of plasma coincident with the hotspots and the oldest regions of plasma residing close to the AGN core. Plots of frequency against flux of representative regions for various ages are shown in Fig. 6.

From Table 3, which shows the statistical values for the model fitting, we see that all three models are able to provide a good description of the observed spectrum with none of the models

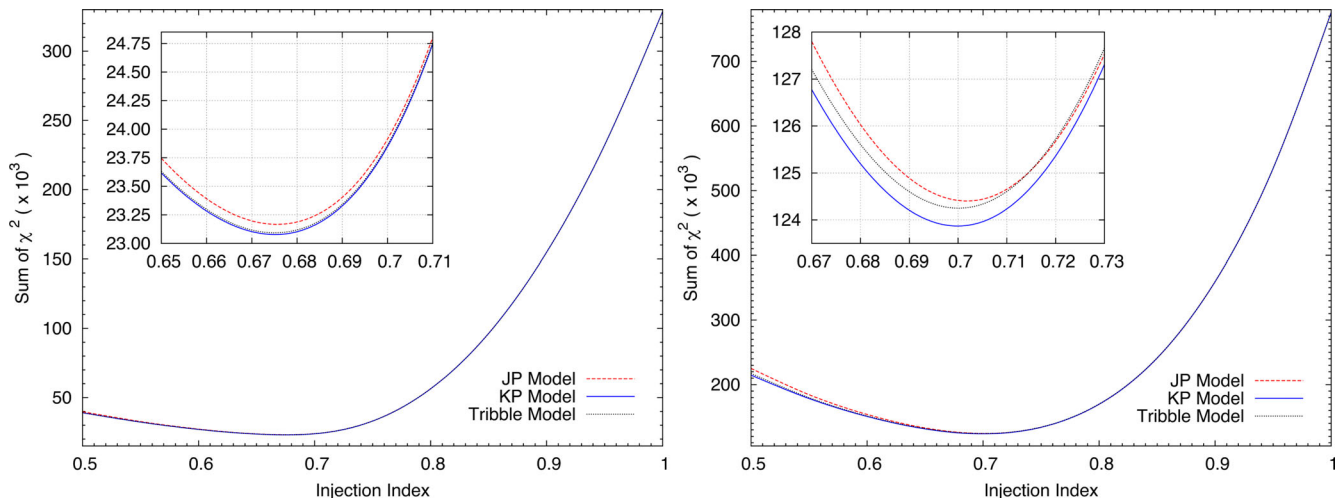


Figure 3. The χ^2 values for 3C 223 (left) and 3C 452 (right) for the JP (red dashed curve), KP (blue solid curve) and Tribble (black dotted curve) models of spectral ageing as a function of injection index. Plots zoomed to the minimum values are shown inset for each panel. The minimum occurs at 0.68 for 3C 223 and at 0.70 for 3C 452 to two significant figures for all models. Note that for 3C 223 the Tribble model closely follows the KP model. Fitting was performed with an initial step of 0.05 between 0.5 and 1.0 and a secondary step size of 0.01 around the minimum values. The data are fitted with natural cubic splines. As all points lie on the fitted spline, they are excluded for clarity.

being rejected at even the 1σ level. From Table 4, we see that the spectral ages of the sources range from $77.05^{+9.22}_{-8.74}$ (Tribble model) to $89.05^{+8.56}_{-7.14}$ (JP model) Myr for 3C 452 and between $73.96^{+17.29}_{-13.92}$ (KP model) and $84.95^{+15.02}_{-13.83}$ (Tribble model) Myr for 3C 223. The large error bars associated with the ages are unsurprising because of the limited number of data points at GHz frequencies, where curvature due to ageing is most easily constrained, a point discussed further in Section 4.2.

While the statistics of Table 3 suggest that the models of spectral ageing tested provide a good description of the source as a whole, localized regions of high χ^2 values that are spatially coincident for all three models are also observed. From the χ^2 maps of Figs 5 and 4, we see that these poorly fitted regions are mainly confined to two areas, the first of these being at the tip the lobes where the gradient in the flux is sharpest (Fig. 1). Such edge effects have previously been discussed by H13 and H15 and are likely a result of insufficient image fidelity in these regions. We conclude that fitting here is unlikely to provide a robust measure of the age of the plasma and so this area is excluded from subsequent analysis.

The second area of poorly fitted regions is located coincident with the hotspots. This has also been observed in previous studies at GHz frequencies by H13 and H15, and it appears to be a fairly common feature when fitting to bright hotspots in FR IIs. However, previous studies have been unable to definitively determine the cause of this discrepancy because the investigations were performed at a higher frequency range. The longer wavelengths used within this paper, where the effects of ageing should be negligible, allow us to probe the possible reason why these regions are poorly described by the models. We discuss this further in Section 4.1, but we note here that it is likely to be a real feature of the spectrum, rather than a result of any imaging effects.

Taking the ages provided by the Tribble model⁹ and comparing them to those of previous studies, the spectral age derived by Nandi

et al. (2010) for 3C 452 of only 27 Myr is significantly lower than the age derived within this paper. We discuss this discrepancy further in Section 4.2 but note here that it is likely to be because of the combination of a steeper injection index, a magnetic field strength determined from equipartition and the size of the regions considered in the original study.

The age of 3C 223 provides much better agreement with those derived by Orrú et al. (2010) who find an age of 72 ± 4 Myr, well within our margin of error. While they use similar methods to those of Nandi et al. (2010), we see from Fig. 4 that 3C 223 has far fewer cross-lobe age variations, meaning that the superposition of spectra plays a much less significant role in determining the derived model parameters and age. Similarly, H16 find that the magnetic field strength is 75 per cent of the equipartition value and so remains relatively close to that assumed by Orrú et al. (2010). The ages presented within this paper for 3C 223 are therefore in good agreement with the literature, although additional constraints at GHz frequencies are required if a more accurate age is to be determined. We discuss this further in Section 4.2.

3.4 Lobe advance speeds

In order to determine the speed at which the lobes of our sample are advancing through the external medium, we employ the standard method of Alexander & Leahy (1987). Assuming the source is orthogonal to the line of sight and that hotspots are the primary sites for particle acceleration, a characteristic advance speed v_{lobe} is given simply by $v_{\text{lobe}} = d_{\text{hs}}/t_s$, where d_{hs} is the distance between the core and the hotspot and t_s is the age of the source. Within this paper, we define hotspots to be the bright, flat spectrum emission located near the tip of the lobes where particle acceleration is most likely to be taking place. However, we acknowledge that this does not necessarily fit the strict morphological definition laid out by, for example, Leahy et al. (1997), who define a hotspot as a single distinct feature; its largest dimension is less than 10 per cent of the lobe's major axis, its peak brightness is 10 times the rms noise and it is separated from any nearby peaks by a minimum falling two-thirds less than the fainter peak.

⁹ We choose the Tribble model here as it has previously been shown (H13; H15) to provide the best balance between goodness-of-fit and physical plausibility, although the large errors associated with all of the models mean that this selection makes only a marginal difference for these comparisons.

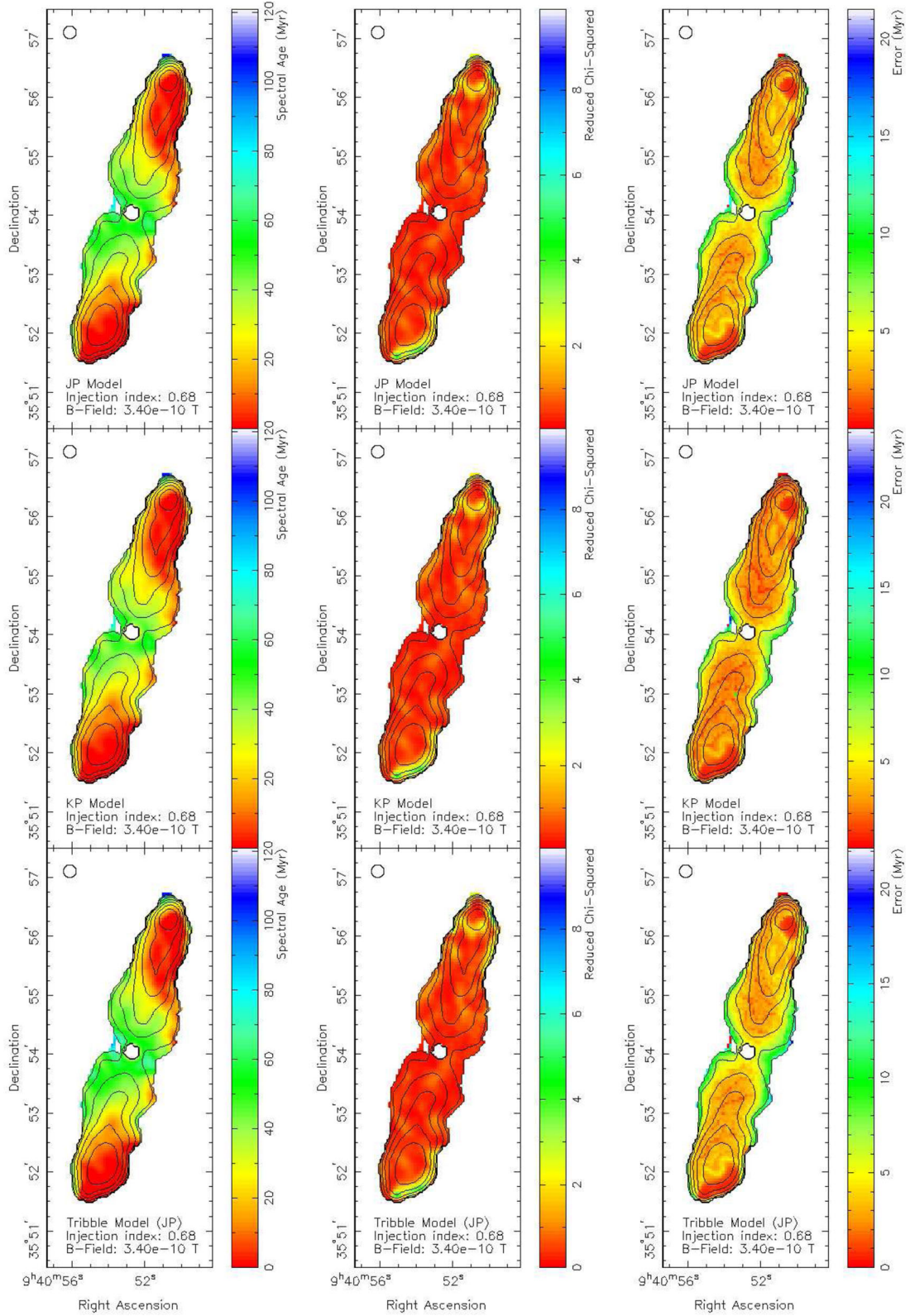


Figure 4. Spectral ageing maps of 3C 223 (left) with corresponding χ^2 (middle) and error maps (right) for the JP (top), KP (middle) and Tribble (bottom) models of spectral ageing. All maps have been overlaid with 1.4-GHz flux contours. A magnetic field strength of 0.34 nT (H16) was used for all fits along with an injection index of 0.68 as described in Section 3.3. The maximum spectral ages of all models are given in Table 4.

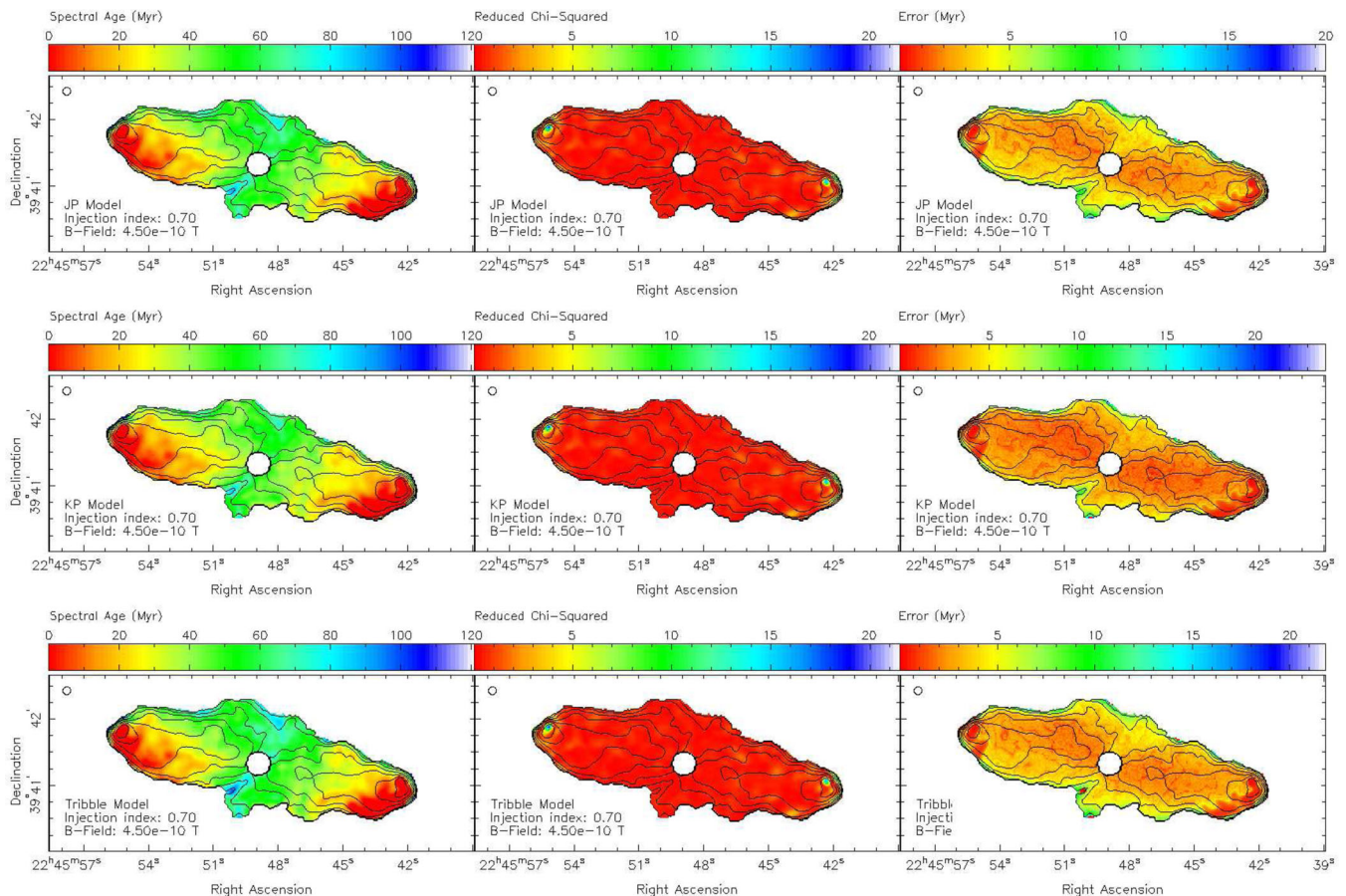


Figure 5. Spectral ageing maps of 3C 452 (left) with corresponding χ^2 (middle) and error maps (right) for the JP (top), KP (middle) and Tribble (bottom) models of spectral ageing. All maps have been overlaid with 1.4-GHz flux contours. A magnetic field strength of 0.45 nT (H16) was used for all fits along with an injection index of 0.70 as described in Section 3.3. The maximum spectral ages of all models are given in Table 4.

Applying this to our sample, we find that 3C 223 is expanding more rapidly, with the northern lobe advancing between $1.33^{+0.06}_{-0.05}$ (Tribble) and $1.53^{+0.08}_{-0.06}$ (KP) $\times 10^{-2} c$ and the southern lobe between $1.37^{+0.06}_{-0.05}$ (Tribble) and $1.58^{+0.08}_{-0.06}$ (KP) $\times 10^{-2} c$. 3C 452 is advancing at roughly half the speed of 3C 223, with the eastern lobe between $0.71^{+0.03}_{-0.03}$ (JP) and $0.82^{+0.04}_{-0.04}$ (Tribble) $\times 10^{-2} c$ and the western lobe between $0.73^{+0.03}_{-0.03}$ (JP) and $0.84^{+0.04}_{-0.04}$ (Tribble) $\times 10^{-2} c$. A summary of the derived characteristic advance speeds for each source and lobe is given in Table 4.

Previous studies of similar, well-established FR IIs (Myers & Spangler 1985; Alexander & Leahy 1987; Liu, Pooley & Riley 1992; O’Dea et al. 2009) find a range of advance speeds from a few to tens of per cent of the speed of light. 3C 452 and 3C 223 therefore fall at the lower end of this scale; however, a direct comparison may not be appropriate in this case. Previous studies make the assumption that, at low frequencies, the integrated spectrum is a superposition of power-law spectra with negligible curvature, because of ageing. Therefore, it provides a robust measure of the injection index. In light of the results of Section 3.3, where we find that the integrated spectrum has the potential to be significantly steeper than the resolved case, and the results of Croston et al. (2005) and H16, who show that the magnetic field strength of these sources is generally less than equipartition (also see the examples by Brunetti et al. 2002; Isobe et al. 2005; Migliori et al. 2007), it is likely that the spectral ages of the sources in these previous studies are under-

estimated, leading to an increased advance speed when compared to well-resolved studies using modern techniques.

Recent investigations of two FR IIs (3C 28 and 3C 438) by H15, where the injection indices were determined on resolved scales (although equipartition was still assumed), have found advance speeds of around 2 per cent of the speed of light, more in line with those of 3C 452 and 3C 223. However, larger samples using resolved techniques are required to conclusively determine whether the characteristic advance speed of FR IIs is lower than previously thought.

4 DISCUSSION

The results presented in Section 3 provide the first opportunity to accurately determine in detail the spectrum of FR IIs at low frequencies on small spatial scales and to investigate the particle acceleration processes that drive their emission, which is vital if we are to determine the life-cycle of radio galaxies and their impact on the external environment. In the following subsections, we discuss the reliability of our results and we compare the results with previous studies. We explore how these findings affect our understanding of the observed spectrum of FR IIs at low frequencies and the dynamics of these powerful radio sources.

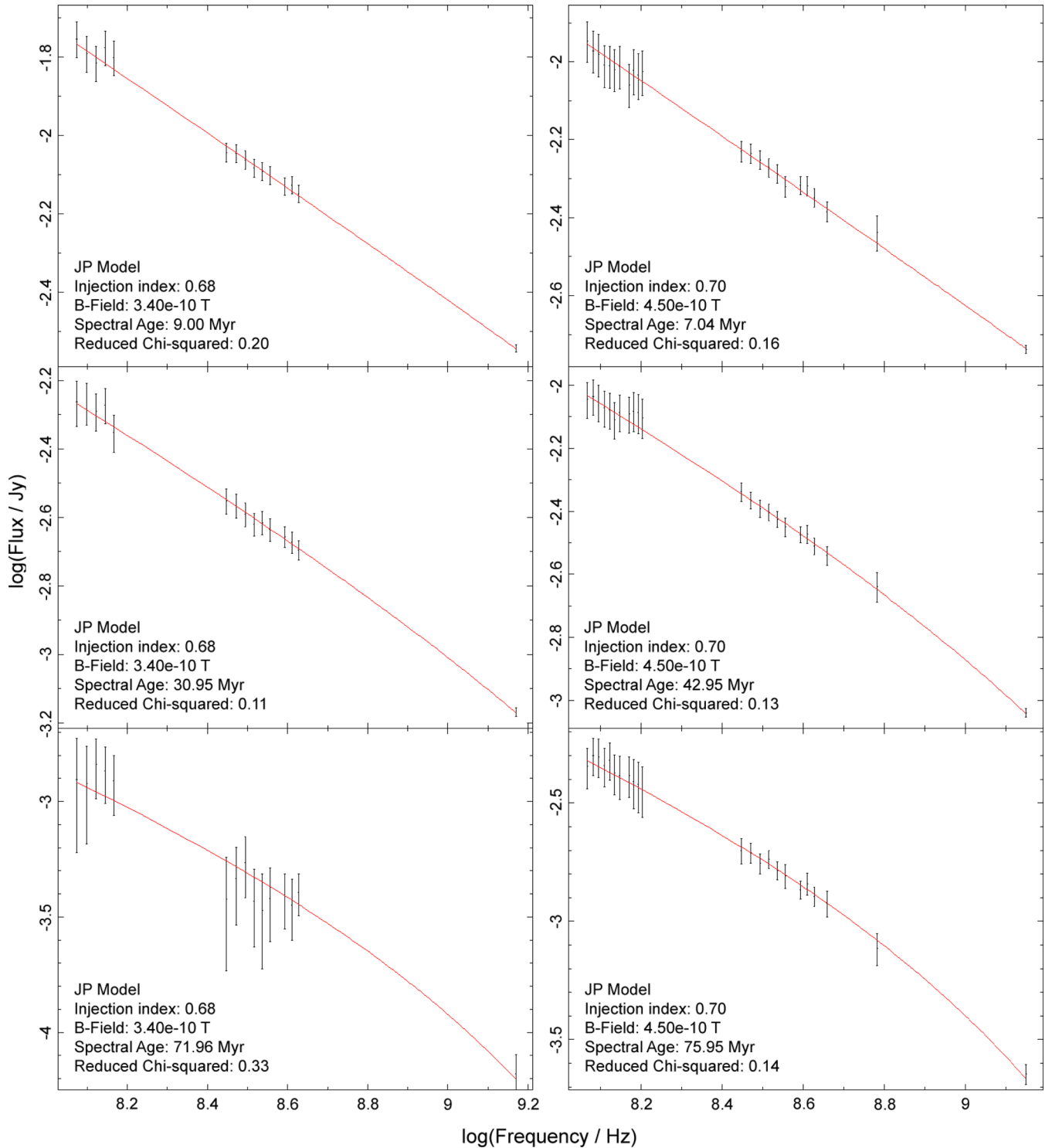


Figure 6. Plots of flux against frequency for a selection of regions in 3C 223 (left) and 3C 452 (right) with the JP model of spectral ageing overlaid (red solid line). Three spectral age ranges are shown: low age (top), moderate age (middle) and high age (bottom). Model parameters, ages (in Myr) and statistics are shown in the bottom-left corner of each panel.

4.1 Initial electron energy distribution and particle acceleration

One of the key recent findings with respect to the parameters of spectral ageing models is that, when tightly constrained over a wide frequency range on small spatial scales, the observed injection index

is significantly steeper than the values of around 0.5–0.6, which have traditionally been assumed.

With the exception of 3C 28 which is thought to be an inactive, remnant radio galaxy, the injection index values are consistent with the previous studies on small spatial scales carried out by [H13](#) and [H15](#), who find values of around 0.7–0.8.

Table 3. Model fitting results. ‘Model’ refers to the spectral ageing model fitted to the target listed in the ‘Source’ column. $\sum \chi^2$ lists the sum of χ^2 over all regions, with an equivalent mean value shown in the ‘Mean χ^2 ’ column. ‘Confidence bins’ lists the number of regions whose χ^2 values fall with the stated confidence range. ‘Rejected’ lists whether the goodness-of-fit to the source as a whole can be rejected. ‘Median confidence’ is the confidence level at which the model can be rejected.

Source	Model	$\sum \chi^2$	Mean χ^2	Confidence bins					Rejected	Median confidence
				<68	68–90	90–95	95–99	≥99		
3C 223	JP	23188	8.85	2285	102	41	80	112	No	<68
	KP	23102	8.82	2281	106	39	80	114	No	<68
	Tribble	23118	8.82	2285	102	41	78	114	No	<68
3C 452	JP	124415	13.42	8384	288	89	136	375	No	<68
	KP	123870	13.36	8391	286	86	136	373	No	<68
	Tribble	124250	13.40	8393	285	84	136	374	No	<68

Table 4. Lobe advance speeds. ‘Model’ is the spectral ageing model fitted to the target listed in the ‘Source’ column. ‘Max age’ is the maximum age of the corresponding ‘Lobe’ in Myr. ‘Angular size’ gives the separation between the core and the hotspot in arcsec, with the corresponding physical size given in the ‘Distance’ column in kpc. ‘Speed’ lists the derived lobe advance speed as a fraction of the speed of light, as detailed in Section 3.4.

Source	Model	Lobe	Max age (Myr)			Angular size (arcsec)	Distance (kpc)	Speed ($10^{-2} v/c$)		
				+	–				+	–
3C 223	JP	North	77.95	13.42	11.73	165.64	346.45	1.450	0.056	0.049
	KP	North	73.96	17.29	13.92	163.20	346.45	1.528	0.076	0.061
	Tribble	North	84.95	15.02	13.83	163.20	346.45	1.330	0.058	0.053
	JP	South	77.95	13.42	11.73	163.20	357.12	1.494	0.056	0.049
	KP	South	73.96	17.29	13.92	163.20	357.12	1.575	0.076	0.061
	Tribble	South	84.95	15.02	13.83	163.20	357.12	1.371	0.058	0.053
3C 452	JP	East	89.05	8.56	7.14	139.32	193.74	0.710	0.031	0.026
	KP	East	85.99	9.70	7.90	139.32	193.74	0.735	0.037	0.030
	Tribble	East	77.05	9.22	8.74	139.32	193.74	0.820	0.039	0.037
	JP	West	89.05	8.56	7.14	146.88	197.86	0.725	0.031	0.026
	KP	West	85.99	9.70	7.90	146.88	197.86	0.750	0.037	0.030
	Tribble	West	77.05	9.22	8.74	146.88	197.86	0.838	0.039	0.037

Interestingly, this is only slightly lower than the average integrated spectral index between 178 and 750 MHz of $\alpha \approx 0.8$ of the 3CRR sample by Laing et al. (1983). This suggests that the model fitting methods used both here and by H13 and H15 are successfully accounting for curvature due to ageing and reliably tracing the low-frequency spectrum, as expected. However, from Fig. 7, which shows the spectral index of 3C 452 and 3C 223 as a function of position (weighted least-squares fit to all data points), it is unclear whether this is truly tracing the initial electron energy distribution.

As discussed in the introduction, the injection index is related to the power-law index, which describes the initial electron energy distribution by equation (4). This energy distribution is then subject to radiative losses, in theory leading to a smooth gradient of spectra between the initial acceleration at the hotspots and the oldest regions of plasma close to the core. From panels C–F of Fig. 7, which show the regions of plasma close to the hotspot, we clearly see, in contradiction to this assumption, a jump in the spectral index from between 0.5 and 0.6 (the historically assumed values) in the hotspots and $\gtrsim 0.7$ (those derived from model fitting and the integrated spectrum) just outside on angular scales, comparable to the resolution of the radio images. For 3C 452, these scales can plausibly be increased because the extended flat spectrum structure connected to the hotspot is a back flow of material that, while not explaining the cause of the steepening, would allow additional time for such a process to occur. However, this cannot be the case for 3C 223 where such an extension is not present. Hence, this rapid spectral steepening must either occur on physical scales less than

approximately 10 and 30 kpc for 3C 452 and 3C 223, respectively, or come from additional processes modifying the observed spectrum of the hotspots relative to that of the lobes.

As previously mentioned in Section 3.3, the effects of spectral ageing are significantly reduced when observed well below the break frequency, ν_t , given in GHz by

$$\nu_t = \frac{(9/4) c_7 B}{(B^2 + B_{\text{CMB}}^2)^{1/2} t^2}, \quad (5)$$

where t is the age of the source in Myr, B is the magnetic field strength in nT, $B_{\text{CMB}} = 0.318(1+z)^2$ nT is the equivalent magnetic field strength for the CMB and $c_7 = 1.12 \times 10^3$ nT³ Myr² GHz is a constant defined by Pacholczyk (1970). For a maximum spectral age of 80 Myr, the break frequency in any region of plasma within our observations must be above 1.53 and 1.65 GHz for 3C 452 and 3C 223, respectively. This suggests that spectral curvature should play a negligible role at LOFAR and P-band wavelengths for the sources in our sample, particularly when close to the acceleration regions. This appears to be borne out in our spectral fitting where both sides of the discontinuity are well fitted by a power law (Fig. 7) with no significant signs of curvature (zero age emission of Figs 4 and 5) and can therefore be ruled out as the cause of the spectral steepening.

One factor that is currently unaccounted for in spectral ageing models is adiabatic expansion. This process is well known to occur in hotspots, reducing the value of γ_{min} from possibly as high as 1000 (Carilli et al. 1991; Hardcastle et al. 1998) to ~ 10 (Godfrey et al. 2009) for the lobes. However, while adiabatic expansion can

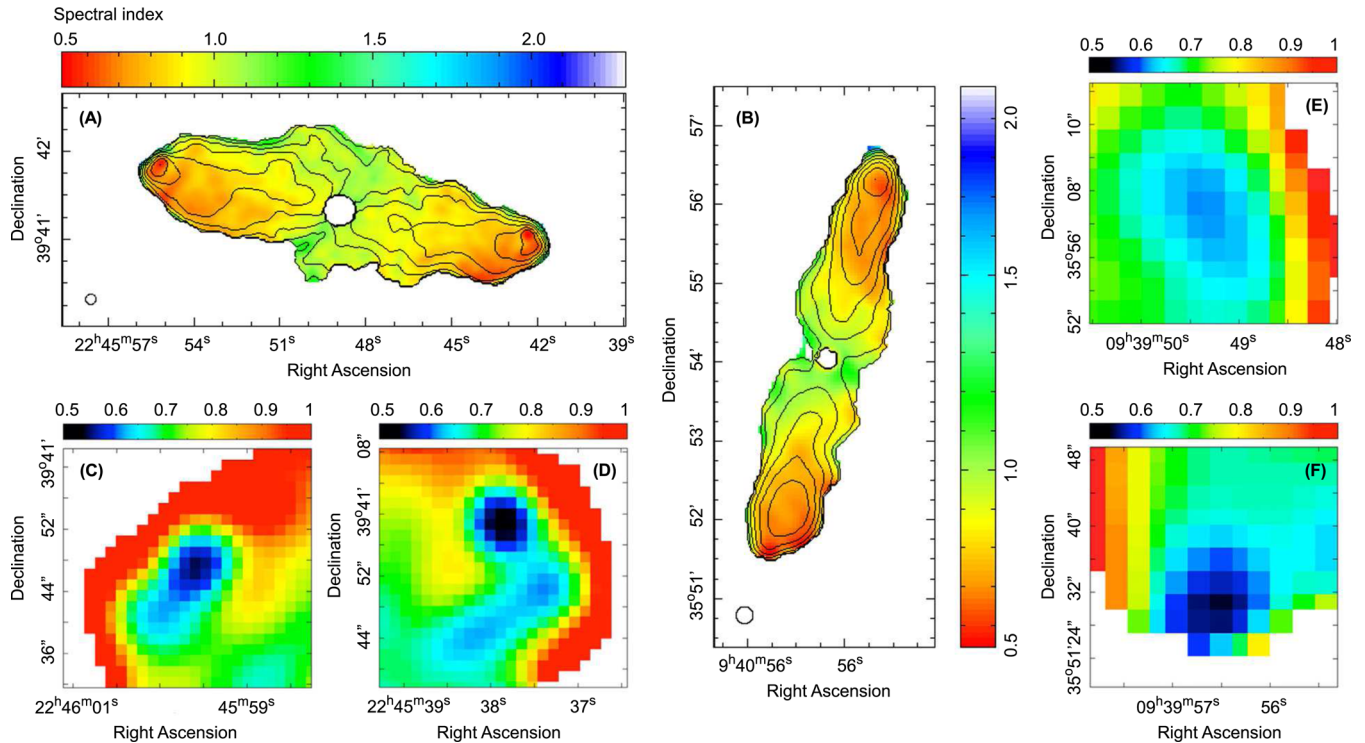


Figure 7. Spectral index maps of 3C 452 (A) and 3C 223 (B) with 1.4-GHz flux contours overlaid and a standard min–max colour scale. The restoring beams of 6 and 13 arcsec for 3C 452 and 3C 223, respectively, are indicated in the bottom-left corner of the images. Panels C–F are zoomed to regions surrounding the hotspots for each source, with the colour scale set to highlight the differences in these spectrally flatter regions of plasma. Note that the jump between $\alpha \approx 0.5$ and $\alpha \approx 0.7$ is not because of the curvature, as discussed in Section 4.1.

cause the break in a curved spectrum to move to lower frequencies, the lack of curvature in these regions means that adiabatic expansion alone will only reduce the intensity of the emission, not increase the steepness of its spectrum. We can therefore confidently rule out adiabatic expansion in homogeneous models alone as the cause of the observed disparity.

Another possible explanation is that the observed spectrum results from the combination of adiabatic expansion, strong magnetic field strengths and the superposition of a range of high-energy cut-offs. The observed emission of the recently accelerated plasma at any given frequency is given by¹⁰

$$S(\nu) = \int_0^\pi \int_{E_{\min}}^{E_{\max}} J(\nu) N(E) dE d\theta, \quad (6)$$

where $N(E)$ is the initial electron energy distribution given by equation (1) and $J(\nu)$ is the emissivity of a single electron given by

$$J(\nu) = \frac{\sqrt{3}e^3}{8\pi\epsilon_0 cm_e} F(x) B \sin^2 \theta. \quad (7)$$

Here, B is the magnetic field strength, θ is the pitch angle of the electron to the magnetic field and $F(x)$ is a constant defined by Pacholczyk (1970), where $x = \nu/\nu_c$ is a function of the critical frequency of the electron; see H13 for further details and see Longair (2011) for a full derivation.

While it is generally assumed that we always observe a single high-energy cut-off (E_{\max}) for the plasma injected into the lobes,

this does not have to be the case. In principle, if the jet plasma is initially accelerated to the observed power law of $\alpha_{\text{HS}} \approx 0.5$ in the hotspot (as one would expect from, for example, first-order Fermi acceleration; Blandford & Ostriker 1978) but there is a significant variance in the high-energy cut-offs, this may result in a steeper than expected spectrum once injected into the lobes. At the point of acceleration, all of these cut-offs are likely to be well above the observed frequency range. However, as this region of frequency space is no longer a power law, they would be driven to lower energies by the rapid adiabatic expansion and strong magnetic field strengths known to exist in hotspots (e.g. Hardcastle, Birkinshaw & Worrall 1998; Hardcastle et al. 2002; Araudo, Bell & Blundell 2015). As the plasma enters the lobe where the magnetic field strength and adiabatic expansion are relatively weak, these high-energy cut-offs (prior to the effects of ageing) become fixed and the observed superposition of these spectra within any given beam may explain the observed rapid steepening of the power-law spectrum. As a result, the E_{\max} term of equation (6) would instead be the sum of a distribution of energy cut-offs, something that is currently not described by models of spectral ageing or radio galaxy dynamics.

While plausible, observations of hotspots at higher energies suggest that such a superposition of cut-offs is unlikely to be the case for all sources because of the observed optical and infrared emission present in the hotspots of at least some FR IIs (e.g. Keel & Martini 1995; Meisenheimer, Yates & Roeser 1997; Werner et al. 2012). This is generally agreed to be a result of synchrotron emission arising from the same electron population that produces the radio emission (e.g. Prieto, Brunetti & Mack 2002; Mack et al. 2009). Thus, such a cut-off cannot be present if the observed spectrum between radio and optical frequencies is to be maintained. Unfortunately, the large angular size of 3C 452 and 3C 223 means that suitable images

¹⁰ Note that the Tribble model is additionally integrated over the Maxwell–Boltzmann distribution. See Hardcastle (2013) and H13 for further details.

at optical wavelengths (e.g. from the *Hubble Space Telescope*) of the hotspot regions are not available because of the relatively small field of view and because observations are generally centred on the host galaxy. However, if such a disparity between the spectrum of the lobe and hotspot emission is common to FR IIs, it is non-trivial to unify a superposition of high-energy cut-offs with the observed power-law spectrum of the optical hotspots.

Perhaps the most plausible argument for the rapid steepening of the spectrum concerns the additional processes modifying the observed hotspot emission. A recent study by McKean et al. (2016), who investigated the low-frequency turnover in the hotspots study of Cygnus A, has found that the long assumed low-energy cut-off (LEC) alone is unable to explain the observed spectrum when constrained by spatially well-resolved LOFAR low-frequency observations. The conclusion is that at least some significant contribution from absorption processes must be present.

While Cygnus A, because of its large angular size, is currently the only source for which it has been possible to perform such a detailed analysis of absorption in hotspots, these processes are able to account for the observed spectral flattening seen at lower resolutions without the need to invoke the narrow range of conditions that would be required for the superposition of high-energy cut-offs described above. While no turnover is observed in the hotspots of either 3C 452 or 3C 223, this is likely to be because of their relatively small angular size, which results in contamination from lobe emission. This emission may also conceal any minor curvature or break in the intrinsic spectrum of the hotspot, hiding the presence of any stochastic acceleration mechanisms such as those discussed by Prieto et al. (2002). Under such conditions, the spectrum may become stretched and may flatten at lower energies, which, once adiabatic expansion within the hotspot is taken into account, would lead us to observe the portion of the spectrum in the lobes that is not modified by these stochastic processes.

Additional effects may also arise from non-homogeneous conditions within the hotspots, particularly with respect to variations in magnetic field strength or if there is a complex magnetic field topology. As this would lead to the electron population of the hotspots ageing differently from those of the lobes, the synchrotron spectrum may not be linked to that of the underlying electron population in a straightforward manner. Therefore, we suggest that absorption processes, possibly in combination with stochastic processes and/or non-homogeneous conditions, are the most likely cause of the observed disparity. Perhaps most importantly, this suggests that the low-frequency spectrum of hotspots is not representative of the underlying initial electron energy distribution. Regardless of the cause, if we are to understand the impact on the wider FR II population, then determining whether such a discontinuity exists in the majority of FR IIs is vital going forward.

4.2 Spectral ages and their robustness

As noted in Section 3.3, all of the models tested are able to provide a good description of the observed spectrum with uncertainties in the region of 10–20 per cent for the oldest regions of plasma. Although these uncertainties are much larger than those of studies at GHz wavelengths, this is not surprising because, while the low-frequency data used in this paper provide excellent insight into the low-energy electron population and constrain parameters such as the injection index, we see from equation (5) that for a spectral age of 80 Myr the break frequencies for 3C 452 and 3C 223 are both $\nu_t \approx 1.5$ GHz and so curvature due to ageing is dominated by a single data point. In the context of the current investigation, such

uncertainties are more than sufficient to reach our desired scientific aims but we emphasize the need for broad-band observations well above the break frequency if high-precision ages are to be obtained.

While the ages presented in this paper agree well with previous studies for 3C 223, the lack of higher-frequency observations raises the question of whether this is the cause of the age discrepancy for 3C 452. Nandi et al. (2010) use two additional observations at 4.91 and 8.35 GHz (not suitable for this study because of their lower resolution), which should probe well past the break frequency in the oldest regions of plasma and provide more robust ages. However, there are a number of additional factors that must be considered when determining which, if either, of these ages is correct. The first, and most straightforward to determine, is that of the injection index and magnetic field strength. The injection index of Nandi et al. (2010) was derived in a similar manner to the methods used here, but it was far less well constrained at low frequencies (which dominates the model-dependent determination of the injection index) and used much larger spatial regions, which are known to affect the derived values (e.g. Stroe et al. 2014; Kapinska et al. 2015; Harwood 2017). Equipartition between the radiating particles and the magnetic field strength is also assumed in this case, resulting in a higher value of $B_{eq} \approx 0.8$ nT but, as shown by H16 through synchrotron/inverse-Compton fitting, the magnetic field strength of 3C 452 is only around half this value. In combination with the steeper injection index, we see from equation (6) that this will naturally lead to younger ages. However, fixing these parameters to those of Nandi et al. (2010) and refitting the JP model, we find a maximum age of only around 45 Myr. These variations can therefore only partly account for the difference in age.

An additional factor, which was not accounted for in previous studies, is that of cross-lobe age variations and the superposition of spectra, which can also have an impact on the derived age of a source. Traditional methods for deriving the spectral age as a function of position (and that used by Nandi et al. 2010) have generally relied on the assumption that, while ages within the lobe increase towards the core, transverse variations are negligible, allowing ‘slices’ to be taken across the lobe in order for the required signal-to-noise level to be reached. While, for sources such as 3C 223 this is a reasonable (if not perfect) assumption to make, it is evident from Fig. 5 that this is not the case for 3C 452. As the superposition of these spectra does not simply result in an averaged spectrum but in a more complex model of emission, this effect is likely to be another significant factor contributing to the observed difference in spectral age compared to previous results. The violation of this assumption appears to be fairly common in FR IIs and has been discussed in detail by H13 and H15. The results presented here further support the need for model fitting to be performed on small spatial scales in order to reduce these effects if reliable ages are to be determined.

Because of improved constraints on the injection index and magnetic field strength, along with the known superposition of spectra and cross-lobe variations in the lower-resolution study, we conclude that the age of 3C 452 has been previously underestimated and the values presented within this paper are robust for the given models.

4.3 Revised energetics

As noted in Section 3.1, the angular size of 3C 452 as measured from the 368-MHz VLA image differs from that of the original values of Laing et al. (1983). Therefore, we take this opportunity to remeasure the parameters used by Croston et al. (2004, 2005) – and subsequently H16, who made a direct comparison – to ensure that the values used to derive the source volumes, and subsequent total

Table 5. Source energetics and dynamical ages. ‘Lobe’ gives the region considered in subsequent columns for the target listed in the ‘Source’ column. ‘Length’ and ‘Radius’ list the physical dimensions of the fitted region used to derive the ‘Volume’ and ‘Energy density’. Here, the term energy density refers to the sum of the energy density in the radiating particles, the magnetic field and any non-radiating particles, such as protons, as used by H16. ‘ p_{int} ’ lists the internal pressure of the source with ‘ ϵ ’, ‘ kT ’ and ‘ Q ’ being the parameters used in determination of the dynamical age, ‘ t_{dynamic} ’. Note that dynamical model values are not available for 3C 223, as detailed in Section 4.4.

Source	Lobe	Length (kpc)	Radius (kpc)	Energy density (J m ⁻³)	Volume (m ³)	ϵ	p_{int} (Pa)	kT (keV)	Q (W)	t_{dynamic} (Myr)
3C 223	Northern	404	67.8	3.90×10^{-13}	1.71×10^{65}	–	1.3×10^{-13}	–	–	–
3C 223	Southern	390	67.8	3.85×10^{-13}	1.65×10^{65}	–	1.3×10^{-13}	–	–	–
3C 452	Total	418	33.6	3.16×10^{-12}	1.14×10^{65}	0.2	1.1×10^{-12}	0.86	7.6×10^{37}	152

energy content of the lobes, are robust. We find that for both 3C 452 and 3C 223, even with the additional emission observed as a result of the low frequencies and increased sensitivity, the volumes are smaller than those found previously. This is most likely because of the lower-resolution images used in the original studies and it leads to an increased total energy content for both sources, the revised values for which are given in Table 5. This does not significantly affect the findings of H16 as it only acts to further increase the internal pressure of these sources and provides additional support for the conclusion that both sources are at minimum in pressure balance with the external medium.

Uncertainty in the energetics of FR IIs because of their size and, as discussed by H16, low-frequency spectrum is perhaps currently a bigger concern to our understanding of the impact these sources have on their environment than any uncertainties in, for example, their intrinsic age (discussed further in Section 4.4). However, upcoming radio surveys such as the LOFAR Two-metre Sky Survey (LOTSS; Shimwell et al. 2017) and the MeerKAT MIGHTEE survey (Jarvis 2012) will provide a large number of well-resolved sources over a wide frequency range. So, this problem should be relatively straightforward to resolve, based on our new understanding of radio galaxy spectra in the near future.

4.4 Dynamical ages

To estimate the dynamical ages of these sources, which extend well beyond the core radii of their host groups, we need a model that can take account of the density profile, rather than assuming a constant external density, as in H15, or a power law in density, as in Kaiser & Alexander (1997).

We consider a toy model of the expanding radio lobe as a cylinder with length R and cross-sectional area $A = \epsilon R^2$, where ϵ is effectively a measurement of the aspect ratio: $\epsilon = V/R^3$. Then, assuming non-relativistic growth of the source, ram pressure balance requires that

$$\rho_{\text{ext}} \left(\frac{dR}{dt} \right)^2 = p_{\text{int}} - p_{\text{ext}}. \quad (8)$$

The external pressure and density profiles (functions of R) are provided by the modelling of the X-ray observations. Let the one-sided jet power be Q and assume that the jet is light and relativistic so that the jet momentum flux is Q/c ; this momentum flux is distributed over the front area A of the lobe. Then, p_{int} contains a term from this momentum flux and also one from the energy stored in the lobes. We assume that the lobes are filled with a light, relativistic fluid, so that $p = U/3$, and that, as found in simulations (Hardcastle & Krause 2014; English, Hardcastle & Krause 2016), about half of the total energy supplied by the jet goes into heating the shocked material between the bow shock and the contact discontinuity (which, as it is necessarily in pressure balance with lobe

material at the lobe head, we need not consider further here). Then we have

$$\rho_{\text{ext}} \left(\frac{dR}{dt} \right)^2 = \frac{Q}{c\epsilon R^2} + \frac{Qt}{6\epsilon R^3} - p_{\text{ext}}, \quad (9)$$

where

$$\rho_{\text{ext}} = \rho_0 \left[1 + \left(\frac{r}{r_c} \right)^2 \right]^{-3\beta/2} \quad (10)$$

and

$$p_{\text{ext}} = \rho_{\text{ext}} kT / \nu. \quad (11)$$

If we further assume that ϵ is a constant (effectively a self-similar assumption), then the resulting non-linear differential equation for R can be solved numerically for a given Q and external conditions, given some initial condition of the form, e.g. $R = ct$ for $t \ll 1$ Myr (as the equations are singular at $R = 0$, $t = 0$). The simplifying assumption on ϵ is not really justified, as numerical modelling shows that it varies systematically over the lifetime of a source. However, detailed modelling would have to consider not just the transverse growth of the source but also the behaviour of the swept-up material behind the bow shock, which is beyond what is required for the present paper. When the solution of equation (9) is compared with the results of numerical simulation of light, relativistic jets, we see reasonably good agreement on time-scales of a few tens of Myr (English et al. 2016). Differences at early times can be attributed partly to the constant ϵ assumption and partly to the fact that jets in the numerical models are artificially weak at early times because of the coupling of the internal boundary condition to the grid.

The most striking difference is an acceleration of the expansion of the numerical models at late times, which is not observed in the solutions to equation (9). This is because at late times in the models (and in real radio sources) the hot gas pushes the lobes away from the centre of the cluster, so that the lobe volume grows more slowly, and the internal pressure falls less rapidly, than equation (9) would imply. To infer the dynamical age from such a model, we measure a source’s physical lobe size R and the energy content of a lobe $E = Qt/2$ (again adopting the factor of 2 from simulations). We also measure the current value of the lobe aspect ratio parameter $\epsilon = V/R^3$. From a family of solutions to equation (9), we can then determine the values of t and Q that most closely satisfy these constraints. The divergence from numerical models once the lobes have moved out from the cluster centre means that these dynamical ages will tend to be overestimates for large age values, but should be reasonable for the two sources we are considering.

Applying the revised values of Table 5 to the models outlined above, we are able to derive a dynamical age for comparison with its spectral counterpart. Unfortunately, for 3C 223, a combination of low-energy density, the extreme beta model parameters from

the *XMM* fits of Croston et al. (2004) and the large core radius of ~ 300 kpc means that the dynamical models produce unrealistically high dynamical ages of the order of Gyr. This results from the low-energy densities forcing the models to low jet powers and a large expansion time through what is, for a significant fraction of its lifetime, a near constant density environment. As noted by H16, the existing X-ray measurements for 3C 223 are highly uncertain and so the beta models and temperature are poorly constrained. Therefore, we conclude that the dynamical model of 3C 223 does not currently provide realistic values for the source's age suitable for comparison with the spectral ages derived within this paper.

In the case of 3C 452 where we are able to place better constraints on the model parameters, we derive a dynamical age of 152 Myr, almost double that determined from a spectral point of view. Such disparities are not uncommon and have long been the topic of discussion (e.g. Eilek & Arendt 1996; H13) but it has recently been suggested that a simple departure from equipartition between the relativistic particles in the lobes and the magnetic field may be able to resolve such differences in certain cases (e.g. H15; Turner, Shabala & Krause, submitted). However, as for 3C 452, the magnetic field strength is determined through synchrotron/inverse-Compton model fitting (Croston et al. 2004, 2005; H16) and this cannot be the cause of the observed disparity between the derived ages.

One possibility is that models of spectral ageing currently do not accurately represent the intrinsic age of FR IIs, a matter that has been the subject of much debate (e.g. Alexander & Leahy 1987; Eilek 1996; Eilek et al. 1997; Blundell & Rawlings 2000). The need for new and updated models, which account for our improved knowledge of radio galaxies, has been highlighted both in the case of integrated models of spectral ageing, which, when tightly constrained, are unable to reproduce an accurate description of radio galaxy spectra (Harwood 2017), and by the success of the Tribble model on well-resolved scales (Tribble 1993; Hardcastle & Krause 2013; H13; H15) in providing a potentially more realistic description of the magnetic field structure. However, these changes alone are not sufficient to account for the large age differences observed. Therefore, if the underestimation of the spectral age is the primary cause of the disparity, additional factors, such as the source's evolutionary history (e.g. variance in jet power, environment, magnetic field evolution), must be accounted for within the models if they are to provide a reliable measure of a source's intrinsic age.

Alternatively (or perhaps, additionally), the cause of the disparity may lie in the assumptions made within the dynamical models. In a similar way to ages derived from a spectral point of view, these naïve models do not fully account for the complex dynamics occurring over the lifetime of a source and model parameters are often poorly constrained. This is highlighted by 3C 223 where, although the model presented here accounts for a more realistic scenario than a constant or power-law density profile, the dynamical model is unable to determine a robust age. Potentially more realistic dynamical models are currently under development (Hardcastle et al., in preparation) but preliminary results suggest that these only serve to further the disparity. Because of the limited number of sources on which such an analysis has been performed, both dynamically and using the small-scale spectral techniques used within this paper, it is unclear if new dynamical models or simply tighter constraints are needed.

Determining conclusively the intrinsic age of radio galaxies remains an open question. While the difference in spectral ages between studies can be explained in the context of the current models, it emphasizes the need for parameters to be well constrained on

small scales if reliable ages are to be determined, particularly the injection index and magnetic field strengths. Other considerations, such as older regions of plasma being below the sensitivity limit of the telescope and the mixing of electron populations, mean that the spectral ages may also only represent a lower limit on the intrinsic age of a radio source. In the context of the total energy output over the course of a galaxy's lifetime and through all phases of activity, this is further complicated by the need to consider possible recurrent activity in FR IIs. Commonly known as double-doubles, recurrent activity has been observed in a number of radio galaxies (e.g. Lara et al. 1999; Schoenmakers et al. 2000; Saikia, Konar & Kulkarni 2006) and it has previously been suggested that 3C 452 possesses such a morphology. However, a detailed multifrequency analysis by H16 was unable to find any further evidence of remnant lobes. In either case, the analysis that has been carried out within this paper only considers the current phase of activity.

Ultimately, full numerical simulations of FR IIs that include spectral ageing, and are able to account for many more parameters than the simple models presented here, are required (English et al., in preparation) and may prove to be the long-term solution in determining the dynamical age and improving spectral ageing models. Large samples provided by upcoming surveys will be key to this process, providing the physical parameters for these simulations and additional information on how the spectral and/or dynamical models should be updated in order to provide an accurate description of FR IIs.

5 CONCLUSIONS

In this paper we have presented the first well-resolved spectral ageing study of FR IIs at low (<300 MHz) frequencies, which we use to study the low-energy electron distribution and particle acceleration processes occurring in the two nearby radio galaxies, 3C 452 and 3C 223, uncovering previously unknown features within their spectrum. Addressing the primary science questions posed in the introduction, we find the following.

(i) When considered on small spatial scales, the spectrum that describes the low-energy electron population remains steeper and is more complex than historically assumed. A rapid spectral steepening is observed in both sources at the boundary between the hotspot and lobe regions, suggesting that hotspot spectra are not representative of the initial electron energy distribution. We suggest that this is a result of absorption processes and/or non-homogeneous and additional acceleration mechanisms within the hotspots. We caution against using such measurements in determining the injection index of FR IIs.

(ii) The injection index (as derived from the lobe emission) remains steep even when considered at low frequencies and on small spatial scales, consistent with previous findings. The spectral ages of our target sources are $77.05^{+9.22}_{-8.74}$ and $84.95^{+15.02}_{-13.83}$ Myr (Tribble model) for 3C 452 and 3C 223, respectively.

(iii) Even when a non-equipartition magnetic field strength is assumed, a disparity of a factor of ~ 2 is observed between the ages of 3C 452 when considered from spectral and dynamical point of view. It remains unclear whether the spectral or dynamical models, or both, are the cause of this disparity, but upcoming simulations that include spectral ageing may help to resolve this issue.

(iv) The questions raised by these findings have potentially significant implications for our understanding of radio galaxies with respect to their age, energetics and the underlying processes that drive emission in these powerful radio sources. It is clear that for

the two sources investigated, the total energy contained within the lobes is much higher than previously thought, but analysis of upcoming large surveys is required to determine the impact on the population as a whole.

In addition to these primary science questions, we also find the following.

- (v) A faint extension not present in higher-frequency observations is detected in the northern lobe of 3C 223.
- (vi) Revised measurements of 3C 223 at 368 MHz find its physical size to be 796 kpc, placing it within the giant radio galaxy classification range.
- (vii) The lobes of both sources are advancing through the external medium at around 1 per cent of the speed of light.
- (viii) Significant cross-lobe variations are again observed, reinforcing the need to perform fitting on small spatial scales if accurate spectral ages are to be derived.

In order to explore further the observed disparity and particle acceleration processes in hotspots, subarcsecond-resolution imaging and the spectrum of hotspots in a larger sample of FR II sources will be presented in a later paper in this series.

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